### Exercise – 2A

1.

### Sol:

$$x^{2} + 7x + 12 = 0$$
⇒  $x^{2} + 4x + 3x + 12 = 0$ 
⇒  $x(x+4) + 3(x+4) = 0$ 
⇒  $(x+4)(x+3) = 0$ 
⇒  $(x+4) = 0$  or  $(x+3) = 0$ 
⇒  $(x+4) = 0$  or  $(x+3) = 0$ 

$$\Rightarrow x = -4 \text{ or } x = -3$$
Sum of zeroes  $= -4 + (-3) = \frac{-7}{1} = \frac{-(coefficient \ of \ x^{2})}{(coefficient \ of \ x^{2})}$ 
Product of zeroes  $= (-4)(-3) = \frac{12}{1} = \frac{constant \ term}{(coefficient \ of \ x^{2})}$ 

2.

### Sol:

$$x^{2} - 2x - 8 = 0$$

$$\Rightarrow x^{2} - 4x + 2x - 8 = 0$$

$$\Rightarrow x(x - 4) + 2(x - 4) = 0$$

$$\Rightarrow (x - 4) (x + 2) = 0$$

$$\Rightarrow (x - 4) = 0 \text{ or } (x+2) = 0$$

$$\Rightarrow x = 4 \text{ or } x = -2$$
Sum of zeroes =  $4 + (-2) = 2 = \frac{2}{1} = \frac{-(coefficient of x)}{(coefficient of x^{2})}$ 
Product of zeroes =  $(4) (-2) = \frac{-8}{1} = \frac{constant term}{(coefficient of x^{2})}$ 

**3.** 

### Sol:

We have:

$$f(x) = x^{2} + 3x - 10$$

$$= x^{2} + 5x - 2x - 10$$

$$= x(x + 5) - 2(x + 5)$$

$$= (x - 2)(x + 5)$$

$$\therefore f(x) = 0 \Rightarrow (x - 2)(x + 5) = 0$$

$$\Rightarrow x - 2 = 0 \text{ or } x + 5 = 0$$

$$\Rightarrow x = 2 \text{ or } x = -5.$$

So, the zeroes of f(x) are 2 and -5.

Sum of zeroes = 
$$2 + (-5) = -3 = \frac{-3}{1} = \frac{-(coefficient of x)}{(coefficient of x^2)}$$
  
Product of zeroes =  $2 \times (-5) = -10 = \frac{-10}{1} = \frac{constant term}{(coefficient of x^2)}$ 

4.

### Sol:

We have:

$$f(x) = 4x^{2} - 4x - 3$$

$$= 4x^{2} - (6x - 2x) - 3$$

$$= 4x^{2} - 6x + 2x - 3$$

$$= 2x (2x - 3) + 1(2x - 3)$$

$$= (2x + 1) (2x - 3)$$

$$\therefore f(x) = 0 \Rightarrow (2x + 1) (2x - 3) = 0$$

$$\Rightarrow 2x + 1 = 0 \text{ or } 2x - 3 = 0$$

$$\Rightarrow x = \frac{-1}{2} \text{ or } x = \frac{3}{2}$$

So, the zeroes of f(x) are  $\frac{-1}{2}$  and  $\frac{3}{2}$ 

Sum of zeroes 
$$=$$
  $\left(\frac{-1}{2}\right) + \left(\frac{3}{2}\right) = \frac{-1+3}{2} = \frac{2}{2} = 1 = \frac{-\left(\text{coefficient of } x\right)}{\left(\text{coefficient of } x^2\right)}$ 

Product of zeroes = 
$$\left(\frac{-1}{2}\right) \times \left(\frac{3}{2}\right) = \frac{-3}{4} = \frac{constant\ term}{(coefficient\ of\ x^2)}$$

5.

### Sol:

We have:

$$f(x) = 5x^{2} - 4 - 8x$$

$$= 5x^{2} - 8x - 4$$

$$= 5x^{2} - (10x - 2x) - 4$$

$$= 5x^{2} - 10x + 2x - 4$$

$$= 5x (x - 2) + 2(x - 2)$$

$$= (5x + 2) (x - 2)$$

$$f(x) = 0 \Rightarrow (5x + 2) (x - 2) = 0$$

$$\Rightarrow 5x + 2 = 0 \text{ or } x - 2 = 0$$

$$\Rightarrow x = \frac{-2}{5} \text{ or } x = 2$$

So, the zeroes of f(x) are  $\frac{-2}{5}$  and 2.

Sum of zeroes = 
$$\left(\frac{-2}{5}\right) + 2 = \frac{-2+10}{5} = \frac{8}{5} = \frac{-(coefficient of x)}{(coefficient of x^2)}$$
  
Product of zeroes =  $\left(\frac{-2}{5}\right) \times 2 = \frac{-4}{5} = \frac{constant term}{(coefficient of x^2)}$ 

**6.** 

Sol:  

$$2\sqrt{3}x^2 - 5x + \sqrt{3}$$

$$\Rightarrow 2\sqrt{3}x^2 - 2x - 3x + \sqrt{3}$$

$$\Rightarrow 2x (\sqrt{3}x - 1) - \sqrt{3} (\sqrt{3}x - 1) = 0$$

$$\Rightarrow (\sqrt{3}x - 1) \text{ or } (2x - \sqrt{3}) = 0$$

$$\Rightarrow (\sqrt{3}x - 1) = 0 \text{ or } (2x - \sqrt{3}) = 0$$

$$\Rightarrow x = \frac{1}{\sqrt{3}} \text{ or } x = \frac{\sqrt{3}}{2}$$

$$\Rightarrow x = \frac{1}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{\sqrt{3}}{3} \text{ or } x = \frac{\sqrt{3}}{2}$$
Sum of zeroes 
$$= \frac{\sqrt{3}}{3} + \frac{\sqrt{3}}{2} = \frac{5\sqrt{3}}{6} = \frac{-(coefficient of x)}{(coefficient of x^2)}$$
Product of zeroes 
$$= \frac{\sqrt{3}}{3} \times \frac{\sqrt{3}}{2} = \frac{\sqrt{3}}{6} = \frac{constant term}{(coefficient of x^2)}$$

7.

Sol:  

$$f(x) = 2x^{2} - 11x + 15$$

$$= 2x^{2} - (6x + 5x) + 15$$

$$= 2x^{2} - 6x - 5x + 15$$

$$= 2x (x - 3) - 5 (x - 3)$$

$$= (2x - 5) (x - 3)$$

$$\therefore f(x) = 0 \Rightarrow (2x - 5) (x - 3) = 0$$

$$\Rightarrow 2x - 5 = 0 \text{ or } x - 3 = 0$$

$$\Rightarrow x = \frac{5}{2} \text{ or } x = 3$$
So, the zeroes of  $f(x)$  are  $\frac{5}{2}$  and  $\frac{3}{2}$ 

So, the zeroes of f(x) are  $\frac{5}{2}$  and 3.

Sum of zeroes 
$$=\frac{5}{2} + 3 = \frac{5+6}{2} = \frac{11}{2} = \frac{-(coefficient \ of \ x)}{(coefficient \ of \ x^2)}$$
  
Product of zeroes  $=\frac{5}{2} \times 3 = \frac{-15}{2} = \frac{constant \ term}{(coefficient \ of \ x^2)}$ 

8.

Sol:  

$$4x^2 - 4x + 1 = 0$$
  
 $\Rightarrow (2x)^2 - 2(2x)(1) + (1)^2 = 0$ 

$$\Rightarrow (2x - 1)^2 = 0 \qquad [\because a^2 - 2ab + b^2 = (a - b)^2]$$

$$\Rightarrow (2x - 1)^2 = 0$$

$$\Rightarrow x = \frac{1}{2} \text{ or } x = \frac{1}{2}$$
Sum of zeroes =  $\frac{1}{2} + \frac{1}{2} = 1 = \frac{1}{1} = \frac{-(coefficient \ of \ x)}{(coefficient \ of \ x^2)}$ 
Product of zeroes =  $\frac{1}{2} \times \frac{1}{2} = \frac{1}{4} = \frac{constant \ term}{(coefficient \ of \ x^2)}$ 

9.

### Sol:

We have:

$$f(x) = x^2 - 5$$

It can be written as  $x^2 + 0x - 5$ .

$$= \left(x^2 - \left(\sqrt{5}\right)^2\right)$$
$$= \left(x + \sqrt{5}\right)\left(x - \sqrt{5}\right)$$

$$\therefore f(x) = 0 \Rightarrow (x + \sqrt{5}) (x - \sqrt{5}) = 0$$
$$\Rightarrow x + \sqrt{5} = 0 \text{ or } x - \sqrt{5} = 0$$
$$\Rightarrow x = -\sqrt{5} \text{ or } x = \sqrt{5}$$

So, the zeroes of f(x) are  $-\sqrt{5}$  and  $\sqrt{5}$ .

Here, the coefficient of x is 0 and the coefficient of  $x^2$  is 1.

Sum of zeroes = 
$$-\sqrt{5} + \sqrt{5} = \frac{0}{1} = \frac{-(coefficient \ of \ x)}{(coefficient \ of \ x^2)}$$

Sum of zeroes = 
$$-\sqrt{5} + \sqrt{5} = \frac{0}{1} = \frac{-(coefficient \ of \ x)}{(coefficient \ of \ x^2)}$$
  
Product of zeroes =  $-\sqrt{5} \times \sqrt{5} = \frac{-5}{1} = \frac{constant \ term}{(coefficient \ of \ x^2)}$ 

10.

#### Sol:

We have:

$$f(x) = 8x^2 - 4$$

It can be written as  $8x^2 + 0x - 4$ 

$$= 4 \{ (\sqrt{2}x)^2 - (1)^2 \}$$
  
= 4 (\sqrt{2}x + 1) (\sqrt{2}x - 1)

$$\therefore f(x) = 0 \Rightarrow (\sqrt{2}x + 1)(\sqrt{2}x - 1) = 0$$

$$\Rightarrow (\sqrt{2}x + 1) = 0 \text{ or } \sqrt{2}x - 1 = 0$$
$$\Rightarrow x = \frac{-1}{\sqrt{2}} \text{ or } x = \frac{1}{\sqrt{2}}$$

$$\rightarrow X - \sqrt{2} \text{ of } X - \sqrt{2}$$

So, the zeroes of f(x) are  $\frac{-1}{\sqrt{2}}$  and  $\frac{1}{\sqrt{2}}$ 

Here the coefficient of x is 0 and the coefficient of  $x^2$  is  $\sqrt{2}$ 

Sum of zeroes 
$$=$$
  $\frac{-1}{\sqrt{2}} + \frac{1}{\sqrt{2}} = \frac{-1+1}{\sqrt{2}} = \frac{0}{\sqrt{2}} = \frac{-(coefficient \ of \ x^2)}{(coefficient \ of \ x^2)}$ 

Sum of zeroes 
$$=$$
  $\frac{-1}{\sqrt{2}} + \frac{1}{\sqrt{2}} = \frac{-1+1}{\sqrt{2}} = \frac{0}{\sqrt{2}} = \frac{-(coefficient of x)}{(coefficient of x^2)}$   
Product of zeroes  $=$   $\frac{-1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} = \frac{-1 \times 4}{2 \times 4} = \frac{-4}{8} = \frac{constant term}{(coefficient of x^2)}$ 

### 11.

### Sol:

We have,

$$f(u) = 5u^2 + 10u$$

It can be written as 5u (u+2)

$$\therefore$$
 f (u) = 0  $\Rightarrow$  5u = 0 or u + 2 = 0

$$\Rightarrow$$
 u = 0 or u =  $-2$ 

So, the zeroes of f(u) are -2 and 0.

Sum of the zeroes = 
$$-2 + 0 = -2 = \frac{-2 \times 5}{1 \times 5} = \frac{-10}{5} = \frac{-(coefficient of x)}{(coefficient of u^2)}$$

Sum of the zeroes = 
$$-2 + 0 = -2 = \frac{-2 \times 5}{1 \times 5} = \frac{-10}{5} = \frac{-(coefficient \ of \ x)}{(coefficient \ of \ u^2)}$$
  
Product of zeroes =  $-2 \times 0 = 0 = \frac{0 \times 5}{1 \times 5} = \frac{-0}{5} = \frac{constant \ term}{(coefficient \ of \ u^2)}$ 

### 12.

$$3x^2 - x - 4 = 0$$

$$\Rightarrow 3x^2 - 4x + 3x - 4 = 0$$

$$\Rightarrow$$
x (3x - 4) + 1 (3x - 4) = 0

$$\Rightarrow (3x - 4)(x + 1) = 0$$

$$\Rightarrow$$
 (3x - 4) or (x + 1) = 0

$$\Rightarrow$$
 x =  $\frac{4}{3}$  or x = -1

Sum of zeroes = 
$$\frac{4}{3}$$
 + (-1) =  $\frac{1}{3}$  =  $\frac{-(coefficient of x^2)}{(coefficient of x^2)}$ 

Sum of zeroes = 
$$\frac{4}{3} + (-1) = \frac{1}{3} = \frac{-(coefficient \ of \ x)}{(coefficient \ of \ x^2)}$$
  
Product of zeroes =  $\frac{4}{3} \times (-1) = \frac{-4}{3} = \frac{constant \ term}{(coefficient \ of \ x^2)}$ 

### **13.**

### Sol:

Let 
$$\alpha = 2$$
 and  $\beta = -6$ 

Sum of the zeroes, 
$$(\alpha + \beta) = 2 + (-6) = -4$$

Product of the zeroes,  $\alpha\beta = 2 \times (-6) = -12$ 

... Required polynomial = 
$$x^2$$
 -  $(\alpha + \beta)x + \alpha\beta = x^2 - (-4)x - 12$   
=  $x^2 + 4x - 12$ 

Sum of the zeroes = 
$$-4 = \frac{-4}{1} = \frac{-(coefficient of x)}{(coefficient of x^2)}$$
  
Product of zeroes =  $-12 = \frac{-12}{1} = \frac{constant term}{(coefficient of x^2)}$ 

Product of zeroes = 
$$-12 = \frac{-12}{1} = \frac{constant\ term}{(coefficient\ of\ x^2)}$$

14.

Let 
$$\alpha = \frac{2}{3}$$
 and  $\beta = \frac{-1}{4}$ .

Sum of the zeroes = 
$$(\alpha + \beta) = \frac{2}{3} + (\frac{-1}{4}) = \frac{8-3}{12} = \frac{5}{12}$$

Product of the zeroes, 
$$\alpha\beta = \frac{2}{3} \times \left(\frac{-1}{4}\right) = \frac{-2}{12} = \frac{-1}{6}$$

$$\therefore \text{ Required polynomial} = x^2 - (\alpha + \beta)x + \alpha\beta = x^2 - \frac{5}{12}x + \left(\frac{-1}{6}\right)$$
$$= x^2 - \frac{5}{12}x - \frac{1}{6}$$

Sum of the zeroes = 
$$\frac{5}{12} = \frac{-(coefficient of x)}{(coefficient of x^2)}$$

Sum of the zeroes = 
$$\frac{5}{12} = \frac{-(coefficient of x)}{(coefficient of x^2)}$$
  
Product of zeroes =  $\frac{-1}{6} = \frac{constant term}{(coefficient of x^2)}$ 

**15.** 

#### Sol:

Let  $\alpha$  and  $\beta$  be the zeroes of the required polynomial f(x).

Then 
$$(\alpha + \beta) = 8$$
 and  $\alpha\beta = 12$ 

$$\therefore f(x) = x^2 - (\alpha + \beta)x + \alpha\beta$$

$$\Rightarrow f(x) = x^2 - 8x + 12$$

Hence, required polynomial  $f(x) = x^2 - 8x + 12$ 

∴ 
$$f(x) = 0 \Rightarrow x^2 - 8x + 12 = 0$$
  
⇒  $x^2 - (6x + 2x) + 12 = 0$ 

$$\Rightarrow x^2 - 6x - 2x + 12 = 0$$

$$\Rightarrow x(x-6)-2(x-6)=0$$

$$\Rightarrow (x-2)(x-6) = 0$$

$$\Rightarrow$$
 (x - 2) = 0 or (x - 6) = 0

$$\Rightarrow$$
 x = 2 or x = 6

So, the zeroes of f(x) are 2 and 6.

16.

### Sol:

Let  $\alpha$  and  $\beta$  be the zeroes of the required polynomial f(x).

Then 
$$(\alpha + \beta) = 0$$
 and  $\alpha\beta = -1$ 

$$\therefore f(x) = x^2 - (\alpha + \beta)x + \alpha\beta$$

$$\Rightarrow f(x) = x^2 - 0x + (-1)$$

$$\Rightarrow$$
 f(x) =  $x^2 - 1$ 

Hence, required polynomial  $f(x) = x^2 - 1$ .

$$\therefore f(x) = 0 \Rightarrow x^2 - 1 = 0$$
$$\Rightarrow (x+1)(x-1) = 0$$
$$\Rightarrow (x+1) = 0 \text{ or } (x-1) = 0$$

$$\Rightarrow$$
 x = -1 or x = 1

So, the zeroes of f(x) are -1 and 1.

**17.** 

### Sol:

Let  $\alpha$  and  $\beta$  be the zeroes of the required polynomial f(x).

Then 
$$(\alpha + \beta) = \frac{5}{2}$$
 and  $\alpha\beta = 1$ 

$$\therefore f(x) = x^2 - (\alpha + \beta) x + \alpha \beta$$

$$\Rightarrow f(x) = x^2 - \frac{5}{2}x + 1$$

$$\Rightarrow$$
 f(x) = 2x<sup>2</sup> - 5x + 2

Hence, the required polynomial is  $f(x) = 2x^2 - 5x + 2$ 

$$f(x) = 0 \Rightarrow 2x^{2} - 5x + 2 = 0$$

$$\Rightarrow 2x^{2} - (4x + x) + 2 = 0$$

$$\Rightarrow 2x^{2} - 4x - x + 2 = 0$$

$$\Rightarrow 2x (x - 2) - 1 (x - 2) = 0$$

$$\Rightarrow (2x - 1) (x - 2) = 0$$

$$\Rightarrow (2x - 1) = 0 \text{ or } (x - 2) = 0$$

$$\Rightarrow$$
 x =  $\frac{1}{2}$  or x = 2

So, the zeros of f(x) are  $\frac{1}{2}$  and 2.

18.

Sol:

We can find the quadratic equation if we know the sum of the roots and product of the roots by using the formula

$$x^2$$
 – (Sum of the roots)x + Product of roots = 0  
 $\Rightarrow x^2 - \sqrt{2}x + \frac{1}{3} = 0$ 

$$\Rightarrow 3x^2 - 3\sqrt{2}x + 1 = 0$$

19.

Sol:

Given: 
$$ax^2 + 7x + b = 0$$

Since,  $x = \frac{2}{3}$  is the root of the above quadratic equation

Hence, it will satisfy the above equation.

Therefore, we will get

$$a\left(\frac{2}{3}\right)^{2} + 7\left(\frac{2}{3}\right) + b = 0$$

$$\Rightarrow \frac{4}{9}a + \frac{14}{3} + b = 0$$

$$\Rightarrow 4a + 42 + 9b = 0$$

$$\Rightarrow 4a + 9b = -42 \qquad \dots (1)$$

Since, x = -3 is the root of the above quadratic equation

Hence, It will satisfy the above equation.

Therefore, we will get

$$a (-3)^2 + 7 (-3) + b = 0$$

$$\Rightarrow 9a - 21 + b = 0$$

$$\Rightarrow$$
 9a + b = 21 .....(2)

From (1) and (2), we get a = 3, b = -6

20.

Sol:

Given: (x + a) is a factor of  $2x^2 + 2ax + 5x + 10$ 

So, we have

$$x + a = 0$$

$$\Rightarrow$$
 x =  $-a$ 

Now, it will satisfy the above polynomial.

Therefore, we will get

$$2(-a)^2 + 2a(-a) + 5(-a) + 10 = 0$$

$$\Rightarrow 2a^2 - 2a^2 - 5a + 10 = 0$$

$$\Rightarrow$$
 -5a = -10

$$\Rightarrow$$
 a = 2

### 21.

Sal

Given:  $x = \frac{2}{3}$  is one of the zero of  $3x^3 + 16x^2 + 15x - 18$ 

Now, we have

$$x = \frac{2}{3}$$

$$\Rightarrow x - \frac{2}{3} = 0$$

Now, we divide  $3x^3 + 16x^2 + 15x - 18$  by  $x - \frac{2}{3}$  to find the quotient

$$\begin{array}{c}
3x^2 + 18x + 27 \\
x - \frac{2}{3} \\
3x^3 + 16x^2 + 15x - 18 \\
3x^3 - 2x^2 \\
- +
\end{array}$$

So, the quotient is  $3x^2 + 18x + 27$ 

Now,

$$3x^2 + 18x + 27 = 0$$

$$\Rightarrow 3x^2 + 9x + 9x + 27 = 0$$

$$\Rightarrow 3x(x+3) + 9(x+3) = 0$$

$$\Rightarrow (x+3)(3x+9) = 0$$
  
\Rightarrow (x+3) = 0 or (3x+9) = 0  
\Rightarrow x = -3 or x = -3

### Exercise – 2B

1.

#### Sol:

The given polynomial is  $p(x) = (x^3 - 2x^2 - 5x + 6)$   $\therefore p(3) = (3^3 - 2 \times 3^2 - 5 \times 3 + 6) = (27 - 18 - 15 + 6) = 0$   $p(-2) = [(-2^3) - 2 \times (-2)^2 - 5 \times (-2) + 6] = (-8 - 8 + 10 + 6) = 0$   $p(1) = (1^3 - 2 \times 1^2 - 5 \times 1 + 6) = (1 - 2 - 5 + 6) = 0$   $\therefore 3, -2$  and 1 are the zeroes of p(x), Let  $\alpha = 3, \beta = -2$  and  $\gamma = 1$ . Then we have:  $(\alpha + \beta + \gamma) = (3 - 2 + 1) = 2 = \frac{-(coefficient \ of \ x^2)}{(coefficient \ of \ x^3)}$   $(\alpha\beta + \beta\gamma + \gamma\alpha) = (-6 - 2 + 3) = \frac{-5}{1} = \frac{coefficient \ of \ x}{coefficient \ of \ x^3}$  $\alpha\beta\gamma = \{3 \times (-2) \times 1\} = \frac{-6}{1} = \frac{-(constant \ term)}{(coefficient \ of \ x^3)}$ 

2.

$$p(x) = (3x^{3} - 10x^{2} - 27x + 10)$$

$$p(5) = (3 \times 5^{3} - 10 \times 5^{2} - 27 \times 5 + 10) = (375 - 250 - 135 + 10) = 0$$

$$p(-2) = [3 \times (-2^{3}) - 10 \times (-2^{2}) - 27 \times (-2) + 10] = (-24 - 40 + 54 + 10) = 0$$

$$p\left(\frac{1}{3}\right) = \left\{3 \times \left(\frac{1}{3}\right)^{3} - 10 \times \left(\frac{1}{3}\right)^{2} - 27 \times \frac{1}{3} + 10\right\} = \left(3 \times \frac{1}{27} - 10 \times \frac{1}{9} - 9 + 10\right)$$

$$= \left(\frac{1}{9} - \frac{10}{9} + 1\right) = \left(\frac{1 - 10 - 9}{9}\right) = \left(\frac{0}{9}\right) = 0$$

$$\therefore 5, -2 \text{ and } \frac{1}{3} \text{ are the zeroes of } p(x).$$
Let  $\alpha = 5, \beta = -2$  and  $\gamma = \frac{1}{3}$ . Then we have:
$$(\alpha + \beta + \gamma) = \left(5 - 2 + \frac{1}{3}\right) = \frac{10}{3} = \frac{-(coefficient \ of \ x^{2})}{(coefficient \ of \ x^{3})}$$

$$(\alpha\beta + \beta\gamma + \gamma\alpha) = (-10 - \frac{2}{3} + \frac{5}{3}) = \frac{-27}{3} = \frac{coefficient \ of \ x}{coefficient \ of \ x^{3}}$$

$$\alpha\beta\gamma = \left\{5 \times (-2) \times \frac{1}{3}\right\} = \frac{-10}{3} = \frac{-(constant \ term)}{(coefficient \ of \ x^{3})}$$

3.

Sol:

If the zeroes of the cubic polynomial are a, b and c then the cubic polynomial can be found as  $x^3 - (a+b+c)x^2 + (ab+bc+ca)x - abc$  .....(1) Let a=2, b=-3 and c=4

Substituting the values in 1, we get

$$x^3 - (2 - 3 + 4)x^2 + (-6 - 12 + 8)x - (-24)$$
  
 $\Rightarrow x^3 - 3x^2 - 10x + 24$ 

4.

Sol:

If the zeroes of the cubic polynomial are a, b and c then the cubic polynomial can be found as  $x^3 - (a + b + c)x^2 + (ab + bc + ca)x - abc$  .....(1)

Let 
$$a = \frac{1}{2}$$
,  $b = 1$  and  $c = -3$ 

Substituting the values in (1), we get

$$x^{3} - \left(\frac{1}{2} + 1 - 3\right)x^{2} + \left(\frac{1}{2} - 3 - \frac{3}{2}\right)x - \left(\frac{-3}{2}\right)$$

$$\Rightarrow x^{3} - \left(\frac{-3}{2}\right)x^{2} - 4x + \frac{3}{2}$$

$$\Rightarrow 2x^{3} + 3x^{2} - 8x + 3$$

5.

Sol:

We know the sum, sum of the product of the zeroes taken two at a time and the product of the zeroes of a cubic polynomial then the cubic polynomial can be found as  $x^3 - (\text{sum of the zeroes})x^2 + (\text{sum of the product of the zeroes taking two at a time})x - product of zeroes$ 

Therefore, the required polynomial is

$$x^3 - 5x^2 - 2x + 24$$

6.

Sol:  

$$x-3$$

$$\begin{array}{c}
x-3 \\
x^3 - 3x^2 + 5x - 3 \\
- 2x \\
- + \\
- 3x^2 + 7x - 3 \\
- 3x^2 + 6 \\
+ - \\
\hline
7x - 9
\end{array}$$

Quotient q(x) = x - 3Remainder r(x) = 7x - 9

7. Sol: 
$$x^{2} + x - 3$$

$$x^{4} + 0x^{3} - 3x^{2} + 4x + 5$$

$$x^{4} - x^{3} + x^{2}$$

$$- + -$$

$$x^{3} - 4x^{2} + 4x + 5$$

$$x^{3} - x^{2} + x$$

$$- + -$$

$$- 3x^{2} + 3x + 5$$

$$- 3x^{2} + 3x - 3$$

$$+ - +$$

$$8$$

Quotient 
$$q(x) = x^2 + x - 3$$
  
Remainder  $r(x) = 8$ 

8.

We can write

$$f(x) \text{ as } x^4 + 0x^3 + 0x^2 - 5x + 6 \text{ and } g(x) \text{ as } -x^2 + 2$$

$$-x^2 + 2 \int_{x^4 + 0x^3 + 0x^2 - 5x + 6}^{-x^2 - 2} \frac{1}{x^4 + 0x^3 + 0x^2 - 5x + 6}$$

$$-2x^2 - 5x + 6$$

$$2x^2 - 4$$

$$- +$$

$$-5x + 10$$

Quotient 
$$q(x) = -x^2 - 2$$
  
Remainder  $r(x) = -5x + 10$ 

9.

Since, the remainder is 0.

Hence,  $x^2 - 3$  is a factor of  $2x^4 + 3x^3 - 2x^2 - 9x - 12$ 

10.

### Sol:

By using division rule, we have

 $Dividend = Quotient \times Divisor + Remainder$ 

$$\therefore 3x^3 + x^2 + 2x + 5 = (3x - 5)g(x) + 9x + 10$$
  
$$\Rightarrow 3x^3 + x^2 + 2x + 5 - 9x - 10 = (3x - 5)g(x)$$

$$\Rightarrow 3x^3 + x^2 - 7x - 5 = (3x - 5)g(x)$$

$$\Rightarrow g(x) = \frac{3x^3 + x^2 - 7x - 5}{3x^3 + x^2}$$

$$\Rightarrow 3x^{3} + x^{2} - 7x - 5 = (3x - 5)g(x)$$

$$\Rightarrow g(x) = \frac{3x^{3} + x^{2} - 7x - 5}{3x - 5}$$

$$3x - 5$$

$$3x^{3} + x^{2} - 7x - 5$$

$$3x^{3} - 5x^{2}$$

$$- +$$

$$6x^{2} - 7x - 5$$

$$6x^{2} - 10x$$

$$- +$$

$$3x - 5$$

$$3x - 5$$

$$- +$$

$$X$$

$$\therefore g(x) = x^2 + 2x + 1$$

11.

Sol:

We can write 
$$f(x)$$
 as  $-6x^3 + x^2 + 20x + 8$  and  $g(x)$  as  $-3x^2 + 5x + 2$ 

$$\begin{array}{c}
x^{2} + 2x + 1 \\
-3x^{2} + 5x + 2
\end{array}$$

$$\begin{array}{c}
x^{2} + 2x + 1 \\
-6x^{3} + x^{2} + 20x + 8 \\
-6x^{3} + 10x^{2} + 4x
\end{array}$$

$$\begin{array}{c}
+ - - \\
-9x^{2} + 16x + 8 \\
-9x^{2} + 15x + 6 \\
+ - - \\
x + 2
\end{array}$$

Quotient = 2x + 3

Remainder = x + 2

By using division rule, we have

 $Dividend = Quotient \times Divisor + Remainder$ 

$$\therefore -6x^3 + x^2 + 20x + 8 = (-3x^2 + 5x + 2)(2x + 3) + x + 2$$

$$\Rightarrow -6x^3 + x^2 + 20x + 8 = -6x^3 + 10x^2 + 4x - 9x^2 + 15x + 6 + x + 2$$

$$\Rightarrow -6x^3 + x^2 + 20x + 8 = -6x^3 + x^2 + 20x + 8$$

**12.** 

Sol:

Let 
$$f(x) = x^3 + 2x^2 - 11x - 12$$

Since -1 is a zero of f(x), (x+1) is a factor of f(x).

On dividing f(x) by (x+1), we get

$$f(x) = x^{3} + 2x^{2} - 11x - 12$$

$$= (x + 1) (x^{2} + x - 12)$$

$$= (x + 1) \{x^{2} + 4x - 3x - 12\}$$

$$= (x + 1) \{x (x+4) - 3 (x+4)\}$$

$$= (x + 1) (x - 3) (x + 4)$$

$$\therefore f(x) = 0 \Rightarrow (x + 1) (x - 3) (x + 4) = 0$$

$$\Rightarrow (x + 1) = 0 \text{ or } (x - 3) = 0 \text{ or } (x + 4) = 0$$

$$\Rightarrow x = -1 \text{ or } x = 3 \text{ or } x = -4$$

Thus, all the zeroes are -1, 3 and -4.

### **13.**

### Sol:

Let  $f(x) = x^3 - 4x^2 - 7x + 10$ 

Since 1 and -2 are the zeroes of f(x), it follows that each one of (x-1) and (x+2) is a factor of f(x).

Consequently,  $(x-1)(x+2) = (x^2 + x - 2)$  is a factor of f(x).

On dividing f(x) by  $(x^2 + x - 2)$ , we get:

$$x^{2} + x - 2$$

$$x^{3} - 4x^{2} - 7x + 10$$

$$x^{3} + x^{2} - 2x$$

$$- - +$$

$$-5x^{2} - 5x + 10$$

$$-5x^{2} - 5x + 10$$

$$+ + -$$

$$X$$

$$f(x) = 0 \Rightarrow (x^{2} + x - 2)(x - 5) = 0$$

$$\exists (x) = 0 \Rightarrow (x + x - 2)(x - 3) = 0$$

$$\Rightarrow (x - 1)(x + 2)(x - 5) = 0$$

$$\Rightarrow x = 1 \text{ or } x = -2 \text{ or } x = 5$$

Hence, the third zero is 5.

### **14.**

#### Sol:

Let 
$$x^4 + x^3 - 11x^2 - 9x + 18$$

Since 3 and -3 are the zeroes of f(x), it follows that each one of (x + 3) and (x - 3) is a factor of f(x).

Consequently,  $(x-3)(x+3) = (x^2-9)$  is a factor of f(x).

On dividing f(x) by  $(x^2 - 9)$ , we get:

$$f(x) = 0 \Rightarrow (x^2 + x - 2) (x^2 - 9) = 0$$

$$\Rightarrow (x^2 + 2x - x - 2) (x - 3) (x + 3)$$

$$\Rightarrow (x - 1) (x + 2) (x - 3) (x + 3) = 0$$

$$\Rightarrow x = 1 \text{ or } x = -2 \text{ or } x = 3 \text{ or } x = -3$$

Hence, all the zeroes are 1, -2, 3 and -3.

15.

### Sol:

Let  $f(x) = x^4 + x^3 - 34x^2 - 4x + 120$ 

Since 2 and -2 are the zeroes of f(x), it follows that each one of (x - 2) and (x + 2) is a factor of f(x).

Consequently,  $(x-2)(x+2) = (x^2-4)$  is a factor of f(x).

On dividing f(x) by  $(x^2 - 4)$ , we get:

$$\begin{array}{c}
x^{2}-4 \\
x^{4} \\
x^{4} \\
-4x^{2}
\end{array}$$

$$\begin{array}{c}
- \\
x^{3} \\
-4x
\end{array}$$

$$\begin{array}{c}
- \\
-30x^{2} + 120 \\
-30x^{2} + 120 \\
-30x^{2} + 120
\end{array}$$

$$\begin{array}{c}
+ \\
- \\
x
\end{array}$$

$$f(x) = 0$$
  
 $\Rightarrow (x^2 + x - 30)(x^2 - 4) = 0$ 

$$\Rightarrow$$
 (x<sup>2</sup> + 6x - 5x - 30) (x - 2) (x + 2)

$$\Rightarrow$$
 [x(x+6) – 5(x+6)] (x – 2) (x + 2)

$$\Rightarrow$$
  $(x-5)(x+6)(x-2)(x+2)=0$ 

$$\Rightarrow$$
 x = 5 or x = -6 or x = 2 or x = -2

Hence, all the zeroes are 2, -2, 5 and -6.

**16.** 

### Sol:

Let 
$$f(x) = x^4 + x^3 - 23x^2 - 3x + 60$$

Since  $\sqrt{3}$  and  $-\sqrt{3}$  are the zeroes of f(x), it follows that each one of  $(x - \sqrt{3})$  and  $(x + \sqrt{3})$  is a factor of f(x).

Consequently,  $(x - \sqrt{3})(x + \sqrt{3}) = (x^2 - 3)$  is a factor of f(x).

On dividing f(x) by  $(x^2 - 3)$ , we get:

$$f(x) = 0$$

$$\Rightarrow$$
 (x<sup>2</sup> + x - 20) (x<sup>2</sup> - 3) = 0

$$\Rightarrow$$
 (x<sup>2</sup> + 5x - 4x - 20) (x<sup>2</sup> - 3)

$$\Rightarrow [x(x+5)-4(x+5)](x^2-3)$$

$$\Rightarrow$$
  $(x-4)(x+5)(x-\sqrt{3})(x+\sqrt{3})=0$ 

$$\Rightarrow$$
 x = 4 or x = -5 or x =  $\sqrt{3}$  or x =  $-\sqrt{3}$ 

Hence, all the zeroes are  $\sqrt{3}$ ,  $-\sqrt{3}$ , 4 and -5.

**17.** 

### Sol:

The given polynomial is  $f(x) = 2x^4 - 3x^3 - 5x^2 + 9x - 3$ 

Since  $\sqrt{3}$  and  $-\sqrt{3}$  are the zeroes of f(x), it follows that each one of  $(x - \sqrt{3})$  and  $(x + \sqrt{3})$  is a factor of f(x).

Consequently,  $(x - \sqrt{3})(x + \sqrt{3}) = (x^2 - 3)$  is a factor of f(x).

On dividing f(x) by  $(x^2 - 3)$ , we get:

$$x^{2} - 3 ) 2x^{4} - 3x^{3} - 5x^{2} + 9x - 3$$

$$2x^{4} - 6x^{2}$$

$$- +$$

$$-3x^{3} + x^{2} + 9x - 3$$

$$-3x^{3} + 9x$$

$$+ -$$

$$x^{2} - 3$$

$$x^{2} - 3$$

$$- +$$

$$x$$

$$f(x) = 0$$

$$\Rightarrow 2x^4 - 3x^3 - 5x^2 + 9x - 3 = 0$$

$$\Rightarrow (x^2 - 3)(2x^2 - 3x + 1) = 0$$

$$\Rightarrow (x^2 - 3)(2x^2 - 2x - x + 1) = 0$$

$$\Rightarrow (x - \sqrt{3})(x + \sqrt{3})(2x - 1)(x - 1) = 0$$

$$\Rightarrow x = \sqrt{3} \text{ or } x = -\sqrt{3} \text{ or } x = \frac{1}{2} \text{ or } x = 1$$

Hence, all the zeroes are  $\sqrt{3}$ ,  $-\sqrt{3}$ ,  $\frac{1}{2}$  and 1.

**18.** 

### Sol:

The given polynomial is  $f(x) = x^4 + 4x^3 - 2x^2 - 20x - 15$ .

Since  $(x - \sqrt{5})$  and  $(x + \sqrt{5})$  are the zeroes of f(x) it follows that each one of  $(x - \sqrt{5})$  and  $(x + \sqrt{5})$  is a factor of f(x).

Consequently,  $(x - \sqrt{5})(x + \sqrt{5}) = (x^2 - 5)$  is a factor of f(x).

On dividing f(x) by  $(x^2 - 5)$ , we get:

$$x^{2} - 5 ) x^{4} + 4x^{3} - 2x^{2} - 20x - 15 (2x^{2} - 3x + 1)$$

$$x^{4} - 5x^{2}$$

$$- +$$

$$4x^{3} + 3x^{2} - 20x - 15$$

$$4x^{3} - 20x$$

$$- +$$

$$3x^{2} - 15$$

$$3x^{2} - 15$$

$$- +$$

$$x$$

$$f(x) = 0$$

$$\Rightarrow x^4 + 4x^3 - 7x^2 - 20x - 15 = 0$$

$$\Rightarrow (x^2 - 5)(x^2 + 4x + 3) = 0$$

$$\Rightarrow (x - \sqrt{5})(x + \sqrt{5})(x + 1)(x + 3) = 0$$

$$\Rightarrow x = \sqrt{5} \text{ or } x = -\sqrt{5} \text{ or } x = -1 \text{ or } x = -3$$

Hence, all the zeroes are  $\sqrt{5}$ ,  $-\sqrt{5}$ , -1 and -3.

19.

### Sol:

The given polynomial is  $f(x) = 2x^4 - 11x^3 + 7x^2 + 13x - 7$ .

Since  $(3 + \sqrt{2})$  and  $(3 - \sqrt{2})$  are the zeroes of f(x) it follows that each one of  $(x + 3 + \sqrt{2})$  and  $(x + 3 - \sqrt{2})$  is a factor of f(x).

Consequently, 
$$[(x - (3 + \sqrt{2})] [(x - (3 - \sqrt{2})] = [(x - 3) - \sqrt{2}] [(x - 3) + \sqrt{2}]$$
  
=  $[(x - 3)^2 - 2] = x^2 - 6x + 7$ , which is a factor of  $f(x)$ .

On dividing f(x) by  $(x^2 - 6x + 7)$ , we get:

$$x^{2}-6x+7 ) 2x^{4}-11x^{3}+7x^{2}+13x-7 (2x^{2}+x-1)$$

$$- + -$$

$$x^{3}-7x^{2}+13x-7$$

$$x^{3}-6x^{2}+7x$$

$$- + -$$

$$-x^{2}+6x-7$$

$$-x^{2}+6x-7$$

$$f(x) = 0$$

$$\Rightarrow 2x^4 - 11x^3 + 7x^2 + 13x - 7 = 0$$

$$\Rightarrow (x^2 - 6x + 7)(2x^2 + x - 7) = 0$$

$$\Rightarrow (x + 3 + \sqrt{2})(x + 3 - \sqrt{2})(2x - 1)(x + 1) = 0$$

$$\Rightarrow x = -3 - \sqrt{2} \text{ or } x = -3 + \sqrt{2} \text{ or } x = \frac{1}{2} \text{ or } x = -1$$

Hence, all the zeroes are  $(-3 - \sqrt{2})$ ,  $(-3 + \sqrt{2})$ ,  $\frac{1}{2}$  and -1.

### Exercise – 2C

1.

### Sol:

Let the other zeroes of  $x^2 - 4x + 1$  be a.

By using the relationship between the zeroes of the quadratic polynomial.

We have, sum of zeroes = 
$$\frac{-(coefficient \ of \ x)}{coefficient \ of \ x^2}$$
  
 $\therefore 2 + \sqrt{3} + a = \frac{-(-4)}{1}$ 

$$\Rightarrow$$
 a = 2 -  $\sqrt{3}$ 

Hence, the other zeroes of  $x^2 - 4x + 1$  is  $2 - \sqrt{3}$ .

2.

### Sol:

$$f(x) = x^2 + x - p(p + 1)$$

By adding and subtracting px, we get

$$f(x) = x^2 + px + x - px - p(p + 1)$$

$$= x^2 + (p+1) x - px - p (p+1)$$

$$= x[x + (p + 1)] - p[x + (p + 1)]$$

$$= [x + (p + 1)] (x - p)$$

$$f(x) = 0$$

$$\Rightarrow [x + (p+1)](x-p) = 0$$

$$\Rightarrow$$
 [x + (p + 1)] = 0 or (x - p) = 0

$$\Rightarrow$$
 x = - (p + 1) or x = p

So, the zeroes of f(x) are -(p+1) and p.

3.

### Sol:

$$f(x) = x^2 - 3x - m (m + 3)$$

By adding and subtracting mx, we get

$$f(x) = x^2 - mx - 3x + mx - m (m + 3)$$

$$= x[x - (m + 3)] + m[x - (m + 3)]$$

$$= [x - (m + 3)] (x + m)$$

$$f(x) = 0 \Rightarrow [x - (m + 3)](x + m) = 0$$

$$\Rightarrow$$
 [x - (m + 3)] = 0 or (x + m) = 0

$$\Rightarrow$$
 x = m + 3 or x = -m

So, the zeroes of f(x) are -m and +3.

4.

### Sol:

If the zeroes of the quadratic polynomial are  $\alpha$  and  $\beta$  then the quadratic polynomial can be

found as 
$$x^2 - (\alpha + \beta)x + \alpha\beta$$
 ....(1)

Substituting the values in (1), we get

$$x^2 - 6x + 4$$

5.

#### Sol:

Given: x = 2 is one zero of the quadratic polynomial  $kx^2 + 3x + k$ 

Therefore, it will satisfy the above polynomial.

Now, we have

$$k(2)^2 + 3(2) + k = 0$$

$$\Rightarrow 4k + 6 + k = 0$$

$$\Rightarrow$$
 5k + 6 = 0

$$\Rightarrow k = -\frac{6}{5}$$

6.

### Sol:

Given: x = 3 is one zero of the polynomial  $2x^2 + x + k$ 

Therefore, it will satisfy the above polynomial.

Now, we have

$$2(3)^2 + 3 + k = 0$$

$$\Rightarrow 21 + k = 0$$

$$\Rightarrow$$
 k =  $-21$ 

7.

### Sol:

Given: x = -4 is one zero of the polynomial  $x^2 - x - (2k + 2)$ 

Therefore, it will satisfy the above polynomial.

Now, we have

$$(-4)^2 - (-4) - (2k + 2) = 0$$

$$\Rightarrow 16 + 4 - 2k - 2 = 0$$

$$\Rightarrow$$
 2k =  $-18$ 

$$\Rightarrow$$
 k = 9

8.

### Sol:

Given: x = 1 is one zero of the polynomial  $ax^2 - 3(a - 1) x - 1$ Therefore, it will satisfy the above polynomial.

Now, we have

$$a(1)^2 - (a-1)1 - 1 = 0$$

$$\Rightarrow$$
 a - 3a + 3 - 1 = 0

$$\Rightarrow$$
  $-2a = -2$ 

$$\Rightarrow$$
 a = 1

9.

### Sol:

Given: x = -2 is one zero of the polynomial  $3x^2 + 4x + 2k$ 

Therefore, it will satisfy the above polynomial.

Now, we have

$$3(-2)^2 + 4(-2)1 + 2k = 0$$

$$\Rightarrow 12 - 8 + 2k = 0$$

$$\Rightarrow$$
 k =  $-2$ 

**10.** 

#### Sol:

$$f(x) = x^2 - x - 6$$
$$= x^2 - 3x + 2x - 6$$

$$= x(x-3) + 2(x-3)$$

$$=(x-3)(x+2)$$

$$f(x) = 0 \Rightarrow (x - 3)(x + 2) = 0$$

$$\Rightarrow$$
 (x - 3) = 0 or (x + 2) = 0

$$\Rightarrow$$
 x = 3 or x = -2

So, the zeroes of f(x) are 3 and -2.

### 11.

### Sol:

By using the relationship between the zeroes of the quadratic polynomial.

We have

Sum of zeroes = 
$$\frac{-(coefficient \ of \ x)}{coefficient \ of \ x^2}$$

$$\Rightarrow 1 = \frac{-(-3)}{k}$$

$$\Rightarrow$$
 k = 3

## 12.

## Sol:

By using the relationship between the zeroes of he quadratic polynomial.

We have

Product of zeroes = 
$$\frac{constant\ term}{coefficient\ of\ x^2}$$

$$\Rightarrow 3 = \frac{k}{1}$$

$$\Rightarrow$$
 k = 3

### 13.

### Sol:

Given: (x + a) is a factor of  $2x^2 + 2ax + 5x + 10$ 

We have

$$x + a = 0$$

$$\Rightarrow x = -a$$

Since, (x + a) is a factor of  $2x^2 + 2ax + 5x + 10$ 

Hence, It will satisfy the above polynomial

$$\therefore 2(-a)^2 + 2a(-a) + 5(-a) + 10 = 0$$

$$\Rightarrow$$
  $-5a + 10 = 0$ 

$$\Rightarrow$$
 a = 2

### 14.

### Sol:

By using the relationship between the zeroes of the quadratic polynomial.

We have

Sum of zeroes = 
$$\frac{-(coefficient \ of \ x^2)}{coefficient \ of \ x^3}$$
  
 $\Rightarrow a - b + a + a + b = \frac{-(-6)}{2}$   
 $\Rightarrow 3a = 3$   
 $\Rightarrow a = 1$ 

### **15.**

### Sol:

Equating  $x^2 - x$  to 0 to find the zeroes, we will get x(x-1) = 0  $\Rightarrow x = 0$  or x - 1 = 0  $\Rightarrow x = 0$  or x = 1Since,  $x^3 + x^2 - ax + b$  is divisible by  $x^2 - x$ . Hence, the zeroes of  $x^2 - x$  will satisfy  $x^3 + x^2 - ax + b$   $\therefore (0)^3 + 0^2 - a(0) + b = 0$   $\Rightarrow b = 0$ And  $(1)^3 + 1^2 - a(1) + 0 = 0$  [: b = 0]  $\Rightarrow a = 2$ 

### 16.

#### Sol:

By using the relationship between the zeroes of he quadratic polynomial.

We have

Sum of zeroes = 
$$\frac{-(coefficient\ of\ x)}{coefficient\ of\ x^2}$$
 and Product of zeroes =  $\frac{constant\ term}{coefficient\ of\ x^2}$   
 $\therefore \alpha + \beta = \frac{-7}{2}$  and  $\alpha\beta = \frac{5}{2}$   
Now,  $\alpha + \beta + \alpha\beta = \frac{-7}{2} + \frac{5}{2} = -1$ 

### **17.**

#### Sol:

"If f(x) and g(x) are two polynomials such that degree of f(x) is greater than degree of g(x) where  $g(x) \neq 0$ , there exists unique polynomials q(x) and r(x) such that

$$f(x) = g(x) \times q(x) + r(x),$$

where r(x) = 0 or degree of r(x) < degree of <math>g(x).

18.

Sol:

We can find the quadratic polynomial if we know the sum of the roots and product of the roots by using the formula

 $x^2$  – (sum of the zeroes)x + product of zeroes

$$\Rightarrow x^2 - \left(-\frac{1}{2}\right)x + (-3)$$

$$\Rightarrow x^2 + \frac{1}{2}x - 3$$

Hence, the required polynomial is  $x^2 + \frac{1}{2}x - 3$ .

19.

Sol:

To find the zeroes of the quadratic polynomial we will equate f(x) to 0

$$\therefore f(x) = 0$$

$$\Rightarrow 6x^2 - 3 = 0$$

$$\Rightarrow$$
 3(2x<sup>2</sup> – 1) = 0

$$\Rightarrow 2x^2 - 1 = 0$$

$$\Rightarrow 2x^2 = 1$$

$$\Rightarrow x^2 = \frac{1}{2}$$

$$\Rightarrow x = \pm \frac{1}{\sqrt{2}}$$

Hence, the zeroes of the quadratic polynomial  $f(x) = 6x^2 - 3$  are  $\frac{1}{\sqrt{2}}$ ,  $-\frac{1}{\sqrt{2}}$ .

20.

Sol:

To find the zeroes of the quadratic polynomial we will equate f(x) to 0

$$\therefore f(x) = 0$$

$$\Rightarrow 4\sqrt{3}x^2 + 5x - 2\sqrt{3} = 0$$

$$\Rightarrow 4\sqrt{3}x^2 + 8x - 3x - 2\sqrt{3} = 0$$

$$\Rightarrow 4x (\sqrt{3}x + 2) - \sqrt{3}(\sqrt{3}x + 2) = 0$$

$$\Rightarrow (\sqrt{3}x + 2) = 0 \text{ or } (4x - \sqrt{3}) = 0$$

$$\Rightarrow$$
 x =  $-\frac{2}{\sqrt{3}}$  or x =  $\frac{\sqrt{3}}{4}$ 

Hence, the zeroes of the quadratic polynomial  $f(x) = 4\sqrt{3}x^2 + 5x - 2\sqrt{3}$  are  $-\frac{2}{\sqrt{3}}$  or  $\frac{\sqrt{3}}{4}$ 

21.

Sol:

By using the relationship between the zeroes of the quadratic polynomial.

We have

Sum of zeroes = 
$$\frac{-(coefficient\ of\ x)}{coefficient\ of\ x^2}$$
 and Product of zeroes =  $\frac{constant\ term}{coefficient\ of\ x^2}$   
 $\therefore \alpha + \beta = \frac{-(-5)}{1}$  and  $\alpha\beta = \frac{k}{1}$   
 $\Rightarrow \alpha + \beta = 5$  and  $\alpha\beta = \frac{k}{1}$ 

Solving 
$$\alpha - \beta = 1$$
 and  $\alpha + \beta = 5$ , we will get

$$\alpha = 3$$
 and  $\beta = 2$ 

Substituting these values in  $\alpha\beta = \frac{k}{1}$ , we will get

$$k = 6$$

22.

Sol:

By using the relationship between the zeroes of the quadratic polynomial.

We have

Sum of zeroes = 
$$\frac{-(coefficient of x)}{coefficient of x^2}$$
 and Product of zeroes =  $\frac{constant term}{coefficient of x^2}$   
 $\therefore \alpha + \beta = \frac{-1}{6}$  and  $\alpha\beta = -\frac{1}{3}$   
Now,  $\frac{\alpha}{\beta} + \frac{\beta}{\alpha} = \frac{\alpha^2 + \beta^2}{\alpha\beta}$   
 $= \frac{\alpha^2 + \beta^2 + 2\alpha\beta - 2\alpha\beta}{\alpha\beta}$   
 $= \frac{(\alpha + \beta)^2 - 2\alpha\beta}{\alpha\beta}$ 

$$\alpha\beta = \frac{\left(\frac{-1}{6}\right)^2 - 2\left(-\frac{1}{3}\right)}{-\frac{1}{3}} = \frac{\frac{1}{36} + \frac{2}{3}}{-\frac{1}{3}}$$
25

23.

Sol

By using the relationship between the zeroes of he quadratic polynomial. We have

Sum of zeroes = 
$$\frac{-(coefficient\ of\ x)}{coefficient\ of\ x^2}$$
 and Product of zeroes =  $\frac{constant\ term}{coefficient\ of\ x^2}$   
 $\therefore \alpha + \beta = \frac{-(-7)}{5}$  and  $\alpha\beta = \frac{1}{5}$   
 $\Rightarrow \alpha + \beta = \frac{7}{5}$  and  $\alpha\beta = \frac{1}{5}$   
Now,  $\frac{1}{\alpha} + \frac{1}{\beta} = \frac{\alpha + \beta}{\alpha\beta}$   
 $= \frac{\frac{7}{5}}{\frac{1}{5}}$   
 $= 7$ 

### 24.

### Sol:

By using the relationship between the zeroes of the quadratic polynomial. We have

Sum of zeroes 
$$=$$
  $\frac{-(coefficient of x)}{coefficient of x^2}$  and Product of zeroes  $=$   $\frac{constant term}{coefficient of x^2}$   
 $\therefore \alpha + \beta = \frac{-1}{1}$  and  $\alpha\beta = \frac{-2}{1}$   
 $\Rightarrow \alpha + \beta = -1$  and  $\alpha\beta = -2$   
Now,  $\left(\frac{1}{\alpha} - \frac{1}{\beta}\right)^2 = \left(\frac{\beta - \alpha}{\alpha\beta}\right)^2$   
 $= \frac{(\alpha + \beta)^2 - 4\alpha\beta}{(\alpha\beta)^2}$  [ $\because (\beta - \alpha)^2 = (\alpha + \beta)^2 - 4\alpha\beta$ ]  
 $= \frac{(-1)^2 - 4(-2)}{(-2)^2}$  [ $\because \alpha + \beta = -1$  and  $\alpha\beta = -2$ ]  
 $= \frac{(-1)^2 - 4(-2)}{4}$   
 $= \frac{9}{4}$   
 $\because \left(\frac{1}{\alpha} - \frac{1}{\beta}\right)^2 = \frac{9}{4}$   
 $\Rightarrow \frac{1}{\alpha} - \frac{1}{\beta} = \pm \frac{3}{2}$ 

### 25.

### Sol:

By using the relationship between the zeroes of he quadratic polynomial.

We have, Sum of zeroes = 
$$\frac{-(coefficient of x^2)}{coefficient of x^3}$$
$$\therefore a - b + a + a + b = \frac{-(-3)}{1}$$
$$\Rightarrow 3a = 3$$

$$\Rightarrow$$
 a = 1

Now, Product of zeroes =  $\frac{-(constant\ term)}{coefficient\ of\ x^3}$ 

$$(a-b)(a)(a+b) = \frac{-1}{1}$$

$$\Rightarrow$$
 (1 - b) (1) (1 + b) = -1 [:a = 1]

$$\Rightarrow 1 - b^2 = -1$$

$$\Rightarrow$$
 b<sup>2</sup> = 2

$$\Rightarrow$$
 b =  $\pm\sqrt{2}$ 

## Exercise - MCQ

1.

### Sol:

(d) none of these

A polynomial in x of degree n is an expression of the form  $p(x) = a_0 + a_1x + a_2x^2 + \dots + a_nx^n$ , where  $a_n \neq 0$ .

2.

### Sol:

(d)  $x + \frac{3}{x}$  is not a polynomial.

It is because in the second term, the degree of x is -1 and an expression with a negative degree is not a polynomial.

3.

### Sol:

(c) 3, -1  
Let 
$$f(x) = x^2 - 2x - 3 = 0$$
  
 $= x^2 - 3x + x - 3 = 0$   
 $= x(x - 3) + 1(x - 3) = 0$   
 $= (x - 3)(x + 1) = 0$   
 $\Rightarrow x = 3 \text{ or } x = -1$ 

4.

(b) 
$$3\sqrt{2}$$
,  $-2\sqrt{2}$   
Let  $f(x) = x^2 - \sqrt{2}x - 12 = 0$   
 $\Rightarrow x^2 - 3\sqrt{2}x + 2\sqrt{2}x - 12 = 0$   
 $\Rightarrow x(x - 3\sqrt{2}) + 2\sqrt{2}(x - 3\sqrt{2}) = 0$   
 $\Rightarrow (x - 3\sqrt{2})(x + 2\sqrt{2}) = 0$   
 $\Rightarrow x = 3\sqrt{2} \text{ or } x = -2\sqrt{2}$ 

5.

### Sol:

(c) 
$$-\frac{3}{\sqrt{2}}, \frac{\sqrt{2}}{4}$$
  
Let  $f(x) = 4x^2 + 5\sqrt{2}x - 3 = 0$   
 $\Rightarrow 4x^2 + 6\sqrt{2}x - \sqrt{2}x - 3 = 0$   
 $\Rightarrow 2\sqrt{2}x(\sqrt{2}x + 3) - 1(\sqrt{2}x + 3) = 0$   
 $\Rightarrow (\sqrt{2}x + 3)(2\sqrt{2}x - 1) = 0$   
 $\Rightarrow x = -\frac{3}{\sqrt{2}} \text{ or } x = \frac{1}{2\sqrt{2}}$   
 $\Rightarrow x = -\frac{3}{\sqrt{2}} \text{ or } x = \frac{1}{2\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{2}}{4}$ 

**6.** 

### Sol:

(b) 
$$\frac{-3}{2}$$
,  $\frac{4}{3}$   
Let  $f(x) = x^2 + \frac{1}{6}x - 2 = 0$   
 $\Rightarrow 6x^2 + x - 12 = 0$   
 $\Rightarrow 6x^2 + 9x - 8x - 12 = 0$   
 $\Rightarrow 3x (2x + 3) - 4 (2x + 3) = 0$   
 $\Rightarrow (2x + 3) (3x - 4) = 0$   
 $\therefore x = \frac{-3}{2}$  or  $x = \frac{4}{3}$ 

**7.** 

Sol:

(a) 
$$\frac{2}{3}$$
,  $\frac{-1}{7}$   
Let  $f(x) = 7x^2 - \frac{11}{3}x - \frac{2}{3} = 0$   
 $\Rightarrow 21x^2 - 11x - 2 = 0$   
 $\Rightarrow 21x^2 - 14x + 3x - 2 = 0$   
 $\Rightarrow 7x (3x - 2) + 1(3x - 2) = 0$   
 $\Rightarrow (3x - 2) (7x + 1) = 0$ 

8.

Sol:

(c) 
$$x^2 - 3x - 10$$

 $\Rightarrow$  x =  $\frac{2}{3}$  or x =  $\frac{-1}{7}$ 

Given: Sum of zeroes,  $\alpha + \beta = 3$ Also, product of zeroes,  $\alpha\beta = -10$ 

$$\therefore$$
 Required polynomial =  $x^2 - (\alpha + \beta) + \alpha\beta = x^2 - 3x - 10$ 

9.

Sol:

(c) 
$$x^2 - 2x - 15$$

Here, the zeroes are 5 and -3.

Let 
$$\alpha = 5$$
 and  $\beta = -3$ 

So, sum of the zeroes, 
$$\alpha + \beta = 5 + (-3) = 2$$

Also, product of the zeroes,  $\alpha\beta = 5 \times (-3) = -15$ 

The polynomial will be  $x^2 - (\alpha + \beta) x + \alpha \beta$ 

 $\therefore$  The required polynomial is  $x^2 - 2x - 15$ .

10.

Sol:

(d) 
$$x^2 - \frac{1}{10}x - \frac{3}{10}$$

Here, the zeroes are  $\frac{3}{5}$  and  $\frac{-1}{2}$ 

Let 
$$\alpha = \frac{3}{5}$$
 and  $\beta = \frac{-1}{2}$ 

So, sum of the zeroes,  $\alpha + \beta = \frac{3}{5} + \left(\frac{-1}{2}\right) = \frac{1}{10}$ 

Also, product of the zeroes,  $\alpha\beta = \frac{3}{5} \times \left(\frac{-1}{2}\right) = \frac{-3}{10}$ 

The polynomial will be  $x^2 - (\alpha + \beta) x + \alpha \beta$ .

 $\therefore$  The required polynomial is  $x^2 - \frac{1}{10}x - \frac{3}{10}$ .

### 11.

### Sol:

(b) both negative

Let  $\alpha$  and  $\beta$  be the zeroes of  $x^2 + 88x + 125$ .

Then  $\alpha + \beta = -88$  and  $\alpha \times \beta = 125$ 

This can only happen when both the zeroes are negative.

### 12.

### Sol:

$$(b) -5$$

Given:  $\alpha$  and  $\beta$  be the zeroes of  $x^2 + 5x + 8$ .

If  $\alpha + \beta$  is the sum of the roots and  $\alpha\beta$  is the product, then the required polynomial will be  $x^2 - (\alpha + \beta) x + \alpha\beta$ .

### 13.

#### Sol:

(c) 
$$\frac{-9}{2}$$

Given:  $\alpha$  and  $\beta$  be the zeroes of  $2x^2 + 5x - 9$ .

If  $\alpha + \beta$  are the zeroes, then  $x^2 - (\alpha + \beta) x + \alpha \beta$  is the required polynomial.

The polynomial will be  $x^2 - \frac{5}{2}x - \frac{9}{2}$ .

$$\therefore \alpha\beta = \frac{-9}{2}$$

14.

### Sol:

$$(d) \frac{-6}{5}$$

Since 2 is a zero of  $kx^2 + 3x + k$ , we have:

$$k \times (2)^2 + 3(2) + k = 0$$

$$\Rightarrow$$
 4k + k + 6 = 0

$$\Rightarrow$$
 5k = -6

$$\Rightarrow k = \frac{-6}{5}$$

15.

## Sol:

(b) 
$$\frac{5}{4}$$

Since -4 is a zero of  $(k-1) x^2 + kx + 1$ , we have:

$$(k-1) \times (-4)^2 + k \times (-4) + 1 = 0$$

$$\Rightarrow 16k - 16 - 4k + 1 = 0$$

$$\Rightarrow 12k - 15 = 0$$

$$\Rightarrow k = \frac{15}{12}$$

$$\Rightarrow k = \frac{5}{4}$$

**16.** 

Sol:

(c) 
$$a = -2$$
,  $b = -6$ 

Given: -2 and 3 are the zeroes of  $x^2 + (a + 1)x + b$ .

Now, 
$$(-2)^2 + (a+1) \times (-2) + b = 0 \Rightarrow 4 - 2a - 2 + b = 0$$

$$\Rightarrow$$
 b - 2a = -2 ....(1)

Also, 
$$3^2 + (a + 1) \times 3 + b = 0 \Rightarrow 9 + 3a + 3 + b = 0$$

$$\Rightarrow$$
 b + 3a = -12 ....(2)

On subtracting (1) from (2), we get a = -2

$$b = -2 - 4 = -6$$
 [From (1)]

**17.** 

## Sol:

(a) 
$$k = 3$$

Let  $\alpha$  and  $\frac{1}{\alpha}$  be the zeroes of  $3x^2 - 8x + k$ .

Then the product of zeroes =  $\frac{k}{3}$ 

$$\Rightarrow \alpha \times \frac{1}{\alpha} = \frac{k}{3}$$

$$\Rightarrow 1 = \frac{k}{3}$$

$$\Rightarrow$$
k = 3

**18.** 

## Sol:

$$(d)^{\frac{-2}{3}}$$

Let  $\alpha$  and  $\beta$  be the zeroes of  $kx^2 + 2x + 3k$ .

Then  $\alpha + \beta = \frac{-2}{k}$  and  $\alpha\beta = 3$ 

$$\Rightarrow \alpha + \beta = \alpha \beta$$

$$\Rightarrow \frac{-2}{k} = 3$$

$$\Rightarrow k = \frac{-2}{3}$$

19.

### Sol:

$$(b) -3$$

Since  $\alpha$  and  $\beta$  be the zeroes of  $x^2 + 6x + 2$ , we have:

$$\alpha + \beta = -6$$
 and  $\alpha\beta = 2$ 

$$\therefore \left(\frac{1}{\alpha} + \frac{1}{\beta}\right) = \left(\frac{\alpha + \beta}{\alpha \beta}\right) = \frac{-6}{2} = -3$$

20.

Sol:

(a) -1

It is given that  $\alpha$ ,  $\beta$  and  $\gamma$  are the zeroes of  $x^3 - 6x^2 - x + 30$ .

$$\therefore (\alpha \beta + \beta \gamma + \gamma \alpha) = \frac{\text{co-efficient of } x}{\text{co-efficient of } x^3} = \frac{-1}{1} = -1$$

21.

Sol:

(a) -3

Since,  $\alpha$ ,  $\beta$  and  $\gamma$  are the zeroes of  $2x^3 + x^2 - 13x + 6$ , we have:

$$\alpha\beta\gamma = \frac{-(constant\ term)}{co-efficient\ of\ x^3} = \frac{-6}{2} = -3$$

22.

Sol:

(c) 
$$x^3 - 3x^2 - 10x + 24$$

Given:  $\alpha$ ,  $\beta$  and  $\gamma$  are the zeroes of polynomial p(x).

Also, 
$$(\alpha + \beta + \gamma) = 3$$
,  $(\alpha\beta + \beta\gamma + \gamma\alpha) = -10$  and  $\alpha\beta\gamma = -24$ 

$$\therefore p(x) = x^3 - (\alpha + \beta + \gamma) x^2 + (\alpha\beta + \beta\gamma + \gamma\alpha) x - \alpha\beta\gamma = x^3 - 3x^2 - 10x + 24$$

23.

Sol:

(a) 
$$\frac{-b}{a}$$

Let  $\alpha$ , 0 and 0 be the zeroes of  $ax^3 + bx^2 + cx + d = 0$ 

Then the sum of zeroes =  $\frac{-b}{a}$ 

$$\Rightarrow \alpha + 0 + 0 = \frac{-b}{a}$$

$$\Rightarrow \alpha = \frac{-b}{a}$$

Hence, the third zero is  $\frac{-b}{a}$ .

24.

Sol:

(b) 
$$\frac{c}{a}$$

Let  $\alpha$ ,  $\beta$  and 0 be the zeroes of  $ax^3 + bx^2 + cx + d$ .

Then, sum of the products of zeroes taking two at a time is given by

$$(\alpha\beta + \beta \times 0 + \alpha \times 0) = \frac{c}{a}$$

$$\Rightarrow \alpha \beta = \frac{c}{a}$$

 $\therefore$  The product of the other two zeroes is  $\frac{c}{a}$ .

25.

Sol:

(c) 
$$1 - a + b$$

Since -1 is a zero of  $x^3 + ax^2 + bx + c$ , we have:

$$(-1)^3 + a \times (-1)^2 + b \times (-1) + c = 0$$

$$\Rightarrow a - b + c + 1 = 0$$

$$\Rightarrow$$
 c = 1 - a + b

Also, product of all zeroes is given by

$$\alpha\beta \times (-1) = -c$$

$$\Rightarrow \alpha\beta = c$$

$$\Rightarrow \alpha \beta = 1 - a + b$$

26.

Sol:

(d) 2

Since  $\alpha$  and  $\beta$  are the zeroes of  $2x^2 + 5x + k$ , we have:

$$\alpha + \beta = \frac{-5}{2}$$
 and  $\alpha\beta = \frac{k}{2}$ 

Also, it is given that  $\alpha^2 + \beta^2 + \alpha\beta = \frac{21}{4}$ .

$$\Rightarrow (\alpha + \beta)^2 - \alpha\beta = \frac{21}{4}$$

$$\Rightarrow \left(\frac{-5}{2}\right)^2 - \frac{k}{2} = \frac{21}{4}$$

$$\Rightarrow \frac{25}{4} - \frac{k}{2} = \frac{21}{4}$$

$$\Rightarrow \frac{k}{2} = \frac{25}{4} - \frac{21}{4} = \frac{4}{4} = 1$$

$$\Rightarrow k = 2$$

27.

Sol:

(c) either 
$$r(x) = 0$$
 or  $deg r(x) < deg g(x)$ 

By division algorithm on polynomials, either r(x) = 0 or deg  $r(x) < \deg g(x)$ .

28.

Sol:

(d)  $5x^2$  is a monomial.

 $5x^2$  consists of one term only. So, it is a monomial.

## **Exercise – Formative Assesment**

1.

### Sol:

(c) 3, -1  
Here, 
$$p(x) = x^2 - 2x - 3$$
  
Let  $x^2 - 2x - 3 = 0$   
 $\Rightarrow x^2 - (3 - 1)x - 3 = 0$   
 $\Rightarrow x^2 - 3x + x - 3 = 0$   
 $\Rightarrow x(x - 3) + 1(x - 3) = 0$   
 $\Rightarrow (x - 3)(x + 1) = 0$   
 $\Rightarrow x = 3, -1$ 

2.

### Sol:

$$(a) -1$$

Here, 
$$p(x) = x^3 - 6x^2 - x + 3$$

Comparing the given polynomial with  $x^3 - (\alpha + \beta + \gamma) x^2 + (\alpha \beta + \beta \gamma + \gamma \alpha) x - \alpha \beta \gamma$ , we get:  $(\alpha \beta + \beta \gamma + \gamma \alpha) = -1$ 

**3.** 

### Sol:

(c) 
$$\frac{2}{3}$$

Here, 
$$p(x) = x^2 - 2x + 3k$$

Comparing the given polynomial with  $ax^2 + bx + c$ , we get:

$$a = 1$$
,  $b = -2$  and  $c = 3k$ 

It is given that  $\alpha$  and  $\beta$  are the roots of the polynomial.

$$\therefore \alpha + \beta = \frac{-b}{a}$$

$$\Rightarrow \alpha + \beta = -\left(\frac{-2}{1}\right)$$

$$\Rightarrow \alpha + \beta = 2$$
 ....(i)

Also, 
$$\alpha \beta = \frac{c}{a}$$

$$\Rightarrow \alpha \beta = \frac{3k}{1}$$

$$\Rightarrow \alpha \beta = 3k$$
 ....(ii)

Now, 
$$\alpha + \beta = \alpha \beta$$

$$\Rightarrow$$
 2 = 3k [Using (i) and (ii)]

$$\Rightarrow k = \frac{2}{3}$$

4.

### Sol:

$$(c)\,\frac{5}{2}$$

Let the zeroes of the polynomial be  $\alpha$  and  $\alpha + 4$ 

Here, 
$$p(x) = 4x^2 - 8kx + 9$$

Comparing the given polynomial with  $ax^2 + bx + c$ , we get:

$$a = 4$$
,  $b = -8k$  and  $c = 9$ 

Now, sum of the roots = 
$$\frac{-b}{a}$$

$$\Rightarrow \alpha + \alpha + 4 = \frac{-(-8)}{4}$$

$$\Rightarrow 2\alpha + 4 = 2k$$

$$\Rightarrow \alpha + 2 = k$$

$$\Rightarrow \alpha = (k-2)$$
 ....(i)

Also, product of the roots,  $\alpha \beta = \frac{c}{a}$ 

$$\Rightarrow \alpha (\alpha + 4) = \frac{9}{4}$$

$$\Rightarrow$$
 (k-2) (k-2+4) =  $\frac{9}{4}$ 

$$\Rightarrow$$
  $(k-2)(k+2) = \frac{9}{4}$ 

$$\Rightarrow$$
 k<sup>2</sup> - 4 =  $\frac{9}{4}$ 

$$\Rightarrow 4k^2 - 16 = 9$$

$$\Rightarrow 4k^2 = 25$$

$$\Rightarrow$$
 k<sup>2</sup> =  $\frac{25}{4}$ 

$$\Rightarrow k = \frac{5}{2}$$
 (: k >0)

## 5. Sol:

Here, 
$$p(x) = x^2 + 2x - 195$$

Let 
$$p(x) = 0$$

$$\Rightarrow x^2 + (15 - 13)x - 195 = 0$$

$$\Rightarrow$$
 x<sup>2</sup> + 15x - 13x - 195 = 0

$$\Rightarrow$$
 x (x + 15) - 13(x + 15) = 0

$$\Rightarrow (x+15)(x-13) = 0$$

$$\Rightarrow$$
 x = -15, 13

Hence, the zeroes are -15 and 13.

### **6.**

### Sol:

$$(a+9)x^2 - 13x + 6a = 0$$

Here, 
$$A = (a^2 + 9)$$
,  $B = 13$  and  $C = 6a$   
Let  $\alpha$  and  $\frac{1}{\alpha}$  be the two zeroes.

Then, product of the zeroes =  $\frac{c}{A}$ 

$$\Rightarrow \alpha \cdot \frac{1}{\alpha} = \frac{6a}{a^2 + 9}$$
$$\Rightarrow 1 = \frac{6a}{a^2 + 9}$$

$$\Rightarrow 1 = \frac{6a}{a^2 + 9}$$

$$\Rightarrow a^2 + 9 = 6a$$

$$\Rightarrow$$
  $a^2 - 6a + 9 = 0$ 

$$\Rightarrow a^2 - 2 \times a \times 3 + 3^2 = 0$$

$$\Rightarrow$$
  $(a-3)^2 = 0$ 

$$\Rightarrow$$
 a - 3 = 0

$$\Rightarrow$$
 a = 3

7.

### Sol:

It is given that the two roots of the polynomial are 2 and -5.

Let 
$$\alpha = 2$$
 and  $\beta = -5$ 

Now, the sum of the zeroes,  $\alpha + \beta = 2 + (-5) = -3$ 

Product of the zeroes,  $\alpha \beta = 2 \times (-5) = -15$ 

∴ Required polynomial =  $x^2 - (\alpha + \beta)x + \alpha\beta$ 

$$= x^2 - (-3)x + 10$$

$$= x^2 + 3x - 10$$

8.

### Sol:

The given polynomial =  $x^3 - 3x^2 + x + 1$  and its roots are (a - b), a and (a + b). Comparing the given polynomial with  $Ax^3 + Bx^2 + Cx + D$ , we have:

$$A = 1$$
,  $B = -3$ ,  $C = 1$  and  $D = 1$ 

Now, 
$$(a - b) + a + (a + b) = \frac{-B}{A}$$

$$\Rightarrow$$
 3 a =  $-\frac{-3}{1}$ 

$$\Rightarrow$$
 a = 1

Also, 
$$(a - b) \times a \times (a + b) = \frac{-D}{A}$$

$$\Rightarrow$$
 a (a<sup>2</sup> - b<sup>2</sup>) =  $\frac{-1}{1}$ 

$$\Rightarrow 1 (1^2 - b^2) = -1$$

$$\Rightarrow 1 - b^2 = -1$$

$$\Rightarrow$$
 b<sup>2</sup> = 2

$$\Rightarrow b = \pm \sqrt{2}$$

$$\therefore$$
 a = 1 and b =  $\pm\sqrt{2}$ 

9.

#### Sol:

Let 
$$p(x) = x^3 + 4x^2 - 3x - 18$$

Now, 
$$p(2) = 2^3 + 4 \times 2^2 - 3 \times 2 - 18 = 0$$

 $\therefore$  2 is a zero of p(x).

### 10.

### Sol:

Given:

Sum of the zeroes = -5

Product of the zeroes = 6

∴ Required polynomial =  $x^2$  – (sum of the zeroes) x + product of the zeroes =  $x^2$  – (-5) x + 6 =  $x^2$  + 5x + 6

### 11.

### Sol:

Let  $\alpha$ ,  $\beta$  and  $\gamma$  are the zeroes of the required polynomial.

Then we have:

$$\alpha + \beta + \gamma = 3 + 5 + (-2) = 6$$

$$\alpha\beta + \beta\gamma + \gamma\alpha = 3 \times 5 + 5 \times (-2) + (-2) \times 3 = -1$$
and 
$$\alpha\beta\gamma = 3 \times 5 \times -2 = -30$$
Now, 
$$p(x) = x^3 - x^2(\alpha + \beta + \gamma) + x(\alpha\beta + \beta\gamma + \gamma\alpha) - \alpha\beta\gamma$$

$$= x^3 - x^2 \times 6 + x \times (-1) - (-30)$$

$$= x^3 - 6x^2 - x + 30$$

So, the required polynomial is  $p(x) = x^3 - 6x^2 - x + 30$ .

### **12.**

#### Sol:

Given: 
$$p(x) = x^3 + 3x^2 - 5x + 4$$
  
Now,  $p(2) = 2^3 + 3(2^2) - 5(2) + 4$   
 $= 8 + 12 - 10 + 4$   
 $= 14$ 

## **13.**

Given: 
$$f(x) = x^3 + 4x^2 + x - 6$$
  
Now,  $f(-2) = (-2)^3 + 4(-2)^2 + (-2) - 6$   
 $= -8 + 16 - 2 - 6$   
 $= 0$   
 $\therefore$  (x + 2) is a factor of  $f(x) = x^3 + 4x^2 + x - 6$ .

**Maths** 

14.

Sol:

Given: 
$$p(x) = 6x^3 + 3x^2 - 5x + 1$$
  
=  $6x^3 - (-3)x^2 + (-5)x - 1$ 

Comparing the polynomial with  $x^3 - x^2(\alpha + \beta + \gamma) + x(\alpha\beta + \beta\gamma + \gamma\alpha) - \alpha\beta\gamma$ , we get:

$$\alpha\beta + \beta\gamma + \gamma\alpha = -5$$

and 
$$\alpha \beta \gamma = -1$$

$$\therefore \left( \frac{1}{\alpha} + \frac{1}{\beta} + \frac{1}{\gamma} \right)$$

$$= \left(\frac{\beta\gamma + \alpha\gamma + \alpha\beta}{\alpha\beta\gamma}\right)$$

$$= \left(\frac{-5}{-1}\right)$$

= 5

**15.** 

Sol:

Given: 
$$x^2 - 5x + k$$

The co-efficients are a = 1, b = -5 and c = k.

$$\therefore \alpha + \beta = \frac{-b}{a}$$

$$\Rightarrow \alpha + \beta = \frac{(-5)}{1}$$

$$\Rightarrow \alpha + \beta = 5$$
 ....(1)

Also, 
$$\alpha - \beta = 1$$
 .....(2)

From (1) and (2), we get:

$$2\alpha = 6$$

$$\Rightarrow \alpha = 3$$

Putting the value of  $\alpha$  in (1), we get  $\beta = 2$ .

Now, 
$$\alpha \beta = \frac{c}{a}$$

$$\Rightarrow 3 \times 2 = \frac{k}{1}$$

$$\therefore$$
 k = 6

**16.** 

Sol:

Let 
$$t = x^2$$

So, 
$$f(t) = t^2 + 4t + 6$$

Now, to find the zeroes, we will equate f(t) = 0

$$\Rightarrow t^2 + 4t + 6 = 0$$

Now, 
$$t = \frac{-4 \pm \sqrt{16-24}}{2}$$
  
=  $\frac{-4 \pm \sqrt{-8}}{2}$   
=  $-2 \pm \sqrt{-2}$   
i.e.,  $x^2 = -2 \pm \sqrt{-2}$ 

 $\Rightarrow$  x =  $\sqrt{-2 \pm \sqrt{-2}}$ , which is not a real number.

The zeroes of a polynomial should be real numbers.

 $\therefore$ The given f(x) has no zeroes.

**17.** 

Sol:

$$p(x) = x^3 - 6x^2 + 11x - 6 \text{ and its factor, } x + 3$$
Let us divide p(x) by (x - 3).
Here,  $x^3 - 6x^2 + 11x - 6 = (x - 3)(x^2 - 3x + 2)$ 

$$= (x - 3)[(x^2 - (2 + 1)x + 2]$$

$$= (x - 3)(x^2 - 2x - x + 2)$$

$$= (x - 3)[x(x - 2) - 1(x - 2)]$$

$$= (x - 3)(x - 1)(x - 2)$$

∴The other two zeroes are 1 and 2.

18.

Sol:

Given: 
$$p(x) = 2x^4 - 3x^3 - 3x^2 + 6x - 2$$
 and the two zeroes,  $\sqrt{2}$  and  $-\sqrt{2}$   
So, the polynomial is  $(x + \sqrt{2})(x - \sqrt{2}) = x^2 - 2$ .  
Let us divide  $p(x)$  by  $(x^2 - 2)$   
Here,  $2x^4 - 3x^3 - 3x^2 + 6x - 2 = (x^2 - 2)(2x^2 - 3x + 1)$   
 $= (x^2 - 2)[(2x^2 - (2 + 1)x + 1]$   
 $= (x^2 - 2)(2x^2 - 2x - x + 1)$   
 $= (x^2 - 2)[(2x(x - 1) - 1(x - 1)]$   
 $= (x^2 - 2)(2x - 1)(x - 1)$ 

The other two zeroes are  $\frac{1}{2}$  and 1.

**19.** 

Sol:

Given:  $p(x) = 3x^4 + 5x^3 - 7x^2 + 2x + 2$ Dividing p(x) by  $(x^2 + 3x + 1)$ , we have:

$$x^{2} + 3x + 1$$

$$3x^{4} + 5x^{3} - 7x^{2} + 2x + 2$$

$$3x^{4} + 9x^{3} + 3x^{2}$$

$$- - - -$$

$$-4x^{3} - 10x^{2} + 2x + 2$$

$$-4x^{3} - 12x^{2} - 4x$$

$$+ + + +$$

$$2x^{2} + 6x + 2$$

$$2x^{2} + 6x + 2$$

$$- - - -$$

$$x$$

∴ The quotient is  $3x^2 - 4x + 2$ 

20.

Sol:

Let 
$$p(x) = x^3 + 2x^2 + kx + 3$$
  
Now,  $p(3) = (3)^3 + 2(3)^2 + 3k + 3$   
 $= 27 + 18 + 3k + 3$   
 $= 48 + 3k$ 

It is given that the reminder is 21

$$3k + 48 = 21$$

$$\Rightarrow$$
3k = -27

$$\Rightarrow$$
k = -9