

Operation on sets Venn Diagrams

EXERCISE - 6.1

1. $A = \{0, 1, 2, 3, 4, 5, 6, 7, 8\}$ $B = \{3, 5, 7, 9, 11\}$, $C = \{0, 5, 10, 20\}$

i) $A \cup B = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 11\}$

ii) $A \cup C = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 10, 20\}$

iii) $B \cup C = \{0, 3, 5, 7, 9, 10, 11, 20\}$

iv) $A \cap B = \{3, 5, 7\}$

v) $A \cap C = \{0, 5\}$

vi) $B \cap C = \{5\}$

As $B \cup C$ has 8 elements, $n(B \cup C) = 8$

As $A \cap B$ has 3 elements, $n(A \cap B) = 3$

As $A \cap C$ has 2 elements, $n(A \cap C) = 2$

As $B \cap C$ has 1 element, $n(B \cap C) = 1$

2.

i) $A = \{0, 1, 4, 7\}$ and $\xi = \{x \mid x \in \mathbb{N}, x \leq 10\}$

Given $\xi = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

Complement of $A = A' = \{2, 3, 5, 6, 8, 9, 10\}$

ii) $A = \{\text{Consonants}\}$ and $\xi = \{\text{alphabets of English}\}$

Complement of $A = A' = \{\text{vowels}\}$

$= \{a, e, i, o, u\}$

iii) $A = \{\text{boys in class VIII of all schools in Bengaluru}\}$ and
 $\xi = \{\text{Students in class VIII of all schools in Bengaluru}\}$

Complement of $A = A' = \{ \text{girls in Class VIII of all schools in Bengaluru} \}$

iv. $A = \{ \text{letters of KALKA} \}$ and $\xi = \{ \text{letters of KOLKATA} \}$

Complement of $A = A' = \{ O, T \}$

v. $A = \{ \text{odd natural numbers} \}$ and $\xi = \{ \text{Whole numbers} \}$

Complement of $A = A' = \{ 0, 2, 4, 6, 8, 10, 12, \dots \}$

3. $A = \{ x : x \in \mathbb{N} \text{ and } 3 < x < 7 \}$ and $B = \{ x : x \in \mathbb{W} \text{ and } x \leq 4 \}$

$A = \{ 4, 5, 6 \}$ and $B = \{ 0, 1, 2, 3, 4 \}$

i) $A \cup B = \{ 0, 1, 2, 3, 4, 5, 6 \}$

ii) $A \cap B = \{ 4 \}$

iii) $A - B = \{ 5, 6 \}$

iv) $B - A = \{ 0, 1, 2, 3 \}$

4. $P = \{ 0, 1, 2, 3, 4, 5 \}$ $Q = \{ 4, 5, 6, 7, 8 \}$.

i) $P \cup Q = \{ 0, 1, 2, 3, 4, 5, 6, 7, 8 \}$

ii) $P \cap Q = \{ 4, 5 \}$

iii) $P - Q = \{ 0, 1, 2, 3 \}$

iv) $Q - P = \{ 6, 7, 8 \}$

Yes, $P \cup Q$ is a proper superset of $P \cap Q$ but Vice versa is not possible

Since A contains elements not in B .

5. $A = \{\text{letters of word INTEGRITY}\}$ $B = \{\text{letters of word RECKONING}\}$

$$\text{i) } A \cup B = \{I, N, T, E, G, R, Y, C, K, O\}$$

$$\text{ii) } A \cap B = \{I, N, E, G, R\}$$

$$\text{iii) } A - B = \{T, Y\}$$

$$\text{iv) } B - A = \{C, K, O\}$$

$$\text{a) } n(A) = 7 \quad n(B) = 8 \quad n(A \cap B) = 5 \quad n(A \cup B) = 10$$

$$n(A - B) = 2 \quad n(B - A) = 3$$

$$n(A) + n(B) - n(A \cap B) = 7 + 8 - 5 = 10 = n(A \cup B)$$

$$\text{b) } n(A \cup B) - n(B) = 10 - 8 = 2 = n(A - B)$$

$$n(A) - n(A \cap B) = 7 - 5 = 2 = n(A - B)$$

$$\text{c) } n(A \cup B) - n(A) = 10 - 7 = 3 = n(B - A)$$

$$n(B) - n(A \cap B) = 8 - 5 = 3 = n(B - A)$$

$$\text{d) } n(A - B) + n(B - A) + n(A \cap B) = 2 + 3 + 5 = 10 = n(A \cup B)$$

6. $\Sigma = \{10, 11, 12, 13, 14, \dots, 40\}$

$$A = \{5, 10, 15, 20, 25, 30, 35, 40\}$$

$$B = \{6, 12, 18, 24, 30, 36\}$$

$$\text{i) } A \cup B = \{5, 6, 10, 12, 15, 18, 20, 24, 25, 30, 36, 40\}$$

$$A \cap B = \{30\}$$

$$\text{ii) } n(A) = 8, n(B) = 6, n(A \cap B) = 1 \quad n(A \cup B) = 13$$

$$n(A) + n(B) - n(A \cap B) = 8 + 6 - 1 = 13 = n(A \cup B)$$

7

$$\text{i) } A' = \{5, 9\}$$

$$\text{ii) } B' = \{1, 2, 3, 5, 7, 9\}$$

$$\text{iii) } A \cup B = \{1, 2, 3, 4, 6, 7, 8\}$$

$$\text{iv) } A \cap B = \{4, 6, 8\}$$

$$\text{v) } A - B = A \cap B' = \{1, 2, 3, 6, 7, 9\}$$

$$\text{vi) } B - A = B \cap A' = \{\}$$

$$\text{vii) } (A \cap B)' = \{1, 2, 3, 5, 7, 9\}$$

$$\text{viii) } A' \cup B' = \{1, 2, 3, 5, 7, 9\}$$

$$\text{a) } (A \cap B)' = A' \cup B' = \{1, 2, 3, 5, 7, 9\} \quad \text{verified}$$

$$\text{b) } n(A) = 7 \quad n(A') = 2 \quad n(\Sigma) = 9$$

$$n(A) + n(A') = 7 + 2 = 9 = n(\Sigma) \quad \text{verified}$$

$$\text{c) } n(A \cap B) + n((A \cap B)')$$

$$n(A \cap B) = 3 ; n((A \cap B)') = 6$$

$$6 + 3 = 9 = n(\Sigma) \quad \text{verified}$$

$$\text{d) } n(A - B) = 4 \quad n(B - A) = 0 \quad n(A \cap B) = 3$$

$$n(A - B) + n(B - A) + n(A \cap B) = 4 + 0 + 3 = 7 = n(A \cup B)$$

$$8. \Sigma = \{x : x \in \mathbb{N}, x \leq 10\}, A = \{x : x \geq 5\} \quad B = \{x : 3 \leq x < 8\}$$

$$\Sigma = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\} \quad A = \{5, 6, 7, 8, 9, 10\}$$

$$B = \{3, 4, 5, 6, 7\}$$

$$\text{i) } A \cup B = \{3, 4, 5, 6, 7, 8, 9, 10\} \quad A' = \{0, 1, 2, 3, 4\}$$

$$(A \cup B)' = \{0, 1, 2\} \quad B' = \{0, 1, 2, 8, 9, 10\}$$

$$A' \cap B' = \{0, 1, 2\}$$

$$\text{Therefore } (A \cup B)' = A' \cap B' = \{0, 1, 2\}$$

$$\text{ii) } A \cap B = \{5, 6, 7\} \Rightarrow (A \cap B)' = \{0, 1, 2, 3, 4, 8, 9, 10\}$$

$$A' \cup B' = \{0, 1, 2, 3, 4, 8, 9, 10\}$$

$$\text{Therefore } (A \cap B)' = A' \cup B'$$

$$\text{iii) } A - B = \{8, 9, 10\} \quad \therefore A - B = A \cap B'$$
$$A \cap B' = \{8, 9, 10\}$$

$$\text{iv) } B - A = \{3, 4\} \quad \therefore B - A = B \cap A'$$
$$B \cap A' = \{3, 4\}$$

$$9. \quad n(A) = 20, \quad n(B) = 16, \quad n(A \cup B) = 30 \quad n(A \cap B) = ?$$

$$\text{we know } n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

$$30 = 20 + 16 - n(A \cap B)$$

$$n(A \cap B) = 26 - 30 = 6$$

$$\boxed{n(A \cap B) = 6}$$

$$10. \quad n(\xi) = 20 \quad n(A') = 7 \quad n(A) = ?$$

$$\text{we know } n(A) + n(A') = n(\xi)$$

$$n(A) = 20 - 7 = 13$$

$$\boxed{n(A) = 13}$$

$$11. \quad n(\xi) = 40 \quad n(A) = 20 \quad n(B') = 16 \quad n(A \cup B) = 32$$

$$n(B) + n(B') = n(\xi) \Rightarrow n(B) = 40 - 16 = 24$$

$$n(B) = 24$$

$$\eta(A \cup B) = \eta(A) + \eta(B) - \eta(A \cap B)$$

$$32 = 20 + 24 - \eta(A \cap B)$$

$$\eta(A \cap B) = 44 - 32 = 12$$

$$\boxed{\eta(B) = 24; \eta(A \cap B) = 12}$$

$$12. \quad \eta(\Sigma) = 32, \quad \eta(A) = 20, \quad \eta(B) = 16, \quad \eta((A \cup B)') = 4$$

$$\text{i)} \quad \eta(A \cup B) = \eta(\Sigma) - \eta((A \cup B)')$$
$$= 32 - 4 = 28$$

$$\boxed{\eta(A \cup B) = 28}$$

$$\text{ii)} \quad \eta(A \cap B) = \eta(A) + \eta(B) - \eta(A \cup B)$$
$$= 20 + 16 - 28$$
$$= 36 - 28 = 8$$

$$\boxed{\eta(A \cap B) = 8}$$

$$\text{iii)} \quad \eta(A - B) = \eta(A) - \eta(A \cap B)$$
$$= 20 - 8 = 12$$

$$\boxed{\eta(A - B) = 12}$$

$$13. \quad \eta(\Sigma) = 40; \quad \eta(A) = 15, \quad \eta(B) = 12 \quad \eta((A \cap B)') = 32$$

$$\text{i)} \quad \eta(A) = \eta(\Sigma) - \eta(A') = 40 - 15 = 25$$

$$\text{ii)} \quad \eta(B') = \eta(\Sigma) - \eta(B) = 40 - 12 = 28$$

$$\text{iii)} \quad \eta(A \cap B) = \eta(A) + \eta(B) - \eta(A \cup B) = 25 + 12$$

$$\eta(A \cap B) = \eta(\Sigma) - \eta((A \cap B)') = 40 - 32 = 8$$

$$\text{iv)} \quad \eta(A \cup B) = \eta(A) + \eta(B) - \eta(A \cap B) = 25 + 12 - 8 = 29$$

$$\text{v)} \quad \eta(A - B) = \eta(A) - \eta(A \cap B) = 25 - 8 = 17$$

$$\text{vi)} \quad \eta(B - A) = \eta(B) - \eta(A \cap B) = 12 - 8 = 4$$

$$14. \quad n(A-B) = 12, \quad n(B-A) = 16, \quad n(A \cap B) = 5$$

$$\text{i)} \quad n(A) \quad \text{ii)} \quad n(B) \quad \text{iii)} \quad n(A \cup B)$$

$$\text{i)} \quad n(A-B) = n(A) - n(A \cap B)$$

$$n(A) = 12 + 5 = 17$$

$$\text{ii)} \quad n(B-A) = n(B) - n(A \cap B)$$

$$n(B) = 16 + 5 = 21$$

$$\text{iii)} \quad n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

$$= 17 + 21 - 5 = 38 - 5 = 33$$

$$n(A \cup B) = 33.$$

EXERCISE : 6.2

1. from venn diagram, we find that

i) $A = \{0, 5, 7, 8, 9, 11\}$

ii) $B = \{2, 5, 6, 8\}$

iii) $\Sigma = \{0, 1, 2, 4, 5, 6, 7, 8, 9, 11, 12\}$

iv) $A' = \{1, 2, 4, 12\}$

v) $B' = \{0, 1, 4, 7, 9, 11, 12\}$

vi) $A \cup B = \{0, 2, 5, 6, 7, 8, 9, 11\}$

vii) $A \cap B = \{5, 8\}$

viii) $(A \cup B)' = \{1, 4, 12\}$

ix) $(A \cap B)' = \{0, 1, 2, 4, 6, 7, 9, 11, 12\}$

2.

i) $P = \{a, b, d, e, f, g, h, i\}$

ii) $Q = \{b, d, e\}$

iii) $\Sigma = \{a, b, c, d, e, f, g, h, i\}$

iv) $P' = \{c, j\}$

v) $Q' = \{a, c, f, g, h, i, j\}$

vi) $P \cup Q = \{a, b, d, e, f, g, h, i\}$

vii) $P \cap Q = \{b, d, e\}$

viii) $(P \cup Q)' = \{c, j\}$

ix) $(P \cap Q)' = \{a, c, f, g, h, i, j\}$

3.

$$\text{i)} \Sigma = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$$

$$\text{ii)} A \cap B = \{0, 5, 8\}$$

$$\text{iii)} A \cap B \cap C = \{0, 5\}$$

$$\text{iv)} C' = \{2, 7, 8, 9, 10, 11, 12\}$$

$$\text{v)} A - C = A \cap C' = \{8, 10\}$$

$$\text{vi)} B - C = B \cap C' = \{7, 8, 11\}$$

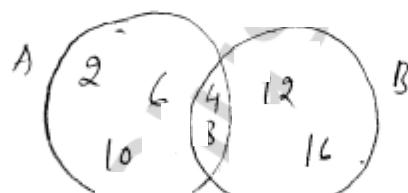
$$\text{vii)} C - B = C \cap B' = \{3, 4, 6\}$$

$$\text{viii)} (A \cup B)' = \{2, 4, 6, 9, 12\}$$

$$\text{ix)} (A \cup B \cup C)' = \{2, 9, 12\}$$

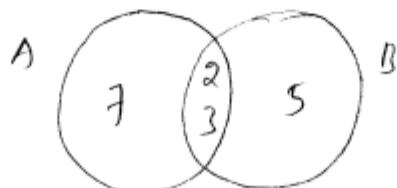
4. i) $A = \{x | x \in \mathbb{N}, x = 2n, n \leq 5\} ; B = \{x | x \in \mathbb{N}, x = 4n, n < 5\}$

$$A = \{2, 4, 6, 8, 10\} \quad B = \{4, 8, 12, 16\}$$



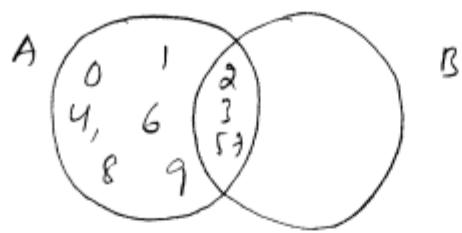
ii) $A = \{\text{prime factors of } 42\} \quad B = \{\text{prime factors of } 60\}$

$$A = \{2, 3, 7\} \quad B = \{2, 3, 5\}$$

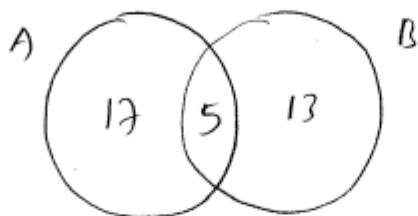


iii) $P = \{x | x \in \mathbb{N}, x < 10\} \quad Q = \{\text{prime factors of } 210\}$

$$P = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\} \quad Q = \{2, 3, 5, 7\}$$



5. $n(A) = 22$ $n(B) = 18$ $n(A \cap B) = 5$

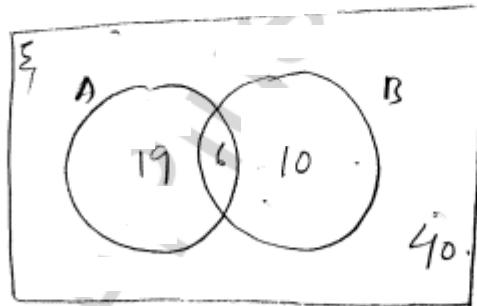


i) $n(A \cup B) = 17 + 5 + 13 = 35$

ii) $n(A - B) = n(A) - n(A \cap B) = 17 - 5 = 12$

iii) $n(B - A) = n(B) - n(A \cap B) = 13 - 5 = 8$

6. $n(A) = 25$ $n(B) = 16$, $n(A \cap B) = 6$, $n((A \cup B)') = 5$



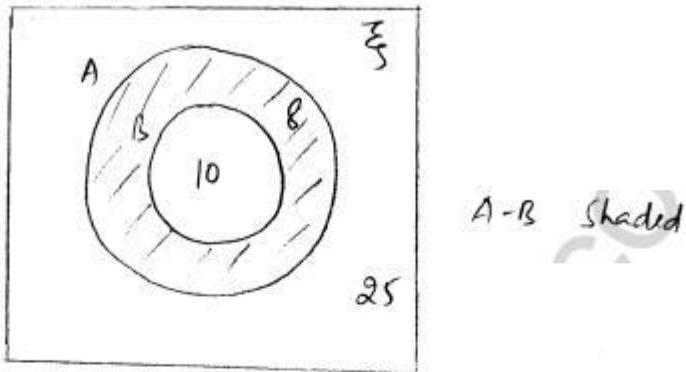
i) $n(A \cup B) = 19 + 6 + 10 = 35$

ii) $n(\Sigma) = n(A \cup B) + n((A \cup B)') = 35 + 5 = 40$

iii) $n(A - B) = n(A) - n(A \cap B) = 25 - 6 = 19$

iv) $n(B - A) = n(B) - n(A \cap B) = 16 - 6 = 10$

$$7. \quad n(\xi) = 25 \quad n(A') = 7 \quad n(B) = 10 \quad B \subset A$$

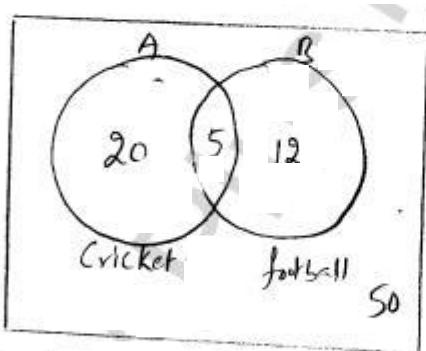


$$n(A) = n(\xi) - n(A') = 25 - 7 = 18$$

$$n(A-B) = n(A) - n(A \cap B) = 18 - 10 = 8$$

\therefore Cardinal number of set $A-B$ is 8.

8.



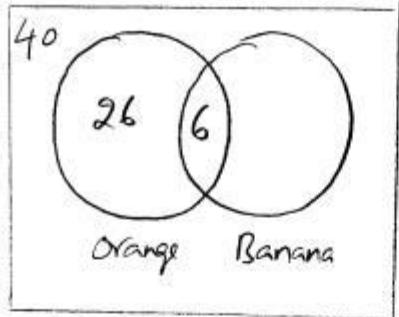
i) No. of boys who play atleast one of the two games
 $= n(\text{Only cricket}) + n(\text{only football}) + n(\text{both cricket \& football})$
 $= 20 + 12 + 5$
 $= 37$

ii) Neither cricket nor football

$$n((A \cup B)') = \text{Total student} - n(A \cup B)$$

$$\Rightarrow 50 - 37 = 13$$

9.



from Venna Diagram

i) Both orange and Banana.
A B

$$\begin{aligned}
 n(A \cap B) &= \text{no. of students who like both orange and Banana} \\
 &= \text{no. of student who like orange} - \text{no. of student} \\
 &\quad \text{who like orange but} \\
 &= 32 - 26 \\
 &= 6
 \end{aligned}$$

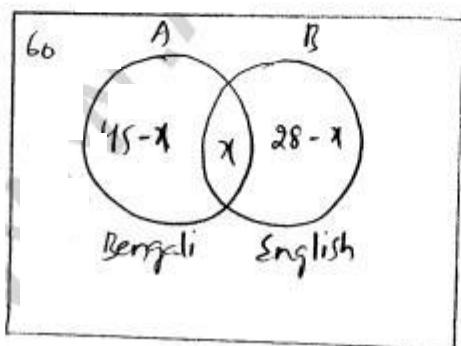
ii) $n(B) = ?$

$$n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

$$\begin{aligned}
 n(B) &= 40 - 32 + 6 = 46 - 32 \\
 &= 14
 \end{aligned}$$

$$\begin{aligned}
 \text{number of student who like only banana} &= 14 - 6 \\
 &= 8
 \end{aligned}$$

10.



$$n(A \cap B) = x$$

$$n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

$$60 = 45 + 28 - x$$

$$x = 73 - 60$$

$$\boxed{x = 13}$$

∴ No of people who speak both Bengali and English are
13