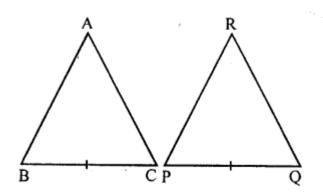
Triangles

Question 1.

It is given that $\triangle ABC \cong \triangle RPQ$. Is it true to say that BC = QR ? Why? Solution:

 $\triangle ABC \cong \triangle RPQ$

.. Their corresponding sides and angles are equal



- ∴ BC = PQ
- :. It is not true to say that BC = QR

Question 2.

"If two sides and an angle of one triangle are equal to two sides and an angle of another triangle, then the two triangles must be congruent." Is the statement true? Why?

Solution:

No, it is not true statement as the angles should be included angle of there two given sides.

Question 3.

In the given figure, AB=AC and AP=AQ. Prove that

- (i) $\triangle APC \cong \triangle AQB$
- (ii) CP = BQ
- (iii) ∠APC = ∠AQB.

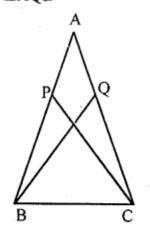
Solution:

Given: In the figure, AB = AC, AP = AO

To prove:

(i)
$$\triangle APC \cong \triangle AQB$$
 (ii) $CP = BQ$

(iii) $\angle APC = \angle AQB$



Proof: In ΔAPC and ΔAQB

$$AC = AB$$
 (Given)
 $AP = AQ$ (Given)
 $\angle A = \angle A$ (Common)
(i) $\because \triangle APC \cong \triangle AQB$ (SAS axiom)
(ii) $BQ = CP$ (c.p.c.t.)
(iii) $\angle APC = \angle AQB$ (c.p.c.t.)

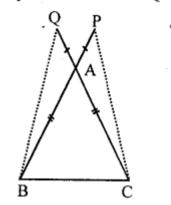
Question 4.

In the given figure, AB = AC, P and Q are points on BA and CA respectively such that AP = AQ. Prove that

- (i) $\triangle APC \cong \triangle AQB$
- (ii) CP = BQ
- (iii) ∠ACP = ∠ABQ.

Solution:

Given: In the given figure, AB = AC
P and Q are point on BA and CA produced
respectively such that AP = AQ



To prove : (i) $\triangle APC \cong \triangle AQB$

(ii)
$$CP = BQ$$

(iii)
$$\angle ACP = \angle ABQ$$

Proof: In $\triangle APC$ and $\triangle AQB$

$$AC = AB$$
 (Given)

$$AP = AQ$$
 (Given)

$$\angle PAC = \angle QAB$$
 (Vertically opposite angle)

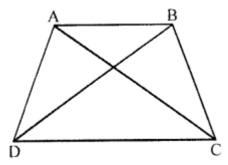
(i)
$$\therefore \Delta APC \cong \Delta BQP$$
 (SAS axiom)

$$\therefore CP = BQ \qquad (c.p.c.t.)$$

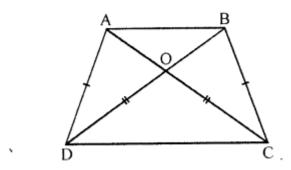
$$\angle ACP = \angle ABQ$$
 (c.p.c.t.)

Question 5.

In the given figure, AD = BC and BD = AC. Prove that : \angle ADB = \angle BCA and \angle DAB = \angle CBA.



Given: In the figure, AD = BC, BD = AC



To prove:

- (i) $\angle ADB = \angle BCA$
- (ii) $\angle DAB = \angle CBA$

Proof: In $\triangle ADB$ and $\triangle ACB$

(commo	AB = AB	
(give	AD = BC	
(give	DB = AC	
(SSS axion	ΔADB ≅ ΔACD	<i>:</i> .
(c.p.c.t	∠ADB=∠BCA	<i>:</i> .
(c.p.c.t	$\angle DAB = \angle CBA$	

Question 6.

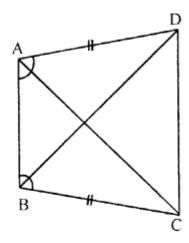
In the given figure, ABCD is a quadrilateral in which AD = BC and \angle DAB = \angle CBA. Prove that

- (i) $\triangle ABD \cong \triangle BAC$
- (ii) BD = AC
- (iii) ∠ABD = ∠BAC.

Given: In the figure ABCD is a quadrilateral

in which AD = BC

 $\angle DAB = \angle CBA$



To prove:

(i)
$$\triangle ABD \cong \triangle BAC$$
 (ii) $BD = AC$

(iii) $\angle ABD = \angle BAC$

Proof: In $\triangle ABD$ and $\triangle ABC$

AB = AB	(Common)
$\angle DAB = \angle CBA$	(Given)
AD = BC	(Given)
(i) $\therefore \triangle ABD \cong \triangle ABC$	(SAS axiom)
(ii) :: BD = AC	(c.p.c.t.)
iii) ∠ABD=∠BAC	(c.p.c.t.)

Question 7.

In the given figure, AB = DC and AB || DC. Prove that AD = BC. Solution:

Given: In the given figure,

AB = DC, $AB \parallel DC$

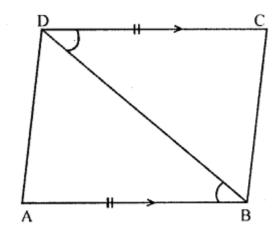
To pove : AD = BC

Proof: :: AB || DC

 $\therefore \angle ABD = \angle CDB$ (Alternate angles)

In ΔABD and ΔCDB

$$AB = DC$$
 (Given)



$$\angle ABD = \angle CDB$$

(Alternate angles)

BD = BD

(Common)

∴ ΔABD≅ΔCDB

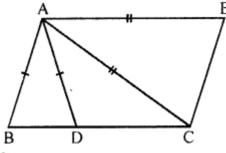
(SAS axiom)

 $\therefore AD = BC$

(c.p.c.t.)

Question 8.

In the given figure. AC = AE, AB = AD and \angle BAD = \angle CAE. Show that BC = DE.



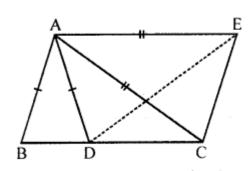
Solution:

Given: In the figure, AC = AE, AB = AD

 $\angle BAD = \angle CAE$

To prove : BC = DE

Construction: Join DE.



Proof: In ΔABC and ΔADE

$$AB = AD$$
 (given)

$$AC = AE$$
 (given)

$$\angle BAD + \angle DAC = \angle DAC + \angle CAE$$

$$\Rightarrow \angle BAC = \angle DAE$$

$$\therefore \triangle ABC \cong \triangle ADE$$
 (SAS axiom)

$$\therefore BC = DE \qquad (c.p.c.t.)$$

Question 9.

In the adjoining figure, AB = CD, CE = BF and \angle ACE = \angle DBF. Prove that

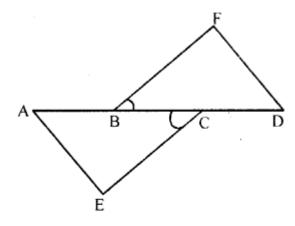
- (i) $\triangle ACE \cong \triangle DBF$
- (ii) AE = DF.

Given: In the given figure,

AB = CD

CE = BF

 $\angle ACE = \angle DBF$



To prove : (i) $\triangle ACE \cong \triangle DBF$

$$(ii)$$
 AE = DF

Proof: : AB = CD

Adding BC to both sides

$$AB + BC = BC + CD$$

$$\Rightarrow$$
 AC = BD

Now in $\triangle ACE$ and $\triangle DBF$

AC = BD (Proved)

CE = BF (Given)

 $\angle ACE = \angle DBF$ (Given)

(i) $\therefore \triangle ACE \cong \triangle DBF$ (SAS axiom)

 $\therefore AE = DE \qquad (c.p.c.t.)$

Question 10.

In the given figure, AB = AC and D is mid-point of BC. Use SSS rule of congruency to show that

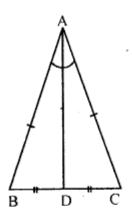
- (i) $\triangle ABD \cong \triangle ACD$
- (ii) AD is bisector of ∠A
- (iii) AD is perpendicular to BC.

Solution:

Given: In the given figure, AB = AC

D is mid point of BC

∴ BD = DC



To prove:

- (i) $\triangle ABD \cong \triangle ACD$
- (ii) AD is bisector of ∠A
- (iii) AD⊥BC

Proof: In $\triangle ABD$ and $\triangle ACD$

AB = AC (Given)

BD = DC (Given)

AD = AD (Common)

- (i) $\therefore \triangle ABD \cong \triangle ACD$
- (ii) $\angle BAD = \angle CAD$ (c.p.c.t.)

∴ AD is the bisector of ∠A

(iii) $\angle ADB = \angle ADC$

But $\angle ADB + \angle ADC = 180^{\circ}$ (Linear pair)

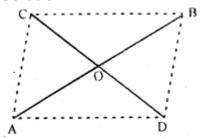
 \therefore $\angle ADB = \angle ADC = 90^{\circ}$

∴ AD ⊥ BC

Question 11.

Two line segments AB and CD bisect each other at O. Prove that :

- (i) AC = BD
- (ii) ∠CAB = ∠ABD
- (iii) AD || CB
- (iv) AD = CB.



In AAOC and AAOC

OC = OD [AB and CD bisect each other]

and AO = OB

Also, $\angle AOC = \angle BOD$ (vertical opposite angles)

 $\therefore \Delta AOC \cong \Delta BOD$

(By S.A.S. axiom of congruency)

(i) Then AC = BD (c.p.c.t.)

(ii) Also $\angle CAO = \angle DBO$ (c.p.c.t.)

i.e. $\angle CAB = \angle ABD$

[\because \angle CAO = \angle CAB and \angle DBO = \angle ABD]

(iii) We have in (ii) part

 $\angle CAB = \angle ABD$

But these are Alternate angles

Hence, AD || CD

(iv) In \triangle AOD and \triangle BOC

OC = OD and BO = AO

(AB and CD bisect each other)

and $\angle BOC = \angle AOD$

(vertical opposite angles)

 $\therefore \triangle AOD \cong \triangle BOC$

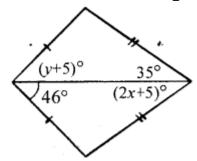
[By S.A.S. axiom of congruency]

Then, AD = BC (c.p.c.t.)

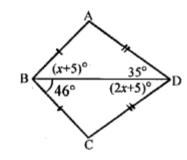
or AD = CB (Q.E.D.)

Question 12.

In each of the following diagrams, find the values of x and y.



Solution:



In $\triangle ABD$ and $\triangle BCD$,

$$AB = BC$$
 (given)

$$AD = CD$$
 (given)

$$BD = BD$$
 (common)

$$\therefore \Delta ABD \cong \Delta BCD$$

(By S.S.S axiom of

$$\therefore \angle ABD = \angle CBD \quad (c.p.c.t.)$$

$$\Rightarrow y+5=46 \Rightarrow y=46-5 \Rightarrow y=41$$

Also
$$\angle ADB = \angle BDC$$
 (c.p.c.t.)

$$\Rightarrow$$
 35° = $(2x + 5)$ ° \Rightarrow 35 = $2x + 5$

$$\Rightarrow 2x + 5 = 35 \Rightarrow 2x = 35 - 5 \Rightarrow 2x = 30$$

$$\Rightarrow \quad x = \frac{30}{2} \quad \Rightarrow \quad x = 15$$

Exercise 10.2

Question 1.

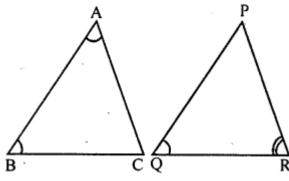
In triangles ABC and PQR, \angle A= \angle Q and \angle B = \angle R. Which side of APQR should be equal to side AB of AABC so that the two triangles are congruent? Give reason for your answer.

Solution:

In ΔABC and ΔPQR

$$\angle A = \angle Q$$

$$\angle B = \angle R$$



$$AB = QP$$

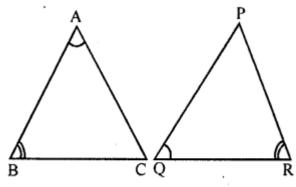
: Two Δs are congruent of their corresponding two angles and included sides are equal

Question 2.

In triangles ABC and PQR, $\angle A = \angle Q$ and $\angle B = \angle R$. Which side of APQR should be equal to side BC of AABC so that the two triangles are congruent? Give reason for your answer.

Solution:

In $\triangle ABC$ and $\triangle PQR$



$$\angle A = \angle Q$$

$$\angle B = \angle R$$

and their included sides AB and QR will be equal for their congruency

$$\therefore$$
 BC = PR

(c.p.c.t.)

Question 3.

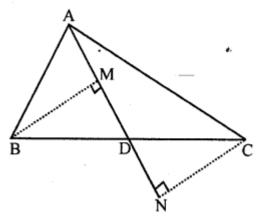
"If two angles and a side of one triangle are equal to two angles and a side of another triangle, then the two triangles must be congruent". Is the statement true? Why?

Solution:

The given statement can be true only if the corresponding (included) sides are equal otherwise not.

Question 4.

In the given figure, AD is median of \triangle ABC, BM and CN are perpendiculars drawn from B and C respectively on AD and AD produced. Prove that BM = CN. Solution:



Given: In $\triangle ABC$, AD is median BM and CN are perpendicular to AD form B and C respectively

To prove : BM = CN

Proof: In ΔBMD and ΔCND

BD = CD (AD is median)

 $\angle M = \angle N$ (each 90°)

∠BDM = ∠CDN

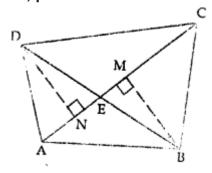
(Vertically opposite angles)

 $\therefore \Delta BMD \cong \Delta CND$ (AAS axiom)

 $\therefore BM = CN \qquad (c.p.c.t.)$

Question 5.

In the given figure, BM and DN are perpendiculars to the line segment AC. If BM = DN, prove that AC bisects BD.



Given: In the figure, BM and DN are

perpendicular to AC

BM = DN

To prove: AC bisects BD i.e., BE = ED

Construction: Join BD which intersects AC

at E

Proof: In \triangle BEM and \triangle DEN

BM = DN

(Given)

 $\angle M = \angle N$

(each 90°)

 $\angle DEN = \angle BEM$

(Vertically opposite angles)

∴ ΔBEM ≅ ΔDEN

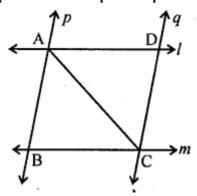
(AAS axiom)

 \therefore BE = ED

⇒ AC bisects BD

Question 6.

In the given figure, I and m are two parallel lines intersected by another pair of parallel lines p and q. Show that $\triangle ABC \cong \triangle CDA$.



In the given figure, two lines l and m are parallel to each other and lines p and q are also a pair of parallel lines intersecting each othat at A, B, C and D. AC is joined.

To prove : $\triangle ABC \cong \triangle CDA$ Proof : In $\triangle ABC$ and $\triangle CDA$

AC = AC (Common)

 $\angle ACB = \angle CAD$ (Alternate angles)

 $\angle BAC = \angle ACD$ (Alternate angles)

 $\therefore \Delta ABC \cong \Delta DCA$ (ASA axiom)

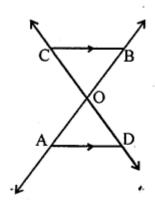
Question 7.

In the given figure, two lines AB and CD intersect each other at the point O such that BC \parallel DA and BC = DA. Show that O is the mid-point of both the line segments AB and CD.

Solution:

Given: In the given figure, lines AB and CD intersect each other at O such that BC \parallel AD

and BC = DA



To prove: O is the mid point of AB and CD

Proof: $\triangle AOD$ and $\triangle BOC$

AD = BC (Given)

 $\angle OAD = \angle OBC$ (Alternate angles)

 $\angle ODA = \angle OCB$ (Alternate angles)

∴ $\triangle AOD \cong \triangle BOC$ (SAS axiom)

∴ OA = OB and OD = OC

.. O is the mid-point of AB and CD

Question 8.

In the given figure, $\angle BCD = \angle ADC$ and $\angle BCA = \angle ADB$. Show that

(i) $\triangle ACD \cong \triangle BDC$

(ii) BC = AD

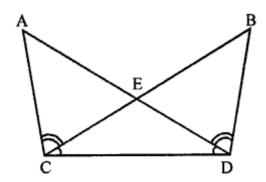
(iii) $\angle A = \angle B$.

Solution:

Given: In the given figure,

 $\angle BCD = \angle ADC$

 $\angle BCA = \angle ADB$



To prove:

(i)
$$\triangle ACD \cong \triangle BDC$$
 (ii) $BC = AD$

(iii)
$$\angle A = \angle B$$

Proof:
$$\because \angle BCA = \angle ADB$$

and
$$\angle BCD = \angle ADC$$

Adding we get,

$$\angle BCA + \angle BCD = \angle ADB + \angle ADC$$

$$\Rightarrow \angle ACD = \angle BDC$$

Now in AACD and ABDC

$$CD = CD$$
 (Common)

$$\angle ACD = \angle BDC$$
 (Proved)

$$\angle ADC = \angle BCD$$
 (Given)

(i)
$$\therefore \triangle ACD \cong \triangle BDC$$
 (ASA axiom)

$$\therefore AD = BC \qquad (c.p.c.t.)$$

$$\angle A = \angle B$$
 (c.p.c.t.)

Question 9.

In the given figure, $\angle ABC = \angle ACB$, D and E are points on the sides AC and AB respectively such that BE = CD. Prove that

- (i) $\triangle EBC \cong \triangle DCB$
- (ii) $\triangle OEB \cong \triangle ODC$

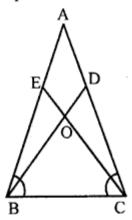
(iii) OB = OC.

Solution:

Given: In the given figure,

 $\angle ABC = \angle ACB$

D and E are the points on AC and AB such



To prove : (i) $\triangle EBC \cong \triangle DCB$

(ii) $\triangle OEB \cong \triangle ODC$

(iii) OB = OC

Proof: In AABC,

∴ ∠ABC = ∠ACB

 \therefore AC = AB (Sides opposite to equal angles)

In \triangle EBC and \triangle DCB,

EB = DC (Given)

BC = BC (Common)

 $\angle CBD = \angle DCB$ (:: $\angle ABC =$

∠ACB)

(i) $:: \Delta EBC \cong \Delta DCB$ (SAS axiom)

 $\angle ECB = \angle DBC$ (c.p.c.t.)

Now in ΔOEB and ΔODC

BE = CD (Given)

 \angle EBO = \angle DCO

 ${\because \angle ABC - \angle DBC = \angle ACB - \angle OCB}$

 $\angle EOB = \angle DOC$

(ii) $\therefore \triangle OEB \cong \triangle ODC$ (AAS axiom)

(iii) \therefore OB = OC (c.p.c.t.)

Question 10.

ABC is an isosceles triangle with AB=AC. Draw AP \perp BC to show that \angle B = \angle C. Solution:

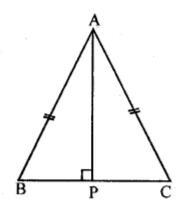
Given: $\triangle ABC$ is an isosceles triangle with

AB = AC $AP \perp BC$

To prove : $\angle B = \angle C$

Proof: In right $\triangle APB$ and $\triangle APC$

Side AP = AP (Common)



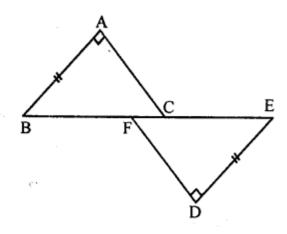
Hyp. AB = AC (Given)
∴ ΔAPB
$$\cong$$
 ΔAPC (RHS axiom)
∴ ∠B = ∠C (c.p.c.t.)

Question 11.

In the given figure, BA \perp AC, DE \perp DF such that BA = DE and BF = EC.

Given: In the given figure,

BA \perp AC, DE \perp DF BA = DE, BF = EC



To prove : $\triangle ABC \cong \triangle DEF$

Proof: : BF = CE

Adding FC both sides

BF + FC = FC + CE

 \Rightarrow BC = EF

Now in right $\triangle ABC$ and $\triangle DEF$

Side AB = DE (Given)

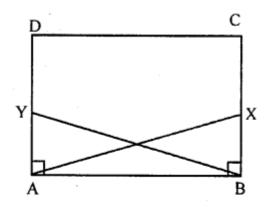
Hyp. BC = EF (Proved)

 $\therefore \Delta \dot{A}BC \cong \Delta DEF$

Question 12.

ABCD is a rectanige. X and Y are points on sides AD and BC respectively such that AY = BX. Prove that BY = AX and \angle BAY = \angle ABX. Solution:

Given: In rectangle ABCD, X and Y are points on the sides AD and BC respectively such that AY = BX



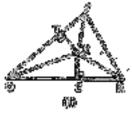
To prove: BY = AX and \angle BAY = \angle ABX

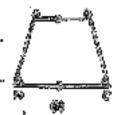
Proof: In $\triangle ABX$ and $\triangle ABY$

AB = AB (Common) $\angle A = \angle B$ (Each 90°) BX = AY (Given) $\therefore \Delta ABX \cong \Delta ABY$ (SAS axiom) AX = BY (c.p.c.t.) or BY AX and $\angle AXB = \angle BYA$ (c.p.c.t.)

Question 13.

- (a) In the figure (1) given below, QX, RX are bisectors of angles PQR and PRQ respectively of A PQR. If $XS\perp QR$ and $XT\perp PQ$, prove that
- (i) $\triangle XTQ \cong \triangle XSQ$
- (ii) PX bisects the angle P.
- (b) In the figure (2) given below, AB || DC and \angle C = \angle D. Prove that
- (i) AD = BC
- (ii) AC = BD.
- (c) In the figure (3) given below, BA || DF and CA II EG and BD = EC . Prove that, .
- (i) BG = DF
- (ii) EG = CF.







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$$\begin{bmatrix} \angle XTP = 90^{\circ} \text{ (given)} \\ \angle XTP = 90^{\circ} \text{ (construction)} \end{bmatrix}$$

(hyp)
$$XP = (hyp) XP$$

(common

XT = XZ

[From (3)

 $\therefore \quad \Delta XTP \cong \Delta XZP$

[By R.H.S. axiom of congruency

 $\therefore \angle XPT = \angle XPZ$

(c.p.c.t.

.. PX bisects the angle P.

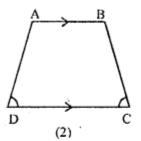
(Q.E.D.

(b) In following figure

Given. AB \parallel DC and \angle C = \angle D

To prove. (i) AD = BC

(ii)AC = BD



Construction. Draw $AE \perp CD$, $BF \perp CD$ an join A to C and B to D.

Proof. (i) In \triangle AED and \triangle BCF

$$\angle AED = \angle BFC$$

(each 90°

[By construction AE \perp CD and BF \perp CD]

$$\angle D = \angle C$$

(given

AE = BF

[Distance between parallel lines are same]

 $\therefore \Delta AED \cong \Delta BCF$

(By A.A.S. axiom of congruency

$$AD = BC$$

.... (1

(ii) In \triangle ACD and \triangle BCD

$$\angle D = \angle C$$

(Given

DC = DC

(Commor

$$AD = BC$$

[From (1)

 $\therefore \Delta ACD \cong \Delta BCD$

(By S.A.Ş. axiom of congruency

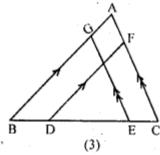
(Q.E.D.

(c) In following figure

Given. BA || DF and CA || EG and BD = EC

To prove. (i) BG = DF

(ii)EG = CF



Proof. (i) In \triangle BEG and \triangle DCF

$$\angle B = \angle D$$

(∵ BA || DF, corresponding angles equal)

 $\angle E = \angle C$

(∵ CA || EG corresponding angles equal)

and BE = BC - EC = BC - BD = DC

i.e. BE = DC

 $\therefore \Delta BEG \cong \Delta DCF$

(By A.S.A. axiom of congruency)

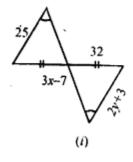
 $\therefore BG = DF \quad (c.p.c.t.)$

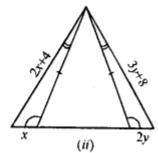
(iii) EG = CF (c.p.c.t.)

(Q.E.D.)

Question 14.

In each of the following diagrams, find the values of x and y.





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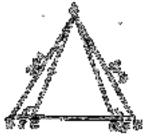
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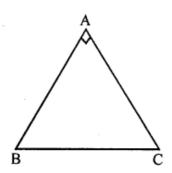
Exercise 10.3

Question 1.

ABC is a right angled triangle in which $\angle A = 90^{\circ}$ and AB = AC. Find $\angle B$ and $\angle C$. In right $\triangle ABC$, $\angle A = 90^{\circ}$

$$\therefore \angle B + \angle C = 180^{\circ} - \angle A$$

= 180° - 90° = 90°



$$:: AB = AC$$

$$\therefore$$
 $\angle C = \angle B$ (Angles opposite to equal sides)

$$\therefore \angle B + \angle B = 90^{\circ} \Rightarrow 2\angle B = 90^{\circ}$$

$$\therefore \angle B = \frac{90^{\circ}}{2} = 45^{\circ}$$

Question 2.

Show that the angles of an equilateral triangle are 60° each. Solution:

ΔABC is an equilateral triangle

$$\therefore$$
 AB = BC = CA

$$\therefore \angle A = \angle B = \angle C$$
 (Opposite to equal sides)

But
$$\angle A + \angle B + \angle C = 180^{\circ}$$

(Sum of angls of a triangle)

$$\therefore \angle A + \angle A + \angle A = 180^{\circ}$$

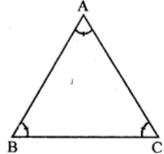
$$\Rightarrow 3\angle A = 180^{\circ} \Rightarrow \angle A = \frac{180^{\circ}}{3} = 60^{\circ}$$

$$\therefore \angle A = \angle B = \angle C = 60^{\circ}$$

Question 3.

Show that every equiangular triangle is equilateral. Solution:

ΔABC is an equaiangular



$$\therefore \angle A = \angle B = \angle C$$

In $\triangle ABC$

$$\therefore \angle B = \angle C$$

...(i)

Similarly, $\angle C = \angle A$

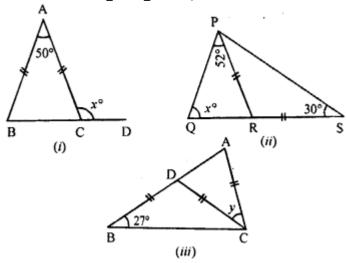
From (i) and (ii)

$$AB = BC = AC$$

∴ ∆ABC is an equilateral triangle

Question 4.

In the following diagrams, find the value of x:



Solution:

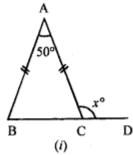
(m)

(1) In following diagram given that AB = AC

i.e. $\angle B = \angle ACB$ (angles opposite to equal sides in a triangles are equal)

Now, $\angle A + \angle B + \angle ACB = 180^{\circ}$

(sum of all angles in a triangle is 180°)



$$\Rightarrow$$
 50° + \angle B + \angle B = 180°

[
$$\therefore \angle A = 50^{\circ} \text{ (given) } \angle B = \angle ACB$$
]

$$\Rightarrow$$
 $50^{\circ} + 2 \angle B = 180^{\circ} \Rightarrow 2 \angle B = 180^{\circ} - 50^{\circ}$

$$\Rightarrow$$
 2 \angle B = 130° \Rightarrow \angle B = $\frac{130}{2}$ = 65°

$$\therefore$$
 \angle ACB = 65°

Also,
$$\angle ACB + x^{\circ} = 180^{\circ}$$
 (Linear pair)

$$65^{\circ} + x^{\circ} = 180^{\circ} \implies x^{\circ} = 180^{\circ} - 65^{\circ}$$

$$\Rightarrow x^{\circ} = 115^{\circ}$$

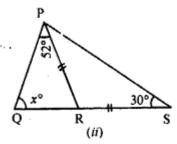
Hence, value of x = 115

(ii) In APRS,

Given that PR = RS

$$\therefore \angle PSR = \angle RPS$$

(angles opposite in a triangle, equal sides are equal)



$$\Rightarrow$$
 30° = \angle RPS \Rightarrow \angle RPS = 30° (1)

$$\angle QPS = \angle QPR + \angle RPS$$

$$\Rightarrow$$
 $\angle QPS = 52^{\circ} + 30^{\circ}$

(Given,
$$\angle$$
 QPR = 52° and from (1), \angle RPS = 30°)

$$\Rightarrow$$
 $\angle QPS = 82^{\circ}$ (2)

Now, in △PQS

$$\angle QPS + \angle QSP + PQS = 180^{\circ}$$

(sum of all angles in a triangles is 180°)

$$\Rightarrow$$
 82° + 30° + x ° = 180°

[From (2) \angle QPS = 82° and \angle QSP = 30° (given)]

$$\Rightarrow$$
 112° + x ° = 180° \Rightarrow x ° = 180° - 112°

Hence, value of x = 68 Ans.

(iii) In the following figure, Given

that,BD=CD=AC and \angle DBC= 27°

Now, in \triangle BCD

BD = CD (given)

 $\angle DBC = \angle BCD \dots (1)$

(In a triangle sides opposite equal angles are equal)

Also,
$$\angle DBC = 27^{\circ}$$

(given) (2)

27°

From (1) and (2), we get

$$\angle BCD = 27^{\circ}$$
 (3)

Now, ext. $\angle CDA = \angle DBC + \angle BCD$

[exterior angle is equal to sum of two interior opposite angles]

$$\Rightarrow$$
 ext. \angle CDA = $27^{\circ} + 27^{\circ}$ [From (2) and (3)]

$$\Rightarrow$$
 $\angle CDA = 54^{\circ}$ (4)

In \triangle ACD,

$$AC = CD$$
 (given)

 $\angle CAD = \angle CDA$ (In a triangle, angles opposite to equal sides are equal)

$$\angle CAD = 54^{\circ}$$
 [From (4)] (5)

Also, in \triangle ACD

$$\angle$$
CAD + \angle CDA + \angle ACD = 180°
(sum of all angles in a triangle is 180°)

$$\Rightarrow$$
 54° + 54° + y = 180° [From (4) and (5)]

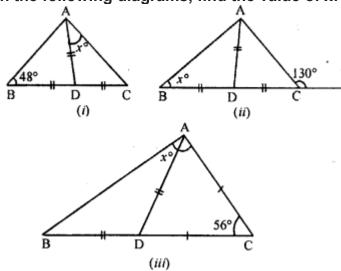
$$\Rightarrow$$
 108° + $y = 180$ ° \Rightarrow $y = 180$ ° - 108°

$$\Rightarrow y = 72^{\circ}$$

Hence, value of $y = 72^{\circ}$

Question 5.

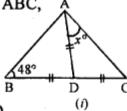
In the following diagrams, find the value of x:



Solution:

(i) In the following figure,

Given. In \triangle ABC,



$$AD = BD = CD$$
.

$$\angle B = 48^{\circ}$$
, $\angle DAC = x^{\circ}$

Now, in △ABD

$$BD = AD$$
 (given)

$$\angle BAD = \angle B$$
 (1)

(angles opposite equal sides in a triangle are

$$\angle B = 48^{\circ}$$
 (2)

Now, in △ABD

From (1) and (2)
$$\angle BAD = 48^{\circ}$$

(3)

Exterior
$$\angle ADC = \angle B + \angle BAD$$

(In a triangle exterior angle is equal to sum of two interior opposite angles)

$$\angle ADC = 48^{\circ} + 48^{\circ} \implies \angle ADC = 96^{\circ} \dots (4)$$

Now, in △ ADC

$$AD = DC$$
 (given)

$$\therefore$$
 $\angle C = \angle DAC$ (5)

(In a triangle, angles opposite equal sides are equal)

$$\angle DAC = x^{\circ}$$
 (given).... (6)

From (5) and (6)

$$\angle C = x^{\circ}$$
 (7)

Now, in △ADC

$$\angle C + \angle ADC + \angle DAC = 180^{\circ}$$

(sum of all the angles in a triangle is 180°)

$$\Rightarrow x^{\circ} + 96^{\circ} + x^{\circ} = 180^{\circ}$$
 [From 4, 6 and 7]

$$\Rightarrow 2x^{\circ} = 180^{\circ} - 96^{\circ} \Rightarrow 2x^{\circ} = \frac{84}{2} \Rightarrow x^{\circ} = 42^{\circ}$$

Hence, value of x = 42

(ii) Given in ΔABC,

Exterior $\angle ACE = 130^{\circ}$ and AD = BD = DC

To calculate the value of x.

Now,
$$\angle ACD + ACE = 180^{\circ}$$
 (1)

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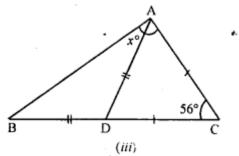
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Given that AC = CD, AD = BD

and
$$\angle BAC = x^{\circ}$$
, $\angle ACD = 56^{\circ}$

o evaluate the value of x.

low, in ∆ ACD

$$_{1}C = CD$$
 (given)

$$\angle ADC = \angle DAC$$
 (1)

In a triangle, angles opposite to equal sides are qual)

Also,
$$\angle ADC + \angle DAC + 56^{\circ} = 180^{\circ}$$

(sum of all angles in a triangle is 180°)

$$\Rightarrow$$
 $\angle DAC + \angle DAC + 56^{\circ} = 180^{\circ}$

[From equation (1) $\angle ADC = \angle DAC$]

$$\Rightarrow$$
 2 \angle DAC + 56° = 180°

$$\Rightarrow$$
 2 \angle DAC = 180° - 56° \Rightarrow 2 \angle DAC = 124°

$$\Rightarrow$$
 $\angle DAC = \frac{124^{\circ}}{2} \Rightarrow \angle DAC = 62^{\circ} \dots (2)$

.e.
$$\angle ADC = 62^{\circ}$$
 (3

 $[From (1) \angle DAC = \angle ADC]$

low, in ∆ABD

$$AD = BD$$
 (given)

$$\angle ABD = \angle BAD$$
 (4)

In a triangle, angles opposite equal sides are qual)

 $\exists ut \ ext. \ \angle ADC = \angle ABD + \angle BAD$

$$\Rightarrow$$
 62° = \angle BAD + \angle BAD [From (3) and (4)]

$$\Rightarrow$$
 62° = 2 \angle BAD \Rightarrow \angle BAD = 62°

$$\Rightarrow \angle BAD = \frac{62^{\circ}}{2} \Rightarrow \angle BAD = 31^{\circ}$$

... (5)

Now, from figure,
$$x^{\circ} = \angle BAD + \angle DAC$$

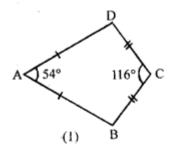
$$c^{\circ} = 31^{\circ} + 62^{\circ} \implies x^{\circ} = 93^{\circ} \text{ [From (4) and (5)]}$$

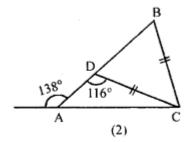
Hence, value of x = 93

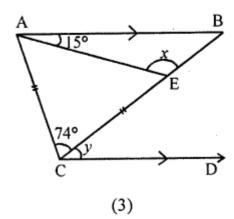
Question 6.

- (a) In the figure (1) given below, AB = AD, BC = DC. Find \angle ABC.
- (b)In the figure (2) given below, BC = CD. Find ∠ACB.
- (c) In the figure (3) given below, AB || CD and CA = CE. If \angle ACE = 74° and \angle BAE =15°, find the values of x and y.

Solution:







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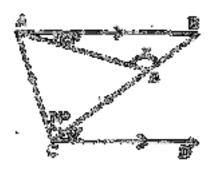
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In
$$\triangle AEC$$

 $AC = CE$
 $\therefore \angle CAE = \angle CEA$
But $ACE = 74^{\circ}$
 $\therefore \angle CAE + \angle CEA = 180^{\circ} - 74^{\circ} = 106^{\circ}$
 $\therefore \angle CAE = \angle CEA = \frac{106^{\circ}}{2} = 53^{\circ}$
Ext. $\angle AEB = \angle CAE + \angle ACE$
 $\Rightarrow x = 53^{\circ} + 74^{\circ} = 127^{\circ}$
 $\therefore AB \parallel CD$
 $\therefore \angle CAB + \angle ACD = 180^{\circ}$
(Sum of cointerior angles)
 $\Rightarrow 15^{\circ} + 53^{\circ} + 74^{\circ} + y^{\circ} = 180^{\circ}$
 $\Rightarrow 142^{\circ} + y = 180^{\circ}$
 $\Rightarrow y = 180^{\circ} - 142^{\circ} = 38^{\circ}$

Question 7.

In $\triangle ABC$, AB = AC, $\angle A = (5x + 20)^{\circ}$ and each of the base angle is $\frac{2}{5}$ th of $\angle A$. Find the measure of $\angle A$.

Solution:

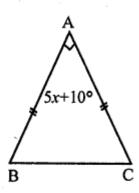
Given: In
$$\triangle ABC$$
, $AB = AC$

$$\angle A = (5x + 20)^{\circ}$$

$$\angle B = \angle C = \frac{2}{5}(\angle A)$$

$$=\frac{2}{5}(5x+20)^{\circ}$$

$$=2(x+4)^{\circ}=2x+8$$



:. But sum of angles of a triangle = 180°

$$\angle A + \angle B + \angle C = 180^{\circ}$$

$$\Rightarrow 5x + 20 + 2x + 8 + 2x + 8 = 180^{\circ}$$

$$9x + 36 = 180^{\circ}$$

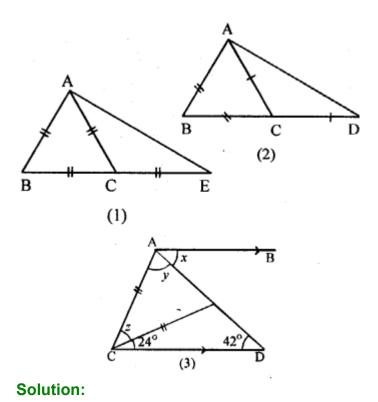
$$9x = 180 - 36 = 144$$

$$x = \frac{144}{9} = 16$$

$$\therefore \angle A = 5x + 20 = 5 \times 16 + 20$$
$$= 80^{\circ} + 20^{\circ} = 100^{\circ}$$

Question 8.

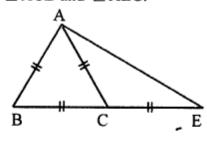
- (a) In the figure (1) given below, ABC is an equilateral triangle. Base BC is produced to E, such that BC'= CE. Calculate ∠ACE and ∠AEC.
- (b) In the figure (2) given below, prove that ∠ BAD : ∠ ADB = 3 : 1.
- (c) In the figure (3) given below, AB \parallel CD. Find the values of x, y and \angle .



(a) In following figure,

Given. ABC is an equilateral triangle BC = CE

To find. \angle ACE and \angle AEC.



(1)

As given that ABC is an equilateral triangle,

i.e.
$$\angle BAC = \angle B = \angle ACB = 60^{\circ}$$
 (1)

(each angle of an equilateral triangle is 60°)

Now, $\angle ACE = \angle BAC + CB$

(exterior angle is equal to sum of two interior opposite angles)

$$\Rightarrow \angle ACE = 60^{\circ} + 60^{\circ}$$
 [By

(1)

$$\Rightarrow$$
 \angle ACE = 120°

Now, in \triangle ACE

Given,
$$AC = CE$$
 (: $AC = BC = CE$)

$$\angle CAE = \angle AEC$$
 (2)

(In a triangle equal sides have equal angles opposite to them)

\lso,
$$\angle CAE + \angle AEC + 120^{\circ} = 80^{\circ}$$
(sum of all angles in a triangle is 180°)

$$\Rightarrow$$
 $\angle AEC + \angle AEC + 120^{\circ} = 180$ [By (2)]

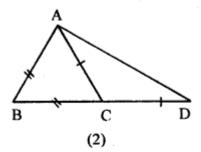
$$\Rightarrow$$
 2 \angle AEC = 180° - 120° \Rightarrow 2 \angle AEC = 60°

$$\Rightarrow 2 \angle AEC = \frac{60^{\circ}}{2} = 30^{\circ}$$

Hence, $\angle ACE = 120^{\circ}$ and $\angle AEC = 30^{\circ}$

b) In following figure

Given. \triangle ABD, AC meets BD in C. AB = BC, AC = CD.



To prove. $\angle BAD : \angle ADB = 3 : 1$

Proof. In AABC,

$$AB = BC$$
 (Given)

$$\therefore \angle ACB = \angle BAC$$
 (1)

(In a triangle, equal angles opposite to them)

In ∆ACD,

$$AC = CD$$
 (Given)

$$\therefore$$
 \angle ADC = \angle CAD

(In a triangle, equal sides have equal angles opposite to them)

$$\Rightarrow$$
 $\angle CAD = \angle ADC$ (2)

From, Adding (1) and (2), we get

$$\angle BAC + \angle CAD = \angle ACB + \angle ADC$$

 $\angle BAD = \angle ACB + \angle ADC$ (3)

Now, in △ACD

Exterior
$$\angle ACB = \angle CAD + \angle ADC$$
(4)

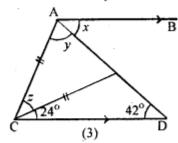
(In an triangle, exterior angle is equal to sum of two interior opposite angles)

$$\Rightarrow$$
 $\angle BAD : \angle ADC = 3 : 1$ (Q.E.D.)

(c) In following figure,

Given. AB || CD, \angle ECD = 24°, \angle CDE = 42°.

To find. The value of x, y and z.



Now, in \triangle CDE,

ext \angle CEA = 24° + 42° [In a triangle exterior angle is equal to sum of two interior opposite angles]

$$\angle CEA = 66^{\circ}$$
 (1)

Now, in \triangle ACE

$$AC = CE$$
 (Given)

$$\therefore$$
 $\angle CAE = \angle CEA$

(In a triangle equal side have equal angles opposite to them)

$$y = 66^{\circ}$$
 (By equation (1)(2)

Also,
$$y + z + \angle CEA = 180^{\circ}$$

(sum of all angles in a triangle is 180°)

$$\Rightarrow$$
 66° + z + 66° = 180°

[From equation (1) and

(2)

$$\Rightarrow z + 132^{\circ} = 180^{\circ} \Rightarrow z = 180^{\circ} - 132^{\circ}$$

$$\Rightarrow z = 48^{\circ} \qquad \dots (3)$$

Given that, AB || CD

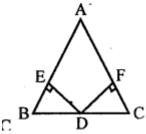
$$\therefore \angle x = \angle ADC \qquad \text{(alternate angles)}$$

$$x = 42^{\circ} \qquad \text{(4)}$$

Hence, from (2), (3) and (4) equation gives $x = 42^{\circ}$, $y = 66^{\circ}$ and $z = 48^{\circ}$

Question 9.

In the given figure, D is mid-point of BC, DE and DF are perpendiculars to AB and AC respectively such that DE = DF. Prove that ABC is an isosceles triangle.

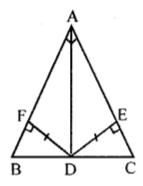


Solution:

Given: In $\triangle ABC$,

D is the mid-point of BC

DE \perp AB, DF \perp AC DE = DE



To prove: $\triangle ABC$ is an isosceles triangle

Proof: In right ΔBED and ΔCDF

Hypotenuse BD = DC (D is mid-point)

Side DF = DE (Given)

 $\therefore \Delta BED \cong \Delta CDF$ (RHS axiom)

 $\therefore \angle B = \angle C$

 \Rightarrow AB = AC (Sides opposite to equal angles)

 \therefore $\triangle ABC$ is an isosceles triangle

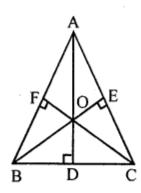
Question 10.

In the given figure, AD, BE and CF arc altitudes of \triangle ABC. If AD = BE = CF, prove that ABC is an equilateral triangle. Solution:

Given: In the figure given,

AD, BE and CF are altitudes of \triangle ABC and

$$AD = BE = CF$$



To prove : $\triangle ABC$ is an equilateral triangle

Proof: In the right $\triangle BEC$ and $\triangle BFC$

Hypotenuse BC = BC

(Common)

Side BE = CF

(Given)

 $\therefore \Delta BEC \cong \Delta BFC$

(RHS axiom)

∴ ∠C = ∠B

(c.p.c.t.)

AB = AC (Sides opposite to equal angles)

...(i)

Similarly we can prove that $\Delta CFA \cong \Delta ADC$

$$\therefore \angle A = \angle C$$

$$\therefore AB = BC$$

...(ii)

From (i) and (ii),

$$AB = BC = AC$$

∴ ∆ABC is an equilateral triangle

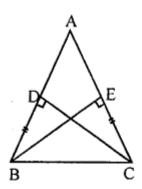
Question 11.

In a triangle ABC, AB = AC, D and E are points on the sides AB and AC respectively such that BD = CE. Show that:

- (i) $\triangle DBC \cong \triangle ECB$
- (ii) ∠DCB = ∠EBC
- (iii) OB = OC,where O is the point of intersection of BE and CD. Solution:

Given: In $\triangle ABC$, AB = AC

D and E are points on the sides AB and AC respectively such that BD = CE



To prove : (i) $\triangle DBC \cong \triangle ECB$

(ii) $\angle DCB = \angle EBC$

OB = OC where O is the point of intersection of BE and CD.

CD and BE are joined

Proof: In $\triangle ABC$, AB = AC

and BD = CE

 \therefore $\angle C = \angle B$ (Opposite to equal sides)

In ΔDBC and ΔECB

BC = BC (Common)

BD = CE (Given)

 $\angle B = \angle C$ (Proved)

(i) $\therefore \triangle DBC \cong \triangle ECB$ (SAS axiom)

 $(ii) :: \angle DCB = \angle EBC \qquad (c.p.c.t.)$

(iii) In ΔOBD and ΔOCE

$$\angle D = \angle E$$
 (each = 90°)

$$DB = EC$$
 (given)

 $\angle DOB = \angle EOC$ (vertically oppositive

angles)

$$: \Delta OBD \cong \Delta OCE$$
 (A.A.S. Axiom)

$$\therefore OB = OC \qquad (c.p.c.t.)$$

Question 12.

ABC is an isosceles triangle in which AB = AC. P is any point in the interior of

 \triangle ABC such that \angle ABP = \angle ACP. Prove that

- (a) BP = CP
- (b) AP bisects ∠BAC.

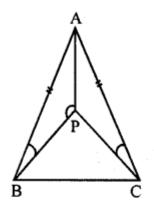
Solution:

Given: In an isosceles $\triangle ABC$, AB = AC

 \boldsymbol{P} is any point inside the ΔABC such that

 $\angle ABP = \angle ACP$

To prove: (a) BP = CP



(b) AP bisects ∠BAC

Proof: In $\triangle APB$ and $\triangle APC$

AP = AP (Common) AB = AC (Given)

 $\angle ABP = \angle ACP$ (Given)

 $\therefore \Delta APB \cong \Delta APC \qquad (SSA axiom)$

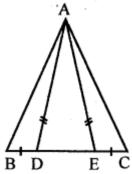
(i) \therefore BP = CP (c.p.c.t.)

and $\angle BAP = \angle CAP$ (c.p.c.t.)

∴ AP bisects ∠BAC

Question 13.

In the adjoining figure, D and E are points on the side BC of \triangle ABC such that BD = EC and AD = AE. Show that \triangle ABD $\cong \triangle$ ACE. Solution:



Given: In the given figure, D and E are the points on the sides BC of $\triangle ABC$,

BD = EC and AD = AE

To prove : $\triangle ABD \cong \triangle ACE$

Proof: : In $\triangle ADE$

 $\angle ADE = \angle AED$

∴ ∠AED = ∠ADE

But $\angle ADE + \angle ADB = 180^{\circ}$ (Linear pair)

and $\angle AED + \angle AEC = 180^{\circ}$ (Linear pair)

 \therefore $\angle ADB = \angle AEC$ ($\because \angle ADE = \angle AED$)

Now in ΔABD and ΔACE

AD = AE (Given)

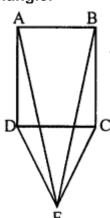
BD = CE (Given)

 $\angle ADB = \angle AEC$ (Proved)

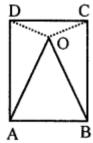
 $\therefore \Delta ABD \cong \Delta ACE \qquad (SAS axiom)$

Question 14.

(a) In the figure (i) given below, CDE is an equilateral triangle formed on a side CD of a square ABCD. Show that \triangle ADE \cong \triangle BCE and hence, AEB is an isosceles triangle.



(b) In the figure (ii) given below, O is a point in the interior of a square ABCD such that OAB is an equilateral triangle. Show that OCD is an isosceles triangle.



Solution:

(a) **Given**: In the figure, CDE is an equilateral triangle on the side CD of square ABCD

AE and BE are joined

To prove: (i) $\triangle ADE \cong \triangle BCE$

(ii) ΔAEB is an isosceles triangle.

Proof: • Each angle of a square is 90° and each angle of an equilateral triangle is 60°

$$\therefore$$
 $\angle ADE = \angle ADC + \angle CDE$

$$= 90^{\circ} + 60^{\circ} = 150^{\circ}$$

Similarly, $\angle BCE = 90^{\circ} + 60^{\circ} = 150^{\circ}$

Now in ΔADE and ΔBCE

$$AD = BC$$

(Sides of a square)

DE = CE (Sides of an equilateral triangle)

$$\angle ADE = \angle BCE$$

(Each 150°)

(i) $\therefore \Delta ADE \cong \Delta BCE$

(SAS axiom)

(ii) ∴ AE - BE

Now in $\triangle AEB$,

$$AE = BE$$

(Proved)

- ∴ ∆AEB is an isosceles triangle
- (b) Given: In the figure, O is a point in interior of the square ABCD such that OAB is an equilateral triangle.

To prove : ΔOCD is an isosceles triangle

Proof: ∵ ∆OAB is an equilateral triangle

$$\therefore$$
 OA = OB = AB

$$\angle OAD = \angle DAB - \angle OAB$$

$$= 90^{\circ} - 60^{\circ} = 30^{\circ}$$

```
Similarly, \angle OBC = 30^{\circ}

Now in \triangle OAD and \triangle OBC

OA = OB (Sides of equilateral triangle)

AD = BC (Sides of a square)

\angle OAD = \angle OBC (Each = 30°)

\therefore \triangle OAD \cong \triangle OBC (SAS axiom)

\therefore OD = OC (c.p.c.t.)

Now in \triangle OCD,

OD = OC
```

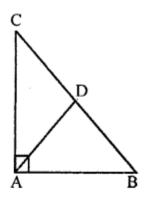
Question 15.

In the given figure, ABC is a right triangle with AB = AC. Bisector of \angle A meets BC at D. Prove that BC = 2AD. Solution:

In the given figure, $\triangle ABC$ is a right angled triangle, right angle at A

$$AB = AC$$

Bisector of ∠A meets BC at D



To prove : BC = 2AD

Proof: In right $\triangle ABC$, $\angle A = 90^{\circ}$ and AB =

AC

$$\therefore \angle B = \angle C = \frac{90^{\circ}}{2} = 45^{\circ} \ (\because \angle B + \angle C = 90^{\circ})$$

∵ AD is bisector of ∠A

$$\therefore \angle DAB = \angle DAC = \frac{90^{\circ}}{2} = 45^{\circ}$$

Now in ∆ADB

$$\angle DAB = \angle B$$

(Each 45°)

$$\therefore$$
 AD = DB

...(i)

Similarly we can prove that in $\triangle ADC$,

$$\angle DAC = \angle C = 45^{\circ}$$

...(ii)

Adding (i) and (ii),

Adding (i) and (ii),

$$AD + AD = DB + DC = BD + DC$$

$$\Rightarrow$$
 2AD = BC

Hence BC = 2AD

Question 1.

In $\triangle PQR$, $\angle P = 70^{\circ}$ and $\angle R = 30^{\circ}$. Which side of this triangle is longest? Give reason for your answer.

Solution:

In
$$\triangle PQR$$
, $\angle P = 70^{\circ}$, $\angle R = 30^{\circ}$
But $\angle P + \angle Q + \angle R = 180^{\circ}$
 $\Rightarrow 70^{\circ} + 30^{\circ} + \angle Q = 180^{\circ}$
 $\Rightarrow 100^{\circ} + \angle Q = 180^{\circ}$

$$\therefore \angle Q = 180^{\circ} - 100^{\circ} = 80^{\circ}$$

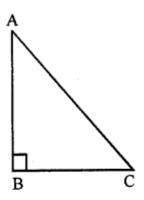
- \therefore $\angle Q = 80^{\circ}$ the greatest angle
- :. Its opposite side PR is the longest side (Side opposite to greatest angle is longest)

Question 2.

Show that in a right angled triangle, the hypotenuse is the longest side.

Solution:

Given: In right angled $\triangle ABC$, $\angle B = 90^{\circ}$



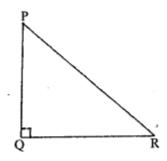
To prove : AC is the longest side

Proof: In $\triangle ABC$,

- ∴ ∠B = 90°
- ∴ ∠A and ∠C are acute angles i.e., less than 90°
- \therefore $\angle B$ is the greatest angle or $\angle B > \angle C$ and $\angle B > \angle A$
- ∴ AC > AB and AC > BC Hence AC is the longest side

Question 3.

PQR is a right angle triangle at Q and PQ : QR = 3:2. Which is the least angle. Solution:



Here, PQR is a right angle triangle at Q. Also given

that

PQ : QR = 3 : 2

Let PQ = 3x, then, QR = 2x

It is clear that QR is the least side.

Then, we know that the least angle has least side opposite to it.

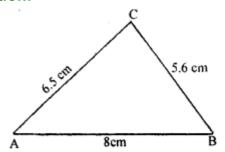
Hence, $\angle P$ is the least angle.

Question 4.

In \triangle ABC, AB = 8 cm, BC = 5.6 cm and CA = 6.5 cm. Which is (i) the greatest angle ?

(ii) the smallest angle?

Solution:



Given that AB = 8 cm, BC = 5.6 cm, CA = 6.5

Here AB is the greatest side

Then $\angle C$ is the greatest angle

(: the greater side has greater angle opposite to it)

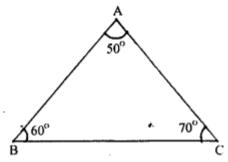
Also, BC is the least side

then ∠A is the least angle

(: the least side has least angle opposite to it)

Question 5.

In $\triangle ABC$, $\angle A = 50^{\circ}$, $\angle B = 60^{\circ}$, Arrange the sides of the triangle in ascending order. Solution:



Given in a ABC,

$$\angle A = 50^{\circ}$$
, $\angle B = 60^{\circ}$

$$\angle C = 180 - (\angle A + \angle B)$$

[sum of all angles in a triangle is 180°]

$$\Rightarrow$$
 $\angle C = 180^{\circ} - (50^{\circ} + 60^{\circ})$

$$\Rightarrow$$
 $\angle C = 180^{\circ} - 110^{\circ} \Rightarrow \angle C = 70^{\circ}$

Now,
$$\angle A \leq \angle B \leq \angle C$$

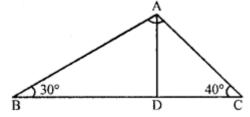
(: greater angles has greater side opposite to it)

Hence, sides of \triangle ABC in ascending order as BC, CA, AB.

Question 6.

In figure given alongside, $\angle B$ = 30°, $\angle C$ = 40° and the bisector of $\angle A$ meets BC at D. Show

- (i) BD > AD
- (ii) DC > AD
- (iii) AC > DC
- (iv) AB > BD



Solution:

Given: In $\triangle ABC$, $\angle B = 30^{\circ}$, $\angle C = 40^{\circ}$ and bisector of $\angle A$ meets BC at D

To prove:

(i)
$$BD > AD$$

(ii)
$$DC > AD$$

(iii)
$$AC > DC$$

(iv)
$$AB > BD$$

Proof: In $\triangle ABC$,

$$\angle B = 30^{\circ}$$
 and $\angle C = 40^{\circ}$

$$\angle BAC = 180^{\circ} - (30^{\circ} + 40^{\circ}) = 180^{\circ} - 70^{\circ} = 110^{\circ}$$

 \therefore AD is bisector of $\angle A$

$$\therefore \angle BAD = \angle CAD = \frac{110^{\circ}}{2} = 55^{\circ}$$

(i) Now in ΔABD,

(ii) In ΔACD,

$$\angle CAD > \angle C$$

(iii)
$$\angle ADC = 180^{\circ} - (40^{\circ} + 55^{\circ}) = 180^{\circ} - 95^{\circ} = 85^{\circ}$$

In ΔADC,

$$\therefore$$
 AC > DC

(iv) Similarly,

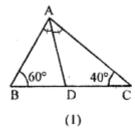
$$\angle ADB = 180^{\circ} - \angle ADC = 180^{\circ} - 85^{\circ} = 95^{\circ}$$

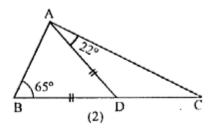
∴ In ∆ADB

Hence proved.

Question 7.

- (a) In the figure (1) given below, AD bisects ∠A. Arrange AB, BD and DC in the descending order of their lengths.
- (b) In the figure (2) given below, \angle ABD = 65°, \angle DAC = 22° and AD = BD. Calculate \angle ACD and state (giving reasons) which is greater : BD or DC ?

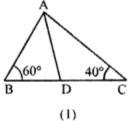




Solution:

(a) Given. In \triangle ABC, AD bisects \angle A, \angle B = 60° and \angle C = 40°

To arrange. AB, BD and DC in the descending order.



In A ABC

$$\angle BAC + \angle B + \angle C = 180^{\circ}$$

[sum of all angles in a triangle is 180°]

$$\Rightarrow$$
 $\angle BAC + 60^{\circ} + 40^{\circ} = 180^{\circ}$

[From given,
$$\angle B = 60^{\circ}$$
, $\angle C = 40^{\circ}$

$$\Rightarrow$$
 $\angle BAC = 180^{\circ} - 100^{\circ} \Rightarrow \angle BAC = 80^{\circ}$

∴ AD bisects ∠A

$$\therefore \angle BAD = \angle DAC = \frac{1}{2} \times \angle BAC$$

$$\Rightarrow$$
 $\angle BAD = \angle DAC = \frac{1}{2} \times 80^{\circ}$

$$\angle BAD = \angle DAC = 40^{\circ}$$
 (1)

In $\triangle ABD$, ext. $\angle ADC = \angle B + \angle BAD$

[In a triangle exterior angle is equal to sum of opposite interior angles]

$$\Rightarrow$$
 $\angle ADC = 100^{\circ}$ (2)

Similarly, In AACD, AADB

$$=40^{\circ}+40^{\circ}=80^{\circ}$$
 (3)

Now,
$$\angle ADB = 80^{\circ}$$
 [From (3)]

$$\angle BAD = 40^{\circ}$$
 [From (2)]

$$\angle DAC = 40^{\circ}$$
 [From (1)]

Now,
$$\angle ADB > \angle DAC = \angle BAD$$

[:
$$80^{\circ} > 40^{\circ} = 40^{\circ}$$
]

Hence, AB, DC, BD in the descending order of their lengths

(Note: It can also written as AB, BD, DC in the

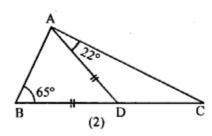
descending order :: DC = BD)

(b) Given. In \triangle ABC, \angle ABD = 65°

 \angle DAC = 22°, and AD = BD.

To calculate the \angle ACD and say which is greater, BD or DC.

Now, in $\triangle ABD$



 \therefore AD = BD (given)

Question 8.

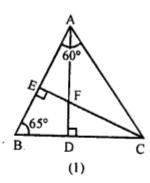
- (a) In the figure (1) given below, prove that (i) CF> AF (ii) DC>DF.
- (b) In the figure (2) given below, AB = AC.

Hence, BD is greater than DC.

Prove that AB > CD.

(c) In the figure (3) given below, AC = CD. Prove that BC < CD.

(a) Given. In ΔABC, AD⊥BC, CF⊥AB.
 AD and ∠E intersect at F.
 ∠BAC = 60°, ∠ABC = 65°



To prove. (i) CF > AF (ii) DC > DF**Proof.** (i) In \triangle AEC, $\angle B + \angle BEC + \angle BCE = 180^{\circ}$ (1) (sum of angles of a triangle = 180°) $\angle B = 65^{\circ}$ (Given) (2) $\angle BEC = 90^{\circ} [(CE \perp AB) Given]$ (3) Putting these value in equation (1), we get $65^{\circ} + 90^{\circ} + \angle BCE = 180^{\circ}$ $155^{\circ} + \angle BCE = 180^{\circ} \implies \angle BCE = 25^{\circ}$ $\angle DCF = 25^{\circ}$ [BCE = $\angle DCF$] (4) ⇒ Now in \triangle CDF, \angle DCF + \angle FDC + \angle CFD = 180° Solution:

[sum of all angles in a triangle is 180°]

$$\Rightarrow$$
 25 + 90° + \angle CFD = 180°

[From (4)
$$\angle$$
 DCF = 25° & AD \perp BC, \angle FDC = 90°]

$$\Rightarrow$$
 115° + \angle CFD = 180°

$$\Rightarrow$$
 \angle CFD = 180° - 115° \angle CFD = 65° (5)

Also,
$$\angle AFC + \angle CFD = 180^{\circ}$$

[AFD is a straight line]

$$\Rightarrow$$
 $\angle AFC + 65^{\circ} = 180^{\circ}$

$$\Rightarrow$$
 \angle AFC = 180 - 65° (\angle CFD = 65°)

$$\Rightarrow$$
 $\angle AFC = 115^{\circ}$ (6)

Now, in ACE,

$$\angle$$
ACE + \angle CEA + \angle BAC = 180°

[sum of all angles in a triangle is 180°]

$$\Rightarrow$$
 $\angle ACE + 90^{\circ} + 60^{\circ} = 180^{\circ}$

[
$$\because$$
 \angle CEA = 90°, \angle BAC = 60°]

$$\Rightarrow$$
 \angle ACE + 150° = 180°

$$\Rightarrow$$
 $\angle ACE = 180^{\circ} - 150^{\circ} \Rightarrow \angle ACE = 30^{\circ}...(7)^{\circ}$

Now, in \triangle AFC,

$$\angle AFC + \angle ACF + \angle FAC = 180^{\circ}$$

[sum of all angles in a triangle is 180°]

$$\Rightarrow$$
 115° + 30° + \angle FAC = 180° (By (6) and (7))

$$\Rightarrow$$
 145° + \angle FAC = 180°

$$\Rightarrow \angle FAC = 180^{\circ} - 145^{\circ}$$

$$\Rightarrow \angle FAC = 35^{\circ}$$
 (8)

```
Now, in \triangle AFC,
\angle FAC = 35°
                                  [From equation (&)]
\angle ACF = 30^{\circ}
                                  [From equation (7)]
∴ ∠FAC > ∠ACF
                             (35^{\circ} > 30^{\circ})
\therefore CF > AF
     [Greater angle has greater side opposite to it]
Now, in \triangle CDF,
\angle DCF = 25^{\circ}
                                  [From equation (4)]
\angle CFD = 65°
                                  [From equation (5)]
∴ ∠CFD > DCF
                                       (:: 65^{\circ} > 25^{\circ})
∴ DC > DF.
```

[greater angle has greater side opposite to it] (Q.E.D.)

(b) Given. In ΔABD, AC meets BD in C.

$$\angle B = 70^{\circ}, \angle D = 40^{\circ} AB = AC.$$

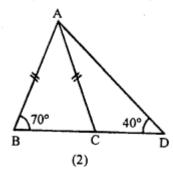
To prove. AB > CD.

Proof. In \triangle ABC,

$$AB = AC$$
 (given)

$$\therefore \angle ACB = \angle B \qquad \dots \dots (1)$$

(In a triangle, equal sides have equal angles opposite to them)



Also,
$$\angle B = 70^{\circ}$$

From (i) and (ii), we get

$$\angle$$
ACB + \angle ACD = 180° [BCD is a st. line]

$$\Rightarrow$$
 70° + \angle ACD = 180° [From equation (3)]

$$\Rightarrow$$
 $\angle ACD = 180^{\circ} - 70^{\circ}$

$$\Rightarrow$$
 $\angle ACD = 110^{\circ}$ (4)

Now, in \triangle ACD,

$$\angle$$
CAD + \angle ACD + \angle D = 180°

[sum of all angles in a triangle is 180°]

⇒
$$\angle$$
 CAD + 110° + 40° = 180° [From (4)

$$\angle ACD = 110^{\circ} \text{ and } \angle D = 40^{\circ}$$
 (given)]

$$\Rightarrow$$
 \angle CAD + 150° = 180°

$$\Rightarrow$$
 \angle CAD = 180 $^{\circ}$ - 150 $^{\circ}$

$$\Rightarrow$$
 $\angle CAD = 30^{\circ}$ (5)

Now, in \triangle ACD

$$\angle ACD = 110^{\circ}$$
 [From equation (4)]

$$\angle CAD = 30^{\circ}$$
 [From equation (5)]

$$\angle D = 40^{\circ}$$
 (given)

$$\therefore \angle D > \angle CAD$$
 (40° > 30°)

[Greater angle has greater side opposite to it]

$$\Rightarrow$$
 AB > CD [:: AB = AC given)]

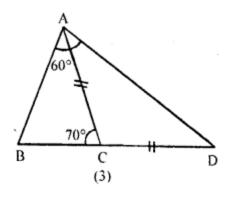
(Q.E.D.)

(c) Given. In
$$\triangle$$
 ACD, AC = CD, \angle BAD = 60°, \angle ACB = 70°

To prove. BC < CD.

Proof. In \triangle ACD,

$$\therefore$$
 AC = CD, (Given)



$$\therefore$$
 $\angle CAD = \angle CDA$ (1)

[In a triangle If two sides are equal, then angles opposite to them are also equal]

Also,
$$\angle ACB = 70^{\circ}$$
 (2)

Now,
$$\angle ACB = \angle CAD + \angle CDA$$

[exterior angle is equal to sum of two interior opposite angles]

$$\Rightarrow$$
 70° = \angle CAD + \angle CAD

[From (1) and (2)]

$$\Rightarrow$$
 70° = 2 \angle CAD

$$\Rightarrow 2 \angle CAD = 70^{\circ}$$

$$\Rightarrow \angle CAD = \frac{70^{\circ}}{2} = 35^{\circ}$$

$$\therefore \angle BAD = 60^{\circ}$$
 (given)

$$\therefore \angle BAC = \angle BAD - \angle CAD$$
$$= 60^{\circ} - 35^{\circ} = 25^{\circ}$$

$$\therefore$$
 $\angle BAC < \angle CAD$ [$\because 25^{\circ} < 35^{\circ}$]

[Greater angles has greater side opposite to it].

(Q.E.D.)

Question 9.

(a) In the figure (i) given below, $\angle B < \angle A$ and $\angle C < \angle D$. Show that AD < BC. (b) In the figure (ii) given below, D is any point on the side BC of $\triangle ABC$. If AB > AC, show that AB > AD. Solution:

(a) In the given figure,

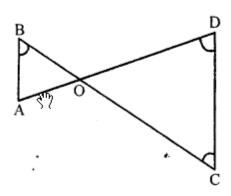
 $\angle B \le \angle A$ and $\angle C \le \angle D$

To prove : AD < BC

Proof: ln ∆ABO

 $\angle B < \angle A$ (Given)

∴ AO < BO ...(i)



Similarly in $\triangle OCD$

 $\angle C \le \angle D$

(Given)

.. OD < OC

Adding (i) and (ii)

AO + OD < BO + OC

 $\Rightarrow AD < BC$

Hence AD < BC

(b) In the given figure,

D is any point on BC of $\triangle ABC$

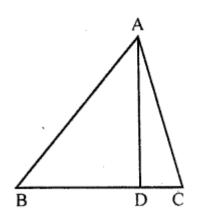
AB>AC

To prove: AB > AD

Proof: ∵ ln ∆ABC

AB>AC

 $\angle C > \angle B$



In AABD

Ext. $\angle ADC > \angle B$

∴ ∠ADC > ∠C

 $(\because \angle C > \angle B)$

: AC>AD

...(i)

But AB > AC

(Given) ...(ii)

:. From (i) and (ii),

AB>AD

Question 10.

- (i) Is it possible to construct a triangle with lengths of its sides as 4 cm, 3 cm and 7 cm? Give reason for your answer,
- (ii) Is it possible to construct a triangle with lengths of its sides as 9 cm, 7 cm and 17 cm? Give reason for your answer.
- (iii) Is it possible to construct a triangle with lengths of its sides as 8 cm, 7 cm and 4 cm? Give reason for your answer.

Solution:

(i) Length of sides of a triangle are 4 cm, 3 cm and 7 cm

We know that sum of any two sides of a triangle is greatar than its third side But 4 + 3 = 7 cm

Which is not possible

Hence to construction of a triangle with sides 4 cm, 3 cm and 7 cm is not possible.

(ii) Length of sides of a triangle are 9 cm, 7 cm and 17 cm

We know that sum of any two sides of a triangle is greater than its third side Now 9 + 7 = 16 < 17 . It is not possible to construct a triangle with these sides.

(iii) Length of sides of a triangle are 8 cm, 7 cm and 4 cm We know that sum of any two sides of a triangle is greater than its third side Now 7 + 4 = 11 > 8

Yes, It is possible to construct a triangle with these sides.

Multiple Choice Questions

Choose the correct answer from the given four options (1 to 18):

Question 1.

Which of the following is not a criterion for congruency of triangles?

- (a) SAS
- (b) ASA
- (c) SSA
- (d) SSS

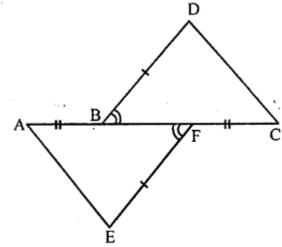
Solution:

Criteria of congruency of two triangles 'SSA' is not the criterion. (c)

Question 2.

In the adjoining figure, AB = FC, EF=BD and \angle AFE = \angle CBD. Then the rule by which \triangle AFE = \triangle CBD is

- (a) SAS
- (b) ASA
- (c) SSS
- (d) AAS



Solution:

In the figure given,

$$\triangle AFE \cong \triangle CBD$$
 by SAS axiom

$$AB + BF = BF + FC$$

$$(:: AB = FC)$$

$$\Rightarrow$$
 AF = BC

$$EF = BD$$

$$\angle AFE = \angle CBD$$

(b)

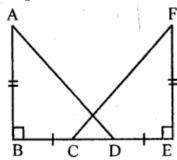
Question 3.

In the adjoining figure, AB \perp BE and FE \perp BE. If AB = FE and BC = DE, then

- (a) $\triangle ABD \cong \triangle EFC$
- (b) $\triangle ABD \cong \triangle FEC$
- (c) $\triangle ABD \cong \triangle ECF$
- (d) $\triangle ABD \cong \triangle CEF$

Solution:

In the figure given,



$$AB \perp BE$$
 and $FE \perp BE$

$$AB = FE$$
, $BC + CD = CD + DE$

$$(:: BC = DE)$$

$$\Rightarrow$$
 AB = FE and BD = CE, \angle B = \angle E

(Each 90°)

(b)

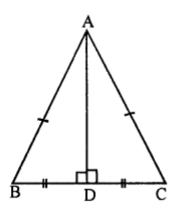
Question 4.

In the adjoining figure, AB=AC and AD is median of \triangle ABC, then AADC is equal to

- (a) 60°
- (b) 120°
- (c) 90°
- (d) 75°

Solution:

In the given figure, AB = ACAD is median of $\triangle ABC$



- \therefore D is mid-point \Rightarrow BD = DC
- ∴ AD ⊥ BC

(c)

Question 5.

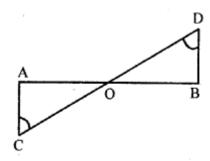
In the adjoining figure, O is mid point of AB. If \angle ACO = \angle BDO, then \angle OAC is equal to

- (a) ∠OCA
- (b) ∠ODB
- (c) ∠OBD
- (d) ∠BOD

Solution:

In the given figure, O is mid-point of AB,

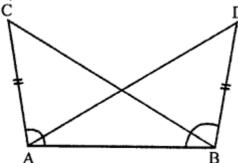
(Vertically opposite angles)



Question 6.

In the adjoining figure, AC = BD. If \angle CAB = \angle DBA, then \angle ACB is equal to

- (a) ∠BAD
- (b) ∠ABC
- (c) ∠ABD
- (d) ∠BDA



In the figure,
$$AC = BD$$

$$\angle CAB = \angle DBA$$

$$AB = AB$$
 (Common)

$$\therefore \Delta ABC \cong \Delta ABD$$
 (SAS axiom)

$$\therefore \angle ACB = \angle BDA$$
 (c.p.c.t.) (d)

Question 7.

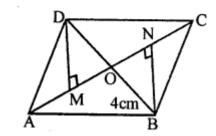
In the adjoining figure, ABCD is a quadrilateral in which BN and DM are drawn perpendiculars to AC such that BN = DM. If OB = 4 cm, then BD is

- (a) 6 cm
- (b) 8 cm
- (c) 10 cm
- (d) 12 cm

Solution:

In the given figure,

ABCD is a quadrilateral



BN
$$\perp$$
 AC, DM \perp AC

$$BN = DM$$
, $OB = 4$ cm

In \triangle ONB and \triangle OMD

$$BN = DM$$

$$\angle N = \angle M$$
 (Each 90°)

∠BON = DOM (Vertically opposite angles)

But
$$OB = 4 \text{ cm}$$

:.
$$BD = BO + OD = 4 + 4 = 8 \text{ cm}$$
 (b)

Question 8.

In $\triangle ABC$, AB = AC and $\angle B = 50^{\circ}$. Then $\angle C$ is equal to

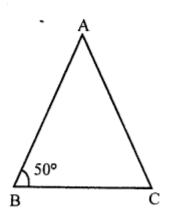
- (a) 40°
- (b) 50°

(c) 80°

(d) 130°

Solution:

In $\triangle ABC$, AB = AC



$$\therefore$$
 $\angle C = \angle B$ (Angles opposite to equal sides)

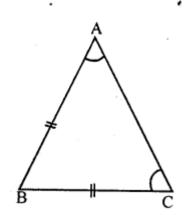
Question 9.

In $\triangle ABC$, BC = AB and $\angle B$ = 80°. Then $\angle A$ is equal to

(b)

- (a) 80°
- (b) 40°
- (c) 50°
- (d) 100°

In $\triangle ABC = BC = AB$



 \therefore $\angle A = \angle C$ (Angles opposite to equal sides)

$$\therefore \angle A + \angle C = 180^{\circ} - 80^{\circ} = 100^{\circ}$$

But
$$\angle A = \angle C = 100^{\circ}$$

and 2∠A

$$\angle A = \frac{100^{\circ}}{2} = 50^{\circ}$$
 (c)

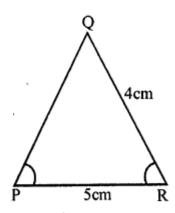
Question 10.

In $\triangle PQR$, $\angle R = \angle P$, QR = 4 cm and PR = 5 cm. Then the length of PQ is

- (a) 4 cm
- (b) 5 cm
- (c) 2 cm
- (d) 2.5 cm

$$\angle R = \angle P$$
, QR = 4 cm

$$PR = 5 cm$$



$$\therefore \angle P = \angle R$$

$$PQ = QR$$

:. (Sides opposite to equal angles

$$\therefore PQ = 4 cm$$
 (a)

Question 11.

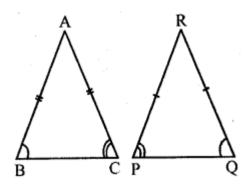
In \triangle ABC and APQR, AB = AC, \angle C = \angle P and \angle B = \angle Q. The two triangles are

- (a) isosceles but not congruent
- (b) isosceles and congruent
- (c) congruent but isosceles
- (d) neither congruent nor isosceles

In ΔABC and ΔPQR

$$AB = AC, \angle C = \angle P$$

$$\angle B = \angle Q$$



$$\therefore$$
 In \triangle ABC, AB = AC

$$\angle C = \angle B$$

(Opposite to equal sides)

But
$$\angle C = \angle P$$
 and $\angle B = \angle Q$

$$\therefore RQ = PR$$

(a)

Question 12.

Two sides of a triangle are of lenghts 5 cm and 1.5 cm. The length of the third side of the triangle can not be

- (a) 3.6 cm
- (b) 4.1 cm
- (c) 3.8 cm
- (d) 3.4 cm

Solution:

In a triangle, two sides are 5 and 1.5 cm.

- : Sum of any two sides of a triangle is greater than its third side
- \therefore Third side < (5 + 1.5) cm
- \Rightarrow Third side < 6.5 cm or third side + 1.5 > 5 cm or third side > 5 - 1.5 = 3.5 cm
- :. Third side cannot be equal to 3.4 cm (d)

Question 13.

If a, b, c are the lengths of the sides of a trianlge, then

```
(a) a - b > c
```

(b)
$$c > a + b$$

$$(c) c = a + b$$

(d)
$$c < A + B$$

a, b, c are the lengths of the sides of a triangge than a + b > c or c < a + b (Sum of any two sides is greater than its third side) **(d)**

Question 14.

It is not possible to construct a triangle when the lengths of its sides are

- (a) 6 cm, 7 cm, 8 cm
- (b) 4 cm, 6 cm, 6 cm
- (c) 5.3 cm, 2.2 cm, 3.1 cm
- (d) 9.3 cm, 5.2 cm, 7.4 cm

Solution:

We know that sum of any two sides of a triangle is greater than its third side $2.2 + 3.1 = 5.3 \Rightarrow 5.3 = 5.3$ is not possible (c)

Question 15.

In $\triangle PQR$, if $\angle R > \angle Q$, then

- (a) QR > PR
- (b) PQ > PR
- (c) PQ < PR
- (d) QR < PR

Solution:

In $\triangle PQR$, $\angle R > \angle Q$

∴ PQ > PR **(b)**

Question 16.

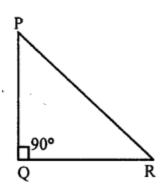
If triangle PQR is right angled at Q, then

- (a) PR = PQ
- (b) PR < PQ
- (c) PR < QR
- (d) PR > PQ

In right angled ΔPQR ,

Side opposite to greater angle is greater

(d)



Question 17.

If triangle ABC is obtuse angled and ∠C is obtuse, then

- (a) AB > BC
- (b) AB = BC
- (c) AB < BC
- (d) AC > AB

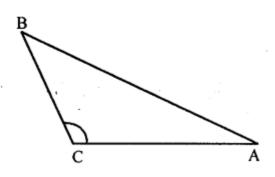
Solution:

In $\triangle ABC$, $\angle C$ is obtuse angle

AB > BC

(Side opposite to greater angle is greater)

(a)



Question P.Q.

A triangle can be constructed when the lengths of its three sides are

- (a) 7 cm, 3 cm, 4 cm
- (b) 3.6 cm, 11.5 cm, 6.9 cm
- (c) 5.2 cm, 7.6 cm, 4.7 cm
- (d) 33 mm, 8.5 cm, 49 mm

We know that in a triangle, if sum of any two sides is greater than its third side, it is possible to construct it 5.2 cm, 7.6 cm, 4.7 cm is only possible. **(c)**

Question P.Q.

A unique triangle cannot be constructed if its

- (a) three angles are given
- (b) two angles and one side is given
- (c) three sides are given
- (d) two sides and the included angle is given

Solution:

A unique triangle cannot be constructed if its three angle are given, (a)

Question 18.

If the lengths of two sides of an isosceles are 4 cm and 10 cm, then the length of the third side is

- (a) 4 cm
- (b) 10 cm
- (c) 7 cm
- (d) 14 cm

Solution:

Lengths of two sides of an isosceles triangle are 4 cm and 10 cm, then length of the third side is 10 cm

(Sum of any two sides of a triangle is greater than its third side and 4 cm is not possible as 4 + 4 > 10 cm.

Chapter Test

Question 1.

In triangles ABC and DEF, $\angle A = \angle D$, $\angle B = \angle E$ and AB = EF. Will the two triangles be congruent? Give reasons for your answer.

Solution:

In AABC and ADEF

 $\angle A = \angle D$

 $\angle B = \angle E$

AB = EF

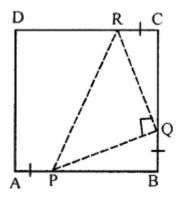
In \triangle ABC, two angles and included side is given but in \triangle DEF, corresponding angles are equal but side is not included of there angle.

Triangles cannot be congruent.

Question 2.

In the given figure, ABCD is a square. P, Q and R are points on the sides AB, BC and CD respectively such that AP= BQ = CR and \angle PQR = 90°. Prove that

- (a) $\triangle PBQ \cong \triangle QCR$
- (b) PQ = QR
- $(c) \angle PRQ = 45^{\circ}$



Given: In the given figure, ABCD is a square P, Q and R are the points on the sides AB, BC and CD respectively such that

$$AP = BQ = CR, \angle PQR = 90^{\circ}$$

To prove: (a) $\triangle PBQ \cong \triangle QCR$

(b)
$$PQ = QR$$

(c)
$$\angle PRQ = 45^{\circ}$$

Proof:
$$: AB = BC = CD$$
 (Sides of square)

and
$$AP = BQ = CR$$
 (Given)

Subtracting, we get

$$AB - AP = BC - BQ = CD - CR$$

$$\Rightarrow$$
 PB = QC = RD

Now in $\triangle PBQ$ and $\angle QCR$

$$PB = QC$$
 (Proved)

$$BQ = CR$$
 (Given)

$$\angle B = \angle C$$
 (Each 90°)

$$\therefore \Delta PBQ \cong \Delta QCR \qquad (SAS axiom)$$

$$\therefore PQ = QR \qquad (c.p.c.t.)$$

But
$$\angle PQR = 90^{\circ}$$
 (Given)

$$\angle RPQ = \angle PRQ$$

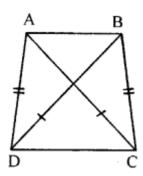
(Angles opposite to equal angles)

But
$$\angle$$
RPQ + \angle PRQ = 90°

$$\angle RPQ = \angle PRQ = \frac{90^{\circ}}{2} = 45^{\circ}$$

Question 3.

In the given figure, AD = BC and BD = AC. Prove that \angle ADB = \angle BCA. Solution:



Given: In the figure,

AD = BC, BD = AC

To prove : $\angle ADB = \angle BCA$ Proof : In $\triangle ADB$ and $\triangle ACB$

AB=AB (Common)

AD=BC (Given)

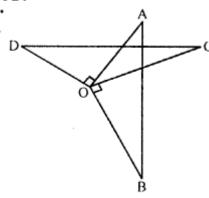
BD=AC (Given)

∴ \triangle ADB \cong \triangle ACB (SSS axiom)

∴ \angle ADB= \angle BCA (c.p.c.t.)

Question 4.

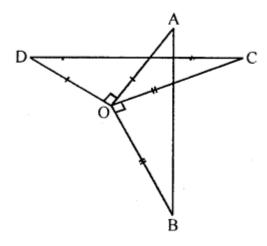
In the given figure, OA \perp OD, OC X OB, OD = OA and OB = OC. Prove that AB = CD.



13

Given : In the figure, OA \perp OD, OC \perp OB.

$$OD = OA, OB = OC$$



To prove : AB = CD

Proof: $\angle AOD = \angle COB$ (each 90°)

Adding∠AOC (both sides)

 $\angle AOD + \angle AOC = \angle AOC + \angle COB$

 $\Rightarrow \angle COD = \angle AOB$

Now, in $\triangle AOB$ and $\triangle DOC$

OA = OD (given)

OB = OC (given)

 $\angle AOB = \angle COD$ (proved)

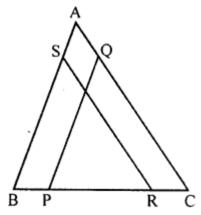
 $\therefore \triangle AOB \cong \triangle DOC$ (SAS axiom)

 $\therefore AB = CD \qquad (c.p.c.t.)$

Question 5.

In the given figure, PQ || BA and RS CA. If BP = RC, prove that:

- (i) \triangle BSR $\cong \triangle$ PQC
- (ii) BS = PQ
- (iii) RS = CQ.

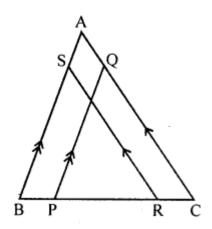


Solution:

Given: In the given figure,

PQ || BA, RS || CA

BP = RC



To prove:

(i)
$$\Delta BSR \cong \Delta PQC$$

$$(ii)$$
 BS = PQ

$$(iii)$$
 RS = CQ

Proof: BP = RC

$$\therefore$$
 BC - RC = BC - BP

$$\therefore$$
 BR = PC

Now, in $\triangle BSR$ and $\triangle PQC$

$$\angle B = \angle P$$
 (corresponding angles)
 $\angle R = \angle C$ (corresponding angles)
 $BR = PC$ (proved)
 $\therefore \Delta BSR \cong \Delta PQC$ (ASA axiom)

Question 6.

In the given figure, AB = AC, D is a point in the interior of \triangle ABC such that \angle DBC = \angle DCB. Prove that AD bisects \angle BAC of \triangle ABC. Solution:

Given : In the figure given, AB = ACD is a point in the interior of $\triangle ABC$

Such that $\angle DBC = \angle DCB$

To prove : AD bisects ∠BAC

Construction: Join AD and produced it to

BC in E

Proof: In $\triangle ABC$,

AB = AC

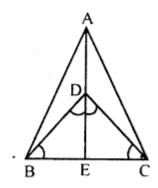
 $\therefore \angle B = \angle C$ (Angles opposite to equal sides)

and $\angle DBC = \angle DCB$

(Given)

Subtracting, we get

$$\angle B - \angle DBC = \angle C - \angle DCB$$



$$\Rightarrow \angle ABD = \angle ACD$$

Now in ΔABD and ΔACD

AD = AD

 $\angle ABD = \angle ACD$ (Proved)

AB=AC (Given)

 $\therefore \Delta ABD \cong \Delta ACD$ (SAS axiom)

 $\therefore \angle BAD = \angle CAD \qquad (c.p.c.t.)$

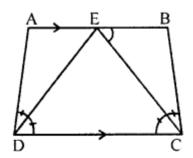
∴ AD is bisector of ∠BAC

Question 7.

In the adjoining figure, AB || DC. CE and DE bisects \angle BCD and \angle ADC respectively. Prove that AB = AD + BC.

(Common)

Given: In the given figure, AB || DC CE and DE bisects ∠BCD and ∠ADC respectively



To prove: AB = AD + BC

Proof: :: AD || DC and ED is the transversal

$$\therefore$$
 $\angle AED = \angle EDC$ (Alternate angles)

=
$$\angle ADC$$
 (: ED is bisector of $\angle ADC$)

$$\therefore$$
 AD=AE ...(i)

(Sides opposite to equal angles)

Similarly,

$$\angle BEC = \angle ECD = \angle ECB$$

$$\therefore BC = EB \qquad \dots(ii)$$

Adding (i) and (ii),

$$AD + BC = AE + EB = AB$$

$$\therefore AB = AD + BC$$

Question 8.

In \triangle ABC, D is a point on BC such that AD is the bisector of \angle BAC. CE is drawn parallel to DA to meet BD produced at E. Prove that \triangle CAE is isosceles Solution:

Given: In $\triangle ABC$,

D is a point on BC such that AD is the bisector of ∠BAC

CE | DA to meet BD produced at E

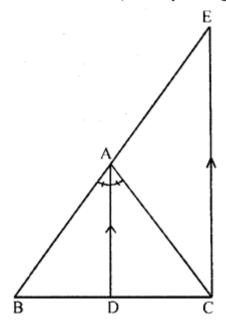
To prove : $\triangle CAE$ is an isosceles

Proof: AD EC and AC is its transversal

 $\therefore \angle DAC = \angle ACE \qquad (Alternate angles)$

and $\angle BAD = \angle CEA$

(Corresponding angles)



But $\angle BAD = \angle DAC$

(∴ AD is bisector of ∠BAC)

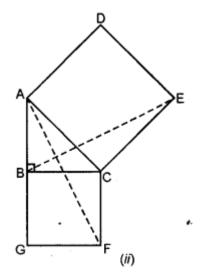
∴ ∠ACE = ∠CAE

AE = AC (Sides opposite to equal angles)

 \therefore \triangle ACE is an isosceles triangle.

Question 9.

In the figure (ii) given below, ABC is a right angled triangle at B, ADEC and BCFG are squares. Prove that AF = BE.



. Given. In right $\triangle ABC$, $\angle B = 90^{\circ}$

ADEC and BCFG are squares on the sides AC and BC of \triangle ABC respectively AF and BE are joined.

To prove. AE = BE

Proof. $\angle ACE = \angle BCF$

(each 90°)

Adding ∠ACB both sides

 $\angle ACB + \angle ACE = \angle ACB + \angle BCF$

⇒ ∠BCE = ∠ACF

Now in ABCE and AACF,

CF = AC (sides of a square)

BC = CF (sides of a square)

 $\angle BCE = \angle ACF \text{ (proved)}$

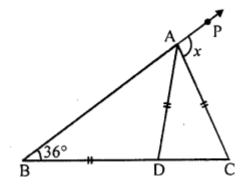
 $\therefore \triangle BCE \cong \triangle ACF (SAS postulate)$

$$\therefore BE = AF \tag{c.p.c.t.}$$

Hence proved.

Question 10.

In the given figure, BD = AD = AC. If \angle ABD = 36°, find the value of x .



Given: In the figure, BD = AD = AC

∠ABD = 36°

To find: Measure of x.

Proof: In $\triangle ABD$,

$$AD = BD$$
 (given)

$$\therefore$$
 $\angle ABD = \angle BAD = 36^{\circ}$ ($\because \angle ABD = 36^{\circ}$)

$$\therefore Ext. \angle ADC = \angle ABD + \angle BAD$$
$$= 36^{\circ} + 36^{\circ} = 72^{\circ}$$

But in $\triangle ADC$

$$AD = AC$$

$$\angle ADC = \angle ACD = 72^{\circ}$$
and Ext. $\angle PBC = \angle ABC + \angle ACD$

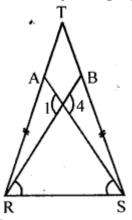
$$= 36^{\circ} + 72^{\circ} = 108^{\circ}$$

$$x = 108^{\circ}$$

Question 11.

In the adjoining figure, TR = TS, $\angle 1$ = 2 $\angle 2$ and $\angle 4$ = 2 $\angle 3$. Prove that RB = SA.

(sum of interior opposite angles)



Given: In the figure, RST is a triangle

$$TR = TS$$
,

$$\angle 1 = 2\angle 2$$
 and $\angle 4 = 2\angle 3$

To prove : RB = SA

Proof: $\angle 1 = \angle 4$

(Vertically opposite angles)

But
$$2\angle 2 = \angle 1$$
 and $2\angle 3 = 4$

$$\therefore 2 \angle 2 = 2 \angle 3$$

$$\therefore$$
 But \angle TRS = \angle TSR (\because TR = TS given)

$$\therefore$$
 \angle TRS - \angle BRS = \angle TSR - \angle ASR

Now in $\triangle RBT$ and $\triangle SAT$

$$\angle T = \angle T$$

(Common)

$$TR = TS$$

(Given)

and
$$\angle TRB = \angle TSA$$

(Proved)

$$\therefore \Delta RBT \cong \Delta SAT$$

(SAS axiom)

$$\therefore RB = SA$$

(c.p.c.t.)

Question 12.

(a) In the figure (1) given below, find the value of x.

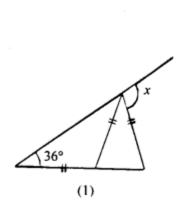
(b) In the figure (2) given below, AB = AC and DE || BC. Calculate

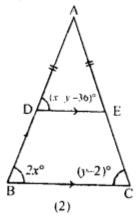
(i)x

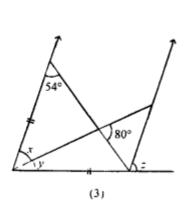
(ii) y

(iii) ∠BAC

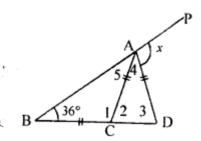
(c) In the figure (1) given below, calculate the size of each lettered angle.







(a) We have to calculate the value of x.



Now, in
$$\triangle$$
 ABC

Also,
$$36^{\circ} + \angle 1 + \angle 5 = 180^{\circ} \ [: AC = BC]$$

[sum of all angles in a triangle is 180°]

$$\Rightarrow$$
 36° + $\angle 1$ + 36° = 180° [from (1)]

$$\Rightarrow$$
 72° + $\angle 1 = 180°$ \Rightarrow $\angle 1 = 180° - 72°$

$$\Rightarrow$$
 $\angle 1 = 108^{\circ}$ (2)

Also,
$$\angle 1 + \angle 2 = 180^{\circ}$$
 (Linear pair)

$$\Rightarrow$$
 108° + \angle 2 = 180° [From (2)]

$$\Rightarrow$$
 $\angle 2 = 180^{\circ} - 108^{\circ} \Rightarrow \angle 2 = 72^{\circ}$ (3)

Also,
$$\angle 2 = \angle 3$$
 (AC = AD)

$$\therefore \angle 3 = 72^{\circ}$$
 [From (3)].... (4)

Now, in △ACD

$$\angle 2 + \angle 3 + \angle 4 = 180^{\circ}$$

[sum of all angles in a triangle is 180°]

$$\Rightarrow$$
 72° + 72° + $\angle 4$ = 180° [From (3) and (4)]

$$\Rightarrow$$
 144° + \angle 4 = 180° \Rightarrow \angle 4 = 180° - 144°

$$\Rightarrow$$
 $\angle 4 = 36^{\circ}$ (5)

$$36^{\circ} + 36^{\circ} + x = 180^{\circ}$$
 [From (1) and (5)]

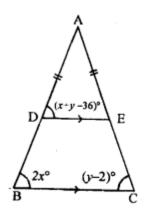
$$72^{\circ} + x = 180 \implies x = 108^{\circ}$$

Hence, value of $x = 108^{\circ}$ Ans.

(b) Given.
$$AB = AC$$
, and $DE \parallel BC$

$$\angle ADE = (x + y - 36)^{\circ}$$

$$\angle ABC = 2x^{\circ} \text{and } \angle ACB = (y-2)^{\circ}$$



To Calculate. (i) x (ii) y (iii) $\angle BAC$

Now, in AABC

$$\therefore AB = AC$$

$$2x = y - 2$$

[In a triangle equal sides here equal angle opposite to them]

$$2x - y = -2$$
 (1)

∴ DE || BC,

$$x + y - 36 = 2x$$

[corresponding angles]

$$\Rightarrow x + y - 2x = 36 \Rightarrow -x + y = 36$$
 (2)
From equation (1) and (2),

$$2x - y = -2$$

$$-x + y = 36$$

$$x = 34$$

Adding,

Substituting the value of x in equation (1), we get

$$2 \times 34 - y = -2 \implies 68 - y = -2$$

$$\Rightarrow 68 + 2 = y \Rightarrow 70 = y \Rightarrow y = 70$$

Hence, value of $x = 34^{\circ}$ and value of $y = 70^{\circ}$

(iii) In AABC

$$\angle BAC + 2 x^{\circ} + (y - 2)^{\circ} = 180^{\circ}$$

[sum of all angles in a triangle is 180°]

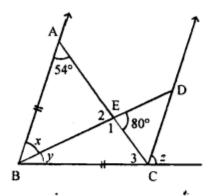
$$\Rightarrow \angle BAC + 2 \times 34^{\circ} + (70 - 2)^{\circ} = 180^{\circ}$$
(Substituting the value of x and y)

$$\Rightarrow$$
 $\angle BAC + 68^{\circ} + 68^{\circ} = 180^{\circ}$

$$\Rightarrow$$
 $\angle BAC = 180^{\circ} - 136^{\circ} \Rightarrow \angle BAC = 44^{\circ}$

Hence, value of $\angle BAC = 44^{\circ}$ Ans.

(c) Given.
$$\angle BAE = 54^{\circ}$$
, $\angle DEC = 80^{\circ}$ and $AB = BC$.



To calculate. The value of x, y and z.

Now
$$\angle 2 = 80^{\circ}$$
 (1)

(vertically opposite angles

∴ AC and BD cut at point E)

In AABE.

$$54^{\circ} + x + \angle 2 = 180^{\circ}$$

(sum of all angles in triangle is 180°)

$$\Rightarrow$$
 54° + x + 80° = 180° (\therefore $\angle 2 = 80°$)

$$\Rightarrow$$
 134° + $x = 180°$ \Rightarrow $x = 180° - 134°$

$$\Rightarrow x = 46^{\circ}$$

Now,
$$\angle 1 + 80^\circ = 180^\circ$$
 (Linear pair)

$$\angle 1 = 180^{\circ} - 80^{\circ} \implies \angle 1 = 100^{\circ} \dots (2)$$

Also,
$$AB = BC$$
 (given)

$$\angle 3 = 54^{\circ}$$

(In a triangle equal sides have equal angles)

Now, in △ABC

$$54^{\circ} + (x + y) + \angle 3 = 180^{\circ}$$

(substituting the value of x and $\angle 3$)

$$\Rightarrow$$
 154° + y = 180° \Rightarrow y = 180° - 154°

$$\Rightarrow y = 26^{\circ} \qquad \dots (3)$$

$$\therefore$$
 AB || CD, $\therefore x+y=z$

[corresponding angles]

$$\Rightarrow$$
 46° + 26° = z [From (2) and (3)]

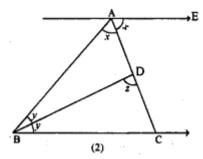
$$\Rightarrow$$
 $z = 46^{\circ} + 26^{\circ}$ \Rightarrow $z = 72^{\circ}$

Hence, value of $x = 46^{\circ}$, $y = 26^{\circ}$

and $z = 72^{\circ}$

Question 13.

- (a) In the figure (1) given below, AD = BD = DC and ∠ACD = 35°. Show that
- (i) AC > DC (ii) AB > AD.
- (b) In the figure (2) given below, prove that
- (i) $x + y = 90^{\circ}$ (ii) $z = 90^{\circ}$ (iii) AB = BC



Solution:

(a) Given: In the figure given,

$$AD = BD = DC$$

To prove : (i) AC > DC, (ii) AB > AD

Proof: In \triangle ADC, AD = DC

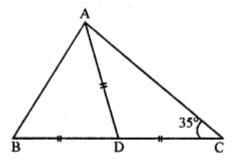
$$\Rightarrow \angle ADC = 180^{\circ} - (\angle DAC + \angle DCA)$$

$$\therefore$$
 $\angle ADC = 180^{\circ} - (35^{\circ} + 35^{\circ})$

$$= 180^{\circ} - 70^{\circ} = 110^{\circ}$$

and Ext.
$$\angle ADB = \angle DAC + \angle DCA = 35^{\circ} +$$

$$35^{\circ} = 70^{\circ}$$



$$:: AD = BD$$

$$\angle BAD = \angle ABD$$

But
$$\angle BAD + \angle ABD = 180^{\circ} - \angle ADB$$

$$\Rightarrow$$
 \angle ABD + \angle ABD = $180^{\circ} - 70^{\circ} = 110^{\circ}$

$$\Rightarrow 2\angle ABD = 110^{\circ} \Rightarrow \angle ABD = \frac{110^{\circ}}{2} = 55^{\circ}$$

(b) Given.
$$\angle EAC = \angle BAC = x$$

$$\angle ABD = \angle DBC = y$$

$$\angle BDC = z$$

To prove. (i)
$$x+y = 90^{\circ}$$
 (ii) $z = 90^{\circ}$

$$(iii)$$
 AB = BC

$$\therefore \angle ACB = x$$
 [Alternate angles](1)

In ∆ABC

$$x + (y + y) + \angle ACB = 180^{\circ}$$

[sum of all angles in a triangle is 180°]

$$\Rightarrow x + 2y + x = 180^{\circ}$$
 [From (1)]

$$\Rightarrow$$
 2x + 2y = 180°

$$\Rightarrow$$
 2 $(x + y) = 180^{\circ}$ (proved) (2)

$$\Rightarrow x + y = 90^{\circ}$$

```
(ii) Now, in \triangle BCD,

y + z + \angle BCD = 180°

[sum of all angles in a triangle is 180°]

\Rightarrow y + z + x = 180°

\Rightarrow 90° + z = 180° [From (2), x + y = 90°]

\Rightarrow z = 90° (proved) ..... (3)

(iii) In \triangle ABC

\angle BAC = \angle BAC = x (each same value)

\therefore AB = CB

(In a triangle equal angles has equal sides)

(proved)
```

Question 14.

In the given figure, ABC and DBC are two isosceles triangles on the same base BC and vertices A and D are on the same side of BC. If AD is extended to intersect BC at P, show that

- (i) $\triangle ABD \cong \triangle ACD$
- (ii) $\triangle ABP \cong \triangle ACP$
- (iii) AP bisects ∠A as well as ∠D
- (iv) AP is the perpendicular bisector of BC.

Given: In the figure, two isosceles triangles ABC and DBC are on the same base BC. With vertices A and D on the same side of BC.

AD is joined and produced to meet BC at P.

To prove:

- (i) $\triangle ABD \cong \triangle ACD$
- (ii) $\triangle ABP \cong \triangle ACP$
- (iii) AP bisects ∠A as well as ∠D
- (iv) AP is the perpendicular bisector of BC
 Proof: ΔABC and ΔDBC are isosceles
 AB = AC and DB = DC
- (i) Now in ΔABD and ΔACP

AB = AC (Proved) DB = DC (Proved)

AD = AD (Common)

 $\therefore \triangle ABD \cong \triangle ACD$ (SSS axiom)

 $\therefore \angle BAD = \angle CAD \qquad (c.p.c.t.)$

∴ ADP bisects ∠A

and $\angle ADB = \angle ADC$ (c.p.c.t.)

But $\angle ADB + \angle BDP = \angle CAD + \angle CDP = 180^{\circ}$

- ∴ ∠BDP = ∠CDP
- ∴ ADP bisects ∠D also

Now in $\triangle APB$ and $\triangle ACD$

AB = AC (Given)

AP = AP (Common)

and $\angle BAD = \angle CAD$ (Proved)

 \therefore $\angle APB \cong \triangle ACP$ (SAS axiom)

 $\therefore BP = CP \qquad (c.p.c.t.)$

and $\angle APB = \angle APC$

But $\angle APB + \angle APC = 180^{\circ}$ (Linear pair)

∴ ∠APB = ∠APC = 90°

and BP = PC

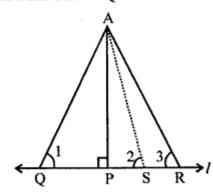
.. AP is perpendicular bisector of BC

Question 15.

In the given figure, $AP \perp I$ and PR > PQ. Show that AR > AQ.

Given: In the given figure,

 $AP \perp l$ and PR > PQ



To prove: AR > AQ

Construction: Take a point S on l,

Such that PS = PQ

Join A and S

Proof: In $\triangle AQP$ and $\triangle ASP$

$$AP = AP$$
 (Common)

$$QP = SP$$
 (Given)

$$\angle APQ = \angle APS$$
 (Each 90°)

$$\therefore \Delta APQ \cong \Delta APS$$
 (SAS axiom)

In AASR

Ext. ASP > ∠ARS

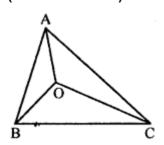
$$\Rightarrow \angle 2 > \angle 3$$

$$\Rightarrow \angle 1 > \angle 3$$
 $(\because \angle 1 = \angle 2)$

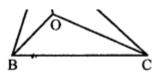
$$\therefore AR > AQ$$

Question 16.

If O is any point in the interior of a triangle ABC, show that OA + OB + OC > $\frac{1}{2}$ (AB + BC + CA).



Given: In the figure, O is any point in the interior of \triangle ABC.



To prove : OA + OB + OC >
$$\frac{1}{2}$$
 (AB + BC + CA)

Construct: Join B and C.

Proof: In ∆OBC

$$OB + OC > BC$$
 ...(i)

(Sum of two sides of a triangle is greater than

its third side)

Similarly OC + OA > CA

and OA + OB > AB

Adding are get,

$$(OB + OC + OC + OA + OA + OB) > BC +$$

CA + AB

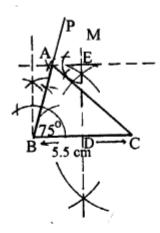
$$\Rightarrow$$
 2(OA + OB + OC) > AB + BC +CA

$$\Rightarrow OA + OB + OC > \frac{1}{2}(AB + BC + CA)$$

Question P.Q.

Construct a triangle ABC given that base BC = 5.5 cm, \angle B = 75° and height = 4.2 cm.

Given. In a triangle ABC, Base BC = 5.5. cm, $\angle B = 750^{\circ}$ and height = 4.2 cm.

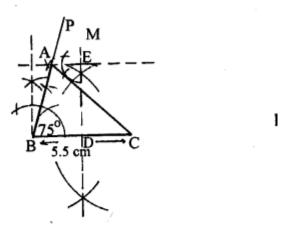


Required. To construct a triangle ABC.

Steps of Construction:

- (1) Draw a line BC = 5.5 cm.
- (2) Draw \angle PBC = 75°.
- (3) Draw the perpendicular bisector of BC and cut the BC at point D.
- (4) Cut the DM at point E such that DE = 4.2 cm.
- (5) Draw the line at point which is parallel to line BC.
- (6) This parallel line cut the BP at point A.
- (7) Join AC.
- (8) ABC is the required triangle.

Given. In a triangle ABC, Base BC = 5.5. cm, $\angle B = 750^{\circ}$ and height = 4.2 cm.



Required. To construct a triangle ABC.

Steps of Construction:

- (1) Draw a line BC = 5.5 cm.
- (2) Draw \angle PBC = 75°.
- (3) Draw the perpendicular bisector of BC and cut the BC at point D.
- (4) Cut the DM at point E such that DE = 4.2 cm.
- (5) Draw the line at point which is parallel to line BC.
- (6) This parallel line cut the BP at point A.
- (7) Join AC.
- (8) ABC is the required triangle.

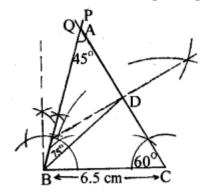
Question P.Q.

Construct a triangle ABC in which BC = 6.5 cm, \angle B = 75° and \angle A = 45°. Also construct median of A ABC passing through B. Solution:

Given. In \triangle ABC, BC = 6.5 cm, \angle B = 75° and \angle A = 45°.

Required. (i) To construct a triangle ABC.

(ii) Construct median of \triangle ABC passing through B.



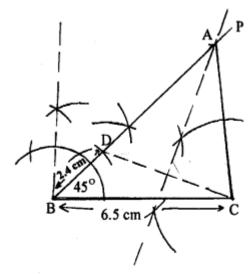
Step of Construction.

- (1) Draw a line BC = 6.5 cm.
- (2) Make $\angle PBC = 75^{\circ}$.
- (3) Make \angle BCQ = 60°.
- (4) BP and CQ cut at point A.
- (5) ABC is the required triangle.
- (6) Draw the bisector of AC.
- (7) The bisector line cut the line AC at point D.
- (8) Join BD.
- (9) BD is the required median of \triangle ABC passing through B.

Question P.Q.

Construct triangle ABC given that AB – AC = 2.4 cm, BC = 6.5 cm. and \angle B = 45°.

Given. A triangle ABC in which AB – AC = 2.4 cm, BC = 6.5 cm, \angle B = 4.5°. Required. To construct a triangle ABC.



Steps of Construction:

- (1) Draw BC = 6.5 cm.
- (2) Draw BP making angle 65° with BC.
- (3) From BP, cut BD = 2.4 cm.
- (4) Join D and C.
- (5) Draw perpendicular bisector of DC which cuts BP at A.
- (6) Join A and C.
- (7) ABC is the required triangle.