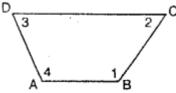
Quadrilateral

IMPORTANT POINTS

4.Quadrilateral: A quadrilateral is a plane figure enclosed by four sides. It has four sides, four interior angles and four vertices.



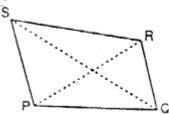
In quadrilateral ABCD, shown alongside:

(i) four sides are : AB, BC, CD and DA.

(ii) four angles are : $\angle ABC$, $\angle BCD$, $\angle CDA$ and $\angle DAB$; which are numbered $\angle 1$, $\angle 2$, $\angle 3$ and $\angle 4$ respectively.

(iii) four vertices are : A, B, C and D.

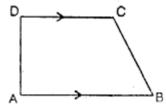
5. Diagonals of a Quadrilateral : The line segments joining the opposite vertices of a quadrilateral are called its diagonals.



The given figure shows a quadrilateral PQRS with diagonals PR and QS.

6. Types of Quadrilaterals :

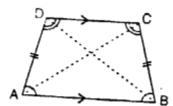
1. Trapezium: A trapezium is a quadrilateral in which one pair of opposite sides are parallel.



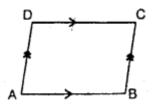
The figure, given alongside, shows a trapezium as its sides AB and DC are parallel i.e. AB \parallel DC.

When the non-parallel sides of the trapezium are equal in length, it is called an isosceles trapezium.

The given figure shows a trapezium ABCD whose non-parallel sides AD and BC are equal in length i.e. AD = BC; therefore it is an isosceles trapezium.



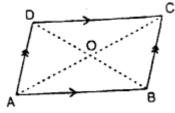
Also, in an isosceles trapezium :



(i) base angles are equal:
i.e. ∠A = ∠B and ∠D =∠C
(ii) diagonals are equal
i.e. AC = BD.

2.Parallelogram : A parallelogram is a quadrilateral, in which both the pairs of opposite sides are parallel.

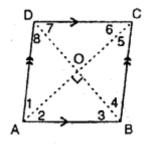
The quadrilateral ABCD, drawn alongside, is a parallelogram; since, AB is parallel to DC and AD is parallel to BC i.e.



AB || DC and AD || BC. Also, in a parallelogram ABCD: (i) opposite sides are equal: i.e. AB = DC and AD = BC. (ii) opposite angles are equal: i.e. $\angle ABC = \angle ADC$ and $\angle BCD = \angle BAD$ (iii) diagonals bisect each other : i.e. OA = OC = $\frac{1}{2}$ AC and OB = OD = $\frac{1}{2}$ BD.

7. Some special types of Parallelograms

(a) Rhombus : A rhombus is a parallelogram in which all its sides are equal.

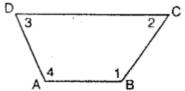


∴In a rhombus ABCD :
(i) opposite sides are parallel:
i.e. AB||DC and AD||BC.
(ii) all the sides are equal:
i.e. AB = BC = CD = DA.
(iii) opposite angles are equal:

i.e. $\angle A = \angle C$ and $\angle B = \angle D$. (iv) diagonals bisect each other at right angle : i.e. $OA = OC = \frac{1}{2}AC$; $OB = OD = \frac{1}{2}BD$. and $\angle AOB = \angle BOC = \angle COD = \angle AOD = 90^{\circ}$ (v) diagonals bisect the angles at the vertices : i.e. $\angle 1 = \angle 2$; $\angle 3 = \angle 4$; $\angle 5 = \angle 6$ and $\angle 7 = \angle 8$.

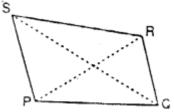
IMPORTANT POINTS

4.Quadrilateral: A quadrilateral is a plane figure enclosed by four sides. It has four sides, four interior angles and four vertices.



In quadrilateral ABCD, shown alongside: (i) four sides are : AB, BC, CD and DA. (ii) four angles are : $\angle ABC, \angle BCD, \angle CDA$ and $\angle DAB$; which are numbered $\angle 1, \angle 2, \angle 3$ and $\angle 4$ respectively. (iii) four vertices are : A, B, C and D.

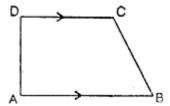
5. Diagonals of a Quadrilateral : The line segments joining the opposite vertices of a quadrilateral are called its diagonals.



The given figure shows a quadrilateral PQRS with diagonals PR and QS.

6. Types of Quadrilaterals :

1. Trapezium: A trapezium is a quadrilateral in which one pair of opposite sides are parallel.

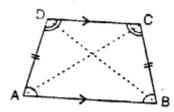


The figure, given alongside, shows a trapezium as its sides AB and DC are parallel i.e. AB || DC.

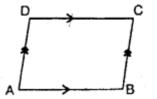
When the non-parallel sides of the trapezium are equal in length, it is called an isosceles trapezium.

The given figure shows a trapezium ABCD whose non-parallel sides AD and BC are

equal in length i.e. AD = BC; therefore it is an isosceles trapezium.



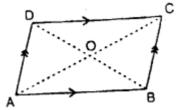
Also, in an isosceles trapezium :



(i) base angles are equal: i.e. $\angle A = \angle B$ and $\angle D = \angle C$ (ii) diagonals are equal i.e. AC = BD.

2.Parallelogram : A parallelogram is a quadrilateral, in which both the pairs of opposite sides are parallel.

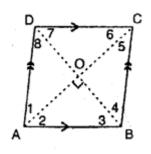
The quadrilateral ABCD, drawn alongside, is a parallelogram; since, AB is parallel to DC and AD is parallel to BC i.e.



AB || DC and AD || BC. Also, in a parallelogram ABCD: (i) opposite sides are equal: i.e. AB = DC and AD = BC. (ii) opposite angles are equal: i.e. $\angle ABC = \angle ADC$ and $\angle BCD = \angle BAD$ (iii) diagonals bisect each other : i.e. OA = OC = $\frac{1}{2}$ AC and OB = OD = $\frac{1}{2}$ BD.

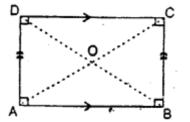
7. Some special types of Parallelograms

(a) Rhombus : A rhombus is a parallelogram in which all its sides are equal.



:. In a rhombus ABCD : (i) opposite sides are parallel: i.e. AB||DC and AD||BC. (ii) all the sides are equal: i.e. AB = BC = CD = DA. (iii) opposite angles are equal: i.e. $\angle A = \angle C$ and $\angle B = \angle D$. (iv) diagonals bisect each other at right angle : i.e. $OA= OC = \frac{1}{2} AC$; $OB = OD = \frac{1}{2} BD$. and $\angle AOB = \angle BOC = \angle COD = \angle AOD = 90^{\circ}$ (v) diagonals bisect the angles at the vertices : i.e. $\angle 1 = \angle 2; \angle 3 = \angle 4; \angle 5 = \angle 6$ and $\angle 7 = \angle 8$.

(b) Rectangle : A rectangle is a parallelogram whose any angle is 90°. A rectangle is also defined as a quadrilateral whose each angle is 90°.



Note : If any angle of a parallelogram is 90°; automatically its each angle is 90°; the reason being that the opposite angles of a parallelogram are equal. Also, in a rectangle:

(i) opposite sides are parallel.

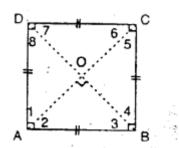
(ii) opposite sides are equal.

(iii) each angle is 90°.

(iv) diagonals are equal.

(v) diagonals bisect each other.

(c) Square : A square is a parallelogram, whose all side are equal and each angle is 90°.



A square can also be defined as :

(i) a rhombus whose any angle is 90°. (ii) a rectangle whose all sides are equal. (iii) a guadrilateral whose all sides are equal and each angle is 90°. ∴ If ABCD is a square : (i) all its sides are equal, i.e. AB = BC = CD = DA(ii) each angle of it is 90°. i.e. $\angle A = \angle B = \angle C = \angle D = 90^{\circ}$. Also, (iii) diagonals are equal. i.e. AC = BD. (iv) diagonals bisect each other at 90°. i.e. $OA = OC = \frac{1}{2}AC;OB = OD = \frac{1}{2}BD$ and $\angle AOB = \angle BOC = \angle COD = \angle DOA = 90^{\circ}$. Since, diagonals AC and BD are equal; therefore ; OA = OC = OB = OD. (v) diagonals bisect the angles at the vertices i.e. $\angle 1 = \angle 2 = 45^{\circ}$ [:: $\angle 1 + \angle 2 = 90^{\circ}$] Similarly: $\angle 3 = \angle 4 = 45^\circ$: $\angle 5 - \angle 6 = 45^{\circ}$ and $\angle 7 = \angle 8 = 45^{\circ}$.

EXERCISE 27 (A)

Question 1.

Two angles of a quadrilateral are 89° and 113°. If the other two angles are equal; find the equal angles.

Solution:

Let the other angle = x° According to given, $89^{\circ} + 113^{\circ} + x^{\circ} + x^{\circ} = 360^{\circ}$ $2x^{\circ} = 360^{\circ} - 202^{\circ}$ $2x^{\circ} = 158^{\circ}$ $x^{\circ} = \frac{158}{2} = 79^{\circ}$ \therefore other two angles = 79° each

Question 2.

Two angles of a quadrilateral are 68° and 76°. If the other two angles are in the ratio 5 : 7; find the measure of each of them.

Solution:

Two angles are 68° and 76° Let other two angles be 5x and 7x $\therefore 68^{\circ}+76^{\circ}+5x + 7x = 360^{\circ}$ $12x + 144^{\circ} = 360^{\circ}$ $12x = 360^{\circ} - 144^{\circ}$ $12x = 216^{\circ}$ $x = 18^{\circ}$ angles are 5x and 7xi.e. $5 \times 18^{\circ}$ and $7 \times 18^{\circ}$ i.e. 90° and 126°

Question 3.

Angles of a quadrilateral are (4x)°, 5(x+2)°, (7x-20)° and 6(x+3)°. Find (i) the value of x. (ii) each angle of the quadrilateral. Solution: Angles of quadrilateral are,

(4x)°, 5(x+2)°, (7x-20)° and 6(x+3)°. 4x+5(x+2)+(7x-20)+6(x+3) = 360° 4x+5x+10+7x-20+6x+18 = 360° 22x+8 = 360° 22x = 360°-8° 22x = 352° x = 16°Hence angles are, $(4x)° = (4\times16)° = 64°$, 5(x+2)° = 5(16+2)° = 90°, $(7x-20)° = (7\times16-20)° = 92°$ 6(x+3)° = 6(16+3) = 114°

Question 4.

Use the information given in the following figure to find : (i) x (ii) $\angle B$ and $\angle C$ D B B C D B $2x+4^{\circ}$ B

Solution: $\therefore \angle A = 90^{\circ} \text{ (Given)}$ $\angle B = (2x+4^{\circ})$ $\angle C = (3x-5^{\circ})$

$$\angle D = (8x - 15^{\circ}) \angle A + \angle B + \angle C + \angle D = 360^{\circ} 90^{\circ} + (2x + 4^{\circ}) + (3x - 5^{\circ}) + (8x - 15^{\circ}) = 360^{\circ} 90^{\circ} + 2x + 4^{\circ} + 3x - 5^{\circ} + 8x - 15^{\circ} = 360^{\circ} \Rightarrow 74^{\circ} + 13x = 360^{\circ} \Rightarrow 13x = 360^{\circ} - 74^{\circ} \Rightarrow 13x = 286^{\circ} \Rightarrow x = 22^{\circ} \because \angle B = 2x + 4 = 2. x 22^{\circ} + 4 - 48^{\circ} \angle C = 3x - 5 = 3 \times 22^{\circ} - 5 = 61^{\circ} Hence (i) 22^{\circ} (ii) \angle B = 48^{\circ}, \angle C = 61^{\circ}$$

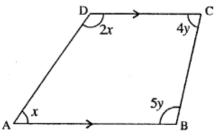
Question 5.

In quadrilateral ABCD, side AB is parallel to side DC. If $\angle A : \angle D = 1 : 2$ and $\angle C : \angle B = 4:5$

(i) Calculate each angle of the quadrilateral.

(ii) Assign a special name to quadrilateral ABCD.

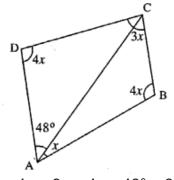
Solution:



Question 6. From the following figure find ; (i) x, (ii) ∠ABC, (iii) ∠ACD.

Solution:

(i) In Quadrilateral ABCD,

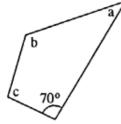


x + 4x + 3x + 4x + 48° = 360° 12x = 360° - 48° 12x = 312 (ii) ∠ABC = 4x 4 x 26 = 104° (iii) ∠ACD = 180°-4x-48° = 180°-4×26°-48° = 180°-104°-48° = 180°-152° = 28°

```
Question 7.
Given : In quadrilateral ABCD ; \angle C = 64^\circ, \angle D = \angle C - 8^\circ ;
\angle A = 5(a+2)^{\circ} and \angle B = 2(2a+7)^{\circ}.
Calculate ∠A.
Solution:
\therefore \angle C = 64^{\circ} (Given)
∴∠D = ∠C- 8°
= 64°- 8°
= 56°
∠A = 5 (a + 2)°
\angle B = 2(2a + 7)^{\circ}
Now \angle A + \angle B + \angle C + \angle D = 360^{\circ}
5(a + 2)^{\circ} + 2(2a + 7)^{\circ} + 64^{\circ} + 56^{\circ} = 360^{\circ}
5a + 10 + 4a + 14^{\circ} + 64^{\circ} + 56^{\circ} = 360^{\circ}
9a + 144° = 360°
9a = 360°-144°
9a = 216°
a = 24°
\therefore \angle A = 5(a + 2)
= 5(24 + 2)
= 130°
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Question 8. In the given figure :

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\angle b = 2a + 15
and \angle c = 3a+5; find the values of b and c.
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Solution:

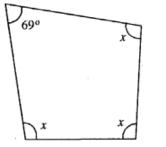
 $\angle b = 2a + 15$ & $\angle c = 3a + 5$::Sum of angles of quadrilateral = 360° $70^{\circ} + a + 2a + 15 + 3a + 5 - 360^{\circ}$ $6a + 90^{\circ} = 360^{\circ}$ $6a = 270^{\circ}$ $a = 45^{\circ}$:: $b = 2a + 15 = 2 \times 45 + 15 = 105^{\circ}$ $c = 3a + 5 = 3 \times 45 + 5 = 140^{\circ}$ 105° and 140°

Question 9.

Three angles of a quadrilateral are equal. If the fourth angle is 69°; find the measure of equal angles.

Solution:

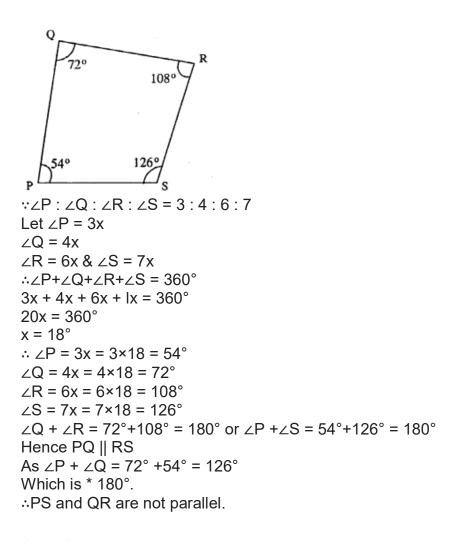
Let each equal angle be $x^{\circ} x + x + x + 69^{\circ} = 360^{\circ}$



3x = 360°-69 3x =291 x = 97° Each equal angle = 97°

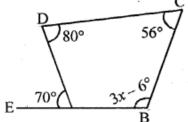
Question 10.

In quadrilateral PQRS, $\angle P : \angle Q : \angle R : \angle S = 3 : 4 : 6 : 7$. Calculate each angle of the quadrilateral and then prove that PQ and SR are parallel to each other. Is PS also parallel to QR ? Solution:



Question 11. Use the information given in the following figure to find the value of x. Solution:

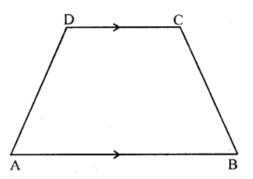
Take A, B, C, D as the vertices of quadrilateral and BA is produced to E (say).



Since $\angle EAD = 70^{\circ}$ $\therefore \angle DAB = 180^{\circ} - 70^{\circ} = 110^{\circ}$ [$\because EAB$ is a straight line and AD stands on it] $\therefore \angle EAD + \angle DAB = 180^{\circ}$ $\therefore 110^{\circ} + 80^{\circ} + 56^{\circ} + 3x = 360^{\circ}$ [\because sum of interior angles of a quadrilateral = 360^{\circ}] $\therefore 3x = 360^{\circ} - 110^{\circ} - 80^{\circ} - 56^{\circ} + 6^{\circ}$ $3x = 360^{\circ} - 240^{\circ} = 120^{\circ}$ $\therefore x = 40^{\circ}$

Question 12.

The following figure shows a quadrilateral in which sides AB and DC are parallel. If $\angle A : \angle D = 4 : 5$, $\angle B = (3x - 15)^\circ$ and $\angle C = (4x + 20)^\circ$, find each angle of the quadrilateral ABCD.



Solution:

Let $\angle A = 4x$ $\angle D = 5x$ Since $\angle A + \angle D = 180^{\circ}$ [: AB || DC] $\therefore 4x + 5x = 180^{\circ}$ $\Rightarrow 9x = 180^{\circ} \Rightarrow x = 20^{\circ}$ $\therefore \angle A = 4$ (20) = 80°, $\angle D = 5$ (20) = 100° Again $\angle B + \angle C = 180^{\circ}$ [: AB || DC] $\therefore 3x - 15^{\circ} + 4x + 20^{\circ} = 180^{\circ}$ $7x = 180^{\circ} - 5^{\circ}$ $\Rightarrow 7x = 175^{\circ} \Rightarrow x = 25^{\circ}$ $\therefore \angle B = 75^{\circ} - 15^{\circ} = 60^{\circ}$ and $\angle C = 4(25) + 20 = 100^{\circ} + 20^{\circ} = 120^{\circ}$

EXERCISE 27 (B)

Question 1. In a trapezium ABCD, side AB is parallel to side DC. If $\angle A = 78^{\circ}$ and $\angle C = 120^{\circ}$, find angles B and D. Solution: \therefore AB || DC and BC is transversal $\therefore \angle B$ and $\angle C$, $\angle A$ and $\angle D$ are Cointerior angles with their sum = 180° i.e. $\angle B + \angle C = 180^{\circ}$ $\Rightarrow \angle B + 120^{\circ} = 180^{\circ}$ $\Rightarrow \angle B = 180^{\circ} - 120^{\circ}$ $\Rightarrow \angle B = 60^{\circ}$ Also $\angle A + \angle D = 180^{\circ}$ $\Rightarrow \angle D = 180^{\circ} - 78^{\circ}$ $\angle D = 102^{\circ}$

Question 2.

In a trapezium ABCD, side AB is parallel to side DC. If $\angle A = x^\circ$ and $\angle D = (3x - 20)^\circ$; find the value of x.

Solution:

 \therefore AB || DC and BC is transversal ∴∠A and ∠B are Co-interior angles with their sum = 180° i.e. ∠A + ∠D = 180°

$$D C
(3x-20)^{\circ}
A
⇒ x^{\circ} + (3x-20)^{\circ} = 180^{\circ}
⇒ x^{\circ} + 3x^{\circ} - 20^{\circ} = 180^{\circ}
⇒ 4x^{\circ} = 180^{\circ} + 20^{\circ}
x^{\circ} = \frac{200}{4} = 50^{\circ}
∴ Value of x = 50^{\circ}$$

Question 3.

The angles A, B, C and D of a trapezium ABCD are in the ratio 3:4:5:6. Le. $\angle A: \angle B: \angle C: \angle D = 3:4:5:6$. Find all the angles of the trapezium. Also, name the two sides of this trapezium which are parallel to each other. Give reason for your answer Solution: As the trapezium ABCD is a quadrilateral, Sum of its interior engles = 260°

 $\therefore \text{ Sum of its interior angles} = 360^{\circ}$ $\Rightarrow \angle A + \angle B + \angle C + \angle D = 360^{\circ}$ $\Rightarrow 3x + 4x + 5x + 6x = 360^{\circ}$ $\Rightarrow 18x = 360^{\circ}$ $\Rightarrow x = \frac{360^{\circ}}{18} = 20^{\circ}$ $\therefore \angle A = 3x = 3 \times 20^{\circ} = 60^{\circ}$ and $\angle B = 4x = 4 \times 20^{\circ} = 80^{\circ}$ and $\angle C = 5x = 5 \times 20^{\circ} = 100^{\circ}$ and $\angle D = 6x = 6 \times 20^{\circ} = 120^{\circ}$ AB is parallel to DC. $\therefore \angle A + \angle D = 180^{\circ},$

 $\angle A$ and $\angle D$ are co-interior angles whose sum = 180°

Question 4.

In an isosceles trapezium one pair of opposite sides are to each Other and the other pair of opposite sides are to each other. Solution:

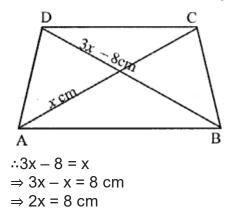
In an isosceles trapezium one pair of opposite sides are **parallel** to each other and the other pair of opposite sides are **equal** to each other.

Question 5.

Two diagonals of an isosceles trapezium are x cm and (3x - 8) cm. Find the value of x.

Solution:

: The diagonals of an isosceles trapezium are of equal length



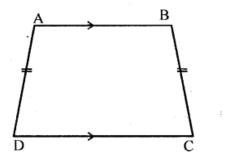
 \Rightarrow x = 4 cm \therefore The value of x is 4 cm

Question 6.

Angle A of an isosceles trapezium is 115°; find the angles B, C and D. Solution:

Since, the base angles of an isosceles trapezium are equal,

$$\therefore \ \angle A = \angle B = 115^{\circ}$$



Also, $\angle A$ and $\angle D$ are co-interior angles and their sum = 180°

- $\therefore \ \angle A + \angle D = 180^{\circ}$
- \Rightarrow 115° + $\angle D$ = 180°

$$\Rightarrow \angle D = 180^\circ - 115^\circ$$

$$\Rightarrow \angle D = 650^{\circ}$$

Also, $\angle D = \angle C = 65^{\circ}$

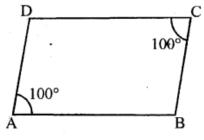
$$\therefore \angle B = 115^{\circ}, \angle C = 65^{\circ} \text{ and } \angle D = 65^{\circ}$$

Question 7.

Two opposite angles of a parallelogram are 100° each. Find each of the other two opposite angles.

Solution:

Given : Two opposite angles of a parallelogram are 100° each



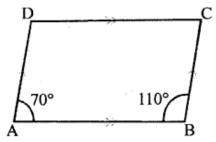
: Adjacent angles of a parallelogram are supplementary, ∴∠A + ∠B = 180° ⇒ $100^{\circ} + \angle B = 180^{\circ}$ ⇒ $\angle B = 180^{\circ} - 100^{\circ}$ ⇒ $\angle B = 80^{\circ}$ Also, opposite angles of a parallelogram are equal $\therefore \angle D = \angle B = 80^{\circ}$ $\therefore \angle B = \angle D = 80^{\circ}$

Question 8.

Two adjacent angles of a parallelogram are 70° and 110° respectively. Find the other two angles of it.

Solution:

Given two adjacent angles of a parallelogram are 70° and 110° respectively.



Since, we know that opposite angles of a parallelogram are equal $\therefore \angle C = \angle A = 70^{\circ}$ and $\angle D = \angle B = 110^{\circ}$

Question 9.

The angles A, B, C and D of a quadrilateral are in the ratio 2:3: 2 : 3. Show this quadrilateral is a parallelogram. Solution:

Given, Angles of a quadrilateral are in the ratio 2:3:2:3

i.e. A : B : C : D are in the ratio 2:3:2:3

To prove - Quadrilateral ABCD is a parallelogram

Prooft - Let us take $\angle A = 2x$, $\angle B = 3x$, $\angle C = 2x$ and $\angle D = 3x$

We know, that the sum of interior angles of a quadrilateral $= 360^{\circ}$

$$\Rightarrow \angle A + \angle B + \angle C + \angle D = 360^{\circ}$$

$$\Rightarrow 2x + 3x + 2x + 3x = 360^{\circ}$$

$$\Rightarrow 10x = 360^{\circ}$$

$$\Rightarrow x = \frac{360^\circ}{10} = 36^\circ$$

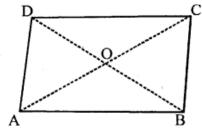
 $\therefore \ \angle A = \angle C = 2x = 2 \times 360^{\circ} = 72^{\circ}$ $\angle B = \angle D = 3x = 3 \times 36^{\circ} = 108^{\circ}$

Now, A quadrilateral ABCD is considered as a parallelogram.

- (i) When opposite angles are equal,
- *i.e.* $\angle A = \angle C = 72^{\circ}$ and $\angle B = \angle D = 108^{\circ}$
- (ii) When adjacent angles are supplementary
 i.e. ∠A + ∠B = 180°
 and ∠C = ∠D = 180°
- \Rightarrow 72° + 108° and 72° + 108° = 180°
- \Rightarrow 180° = 180° and 180° = 180° Since, quadrilateral ABCD fulfils the conditions
- .: Quadrilateral ABCD is a parallelogram.

Question 10.

In a parallelogram ABCD, its diagonals AC and BD intersect each other at point O.



If AC = 12 cm and BD = 9 cm; find; lengths of OA and OD. Solution:

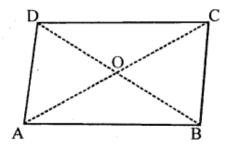
 \therefore When diagonal AC and BD intersect each other at point O,

then
$$OA = OC = \frac{1}{2} AC$$

and $OB = OD = \frac{1}{2} BD$
 $\therefore OA = \frac{1}{2} \times AC = \frac{1}{2} \times 12 = 6 \text{ cm}$
and $OB = \frac{1}{2} \times BD = \frac{1}{2} \times 9 = 4.5 \text{ cm}$

Question 11.

In parallelogram ABCD, its diagonals intersect at point O. If OA = 6 cm and OB = 7.5 cm, find the length of AC and BD.



Solution:

••• When diagonal AC and BD intersect each other at point O,

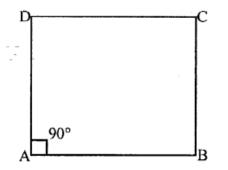
then
$$OA = OC = \frac{1}{2} AC$$

and $OB = OD = \frac{1}{2} BD$
 $\therefore OA = \frac{1}{2} \times AC \implies AC = 2 \times OA$
 $\Rightarrow AC = 2 \times 6 \text{ cm} = 12 \text{ cm},$
and $OB = \frac{1}{2} \times BD \implies BD = 2 \times OB$
 $\Rightarrow BD = 2 \times 7.5 \text{ cm} \implies BD = 15 \text{ cm}$

Question 12.

In parallelogram ABCD, ∠A = 90°
(i) What is the measure of angle B.
(ii) Write the special name of the parallelogram.
Solution:

In parallelogram ABCD, ∠A = 90°



- (i) : In a parallelogram, adjacent angles are supplementary
- $\therefore \ \angle A + \angle B = 180^{\circ}$

$$\Rightarrow 90^{\circ} + \angle B = 180^{\circ}$$

$$\Rightarrow \angle B = 180^{\circ} - 90^{\circ}$$

$$\Rightarrow \angle B = 90^{\circ}$$

(ii) The name of the given parallelogram is a rectangle.

Question 13.

One diagonal of a rectangle is 18 cm. What is the length of its other diagonal? Solution:

 \therefore In a rectangle, diagonals are equal ⇒ AC = BD Given, one diagonal of a rectangle = 18cm \therefore Other diagonal of a rectangle will be = 18cm i.e. AC = BD = 18cm.

Question 14.

Each angle of a quadrilateral is x + 5°. Find: (i) the value of x (ii) each angle of the quadrilateral. Give the special name of the quadrilateral taken.

Solution:

(i) We have,

$$\angle A + \angle B + \angle C + \angle D = 360^{\circ}$$

∵ We know that the sum of interior angles of a quadrilateral is 360°

$$\therefore \ \angle A + \angle B + \angle C + \angle D = 360^{\circ}$$

$$\Rightarrow x + 5^{\circ} + x + 5^{\circ} + x + 5^{\circ} + x + 5^{\circ}$$

$$= 360^{\circ}$$

$$\Rightarrow 4x + 20^{\circ} = 360^{\circ}$$

$$\Rightarrow 4x = 360^{\circ} - 20^{\circ}$$

$$\Rightarrow x = \frac{340^{\circ}}{4} = 85^{\circ}$$
(ii) Each angle of the quadrilateral
ABCD = x + 5^{\circ}
$$= 85^{\circ} + 5^{\circ}$$

$$= 90^{\circ}$$

The name of the given quadrilateral is a rectangle.

Question 15.

If three angles of a quadrilateral are 90° each, show that the given quadrilateral is a rectangle.

Solution:

The given quadrilateral ABCD will be a rectangle, if its each angle is 90° Since, the sum of interior angles of a quadrilateral is 360°.

 $\therefore \angle A + \angle B + \angle C + \angle D = 360^{\circ}$ $\Rightarrow 90^{\circ} + 90^{\circ} + 90^{\circ} + \angle D = 360^{\circ}$ $\Rightarrow 270^{\circ} + \angle D = 360^{\circ}$ $\Rightarrow \angle D = 360^{\circ} - 270^{\circ}$ $\Rightarrow \angle D = 90^{\circ}$

Since, each angle of the quadrilateral is 90°.

∴The given quadrilateral is a rectangle.

Question 16.

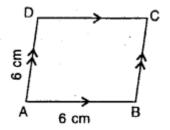
The diagnols of a rhombus are 6 .cm and 8 cm. State the angle at which these diagnols intersect.

Solution:

The diagnols of a Rhombus always intersect at 90°.

Question 17.

Write, giving reason, the name of the figure drawn alongside. Under what condition will this figure be a square.



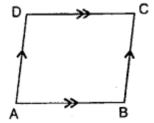
Solution:

Since, all the sides of the given figure are equal. i.e. AB = BC = CD = DA = 6 cm ∴ The given figure is a rhombus.

This figure shall be considered as a square, if any angle is 90°.

Question 18.

Write two conditions that will make the adjoining figure a square.



Solution:

The conditions that will make the ad-joining figure a square are :

(i) All the sides must be equal.

(ii) Any angle is 90°.