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RS Aggarwal Class 9 Mathematics Solutions  
Areas

Exercise 7A

Question 1:

Here,  $b = 24$  cm and  $h = 14.5$  cm

$$\begin{aligned}\text{Area of triangle} &= \left( \frac{1}{2} \times \text{base} \times \text{height} \right) \text{sq units} \\ &= \left( \frac{1}{2} \times 24 \times 14.5 \right) \text{cm}^2 \\ &= 174 \text{ cm}^2\end{aligned}$$

Question 2:

Let height =  $x$  and base =  $3x$

$$\text{Area of triangle} = \left( \frac{1}{2} \times \text{base} \times \text{height} \right) \text{sq units}$$

$$\begin{aligned}\therefore \text{Area of triangle} &= \frac{1}{2} \times x \times 3x \\ &= \frac{3}{2}x^2\end{aligned}$$

We know that, 1 hectare = 10000 sq metre

Rate of sowing the field per hectare = Rs.58

Total cost of sowing the triangular field = Rs.783

$$\Rightarrow \text{Total cost} = \text{Area of the triangular field} \times \text{Rs. 58}$$

$$\Rightarrow \frac{3}{2}x^2 \times \frac{58}{10000} = 783$$

$$\Rightarrow x^2 = \frac{783}{58} \times \frac{2}{3} \times 10000 \text{ sq metre}$$

$$\Rightarrow x^2 = 90000 \text{ sq metre}$$

$$\Rightarrow x = 300 \text{ m}$$

Hence, height = 300 m and base = 900 m.

Question 3:

Here,  $a = 42$  cm,  $b = 34$  cm and  $c = 20$  cm

$$\text{Therefore, } s = \frac{42 + 34 + 20}{2} = 48$$

$$\begin{aligned}\text{Area} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{48(48-42)(48-34)(48-20)} \\ &= \sqrt{48 \times 6 \times 14 \times 28} \\ &= \sqrt{4 \times 4 \times 3 \times 3 \times 2 \times 14 \times 14 \times 2} \\ &= 4 \times 3 \times 2 \times 14 \\ &= 336 \text{ cm}^2\end{aligned}$$

Longest side = 42 cm

$$\Rightarrow b = 42 \text{ cm}$$

Let  $h$  be the height corresponding to the longest side.

$$\text{Area of the triangle} = \frac{1}{2} \times b \times h$$

$$\Rightarrow \frac{1}{2} \times b \times h = 336$$

$$\Rightarrow 42 \times h = 336 \times 2$$

$$\Rightarrow h = \frac{336 \times 2}{42} = 16 \text{ cm}$$

**Question 4:**

Here,  $a = 18$  cm,  $b = 24$  cm and  $c = 30$  cm

$$\text{Therefore, } s = \frac{18 + 24 + 30}{2} = 36$$

$$\begin{aligned}\text{Area} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{36(36-18)(36-24)(36-30)} \\ &= \sqrt{36 \times 18 \times 12 \times 6} \\ &= \sqrt{6 \times 6 \times 6 \times 3 \times 3 \times 4 \times 6} \\ &= 6 \times 6 \times 3 \times 2 \\ &= 216 \text{ cm}^2\end{aligned}$$

Smallest side = 18 cm

Let  $h$  be the height corresponding to the smallest side.

$$\text{Area of the triangle} = \frac{1}{2} \times b \times h$$

$$\Rightarrow \frac{1}{2} \times b \times h = 216$$

$$\Rightarrow 18 \times h = 216 \times 2$$

$$\Rightarrow h = \frac{216 \times 2}{18} = 24 \text{ cm}$$

**Question 5:**

Here,  $a = 91$  m,  $b = 98$  m and  $c = 105$  m

$$\text{Therefore, } s = \frac{91+98+105}{2} = \frac{294}{2} = 147$$

$$\begin{aligned}\text{Area} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{147(147-91)(147-98)(147-105)} \\ &= \sqrt{147 \times 56 \times 49 \times 42} \\ &= \sqrt{49 \times 3 \times 7 \times 2 \times 2 \times 2 \times 49 \times 7 \times 3 \times 2} \\ &= 49 \times 3 \times 2 \times 2 \times 7 \\ &= 4116 \text{ m}^2\end{aligned}$$

Longest side = 105m  $\Rightarrow$   $b=105$

Let  $h$  be the height corresponding to the longest side.

$$\text{Area of the triangle} = \frac{1}{2} \times b \times h$$

$$\Rightarrow \frac{1}{2} \times b \times h = 4116$$

$$\Rightarrow 105 \times h = 2 \times 4116$$

$$\Rightarrow h = \frac{2 \times 4116}{105} = 78.4 \text{ m}$$

**Question 6:**

Let the sides of the triangle be  $5x$ ,  $12x$  and  $13x$ .

Its perimeter =  $(5x + 12x + 13x) = 30x$

$\therefore 30x = 150$  m [given]

$$\Rightarrow x = \frac{150}{30} = 5 \text{ m}$$

Thus, sides of the triangle are;

$$5x = 5 \times 5 = 25 \text{ m}$$

$$12x = 12 \times 5 = 60 \text{ m}$$

$$13x = 13 \times 5 = 65 \text{ m}$$

Let  $a = 25$  m,  $b = 60$  m and  $c = 65$  m.

$$\begin{aligned}\text{Now } s &= \frac{1}{2}(a+b+c) \\ &= \left(\frac{25+60+65}{2}\right) \text{ m} = \frac{150}{2} = 75 \text{ m.}\end{aligned}$$

$$\begin{aligned}\therefore \text{ area of the triangle} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{75(75-25)(75-60)(75-65)} \\ &= \sqrt{75 \times 50 \times 15 \times 10} \\ &= \sqrt{25 \times 3 \times 25 \times 2 \times 5 \times 3 \times 5 \times 2} \\ &= \sqrt{25 \times 25 \times 5 \times 5 \times 3 \times 3 \times 2 \times 2} \\ &= 25 \times 5 \times 3 \times 2 = 750 \text{ sq m.}\end{aligned}$$

$\therefore$  area of the triangle = 750 sq m.

**Question 7:**

Let the sides of the triangle be  $25x$ ,  $17x$  and  $12x$ .

Then, its perimeter =  $(25x + 17x + 12x) = 54x$

$$\Rightarrow 54x = 540$$

$$\Rightarrow x = \frac{540}{54} = 10\text{m.}$$

Thus, sides of the triangle are :

$$25x = 25 \times 10 = 250 \text{ m}$$

$$17x = 17 \times 10 = 170 \text{ m}$$

$$12x = 12 \times 10 = 120 \text{ m}$$

Let,  $a = 250 \text{ m}$ ,  $b = 170 \text{ m}$  and  $c = 120 \text{ m}$

$$\begin{aligned} \text{Now, } s &= \frac{1}{2}(a+b+c) \\ &= \left(\frac{250+170+120}{2}\right)\text{m} \\ &= \left(\frac{540}{2}\right)\text{m} = 270\text{m} \end{aligned}$$

$$\begin{aligned} \therefore \text{ area of the triangle} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{270(270-250)(270-170)(270-120)} \\ &= \sqrt{3 \times 3 \times 3 \times 10 \times 10 \times 2 \times 10 \times 10 \times 5 \times 3} \\ &= 3 \times 3 \times 10 \times 10 \times 10 = 9000\text{m}^2 \end{aligned}$$

$\therefore$  Cost of ploughing the field at the rate of Rs. 18.80 per  $10\text{m}^2$

$$= \frac{18.80}{10} \times 9000 = \text{Rs. } 16920$$

$\therefore$  Cost of ploughing the field = Rs. 16920.

#### Question 8:

One side of a triangular field = 85 m

Second side of a triangular field = 154 m

Let the third side of a triangular field be  $x \text{ m}$

Perimeter (given) = 324 m

$$\therefore 85\text{m} + 154\text{m} + x\text{m} = 324 \text{ m}$$

$$\Rightarrow x = 324 - 239$$

$$\Rightarrow x = 85 \text{ m}$$

$\therefore$  the third side = 85 m

Let  $a = 85 \text{ m}$ ,  $b = 154 \text{ m}$  and  $c = 85 \text{ m}$

$$\begin{aligned} \text{Now } S &= \frac{1}{2}(a+b+c) \\ &= \left(\frac{85+154+85}{2}\right) = \frac{324}{2} = 162 \end{aligned}$$

$$\begin{aligned} \therefore \text{ area of the triangle} &= \sqrt{S(S-a)(S-b)(S-c)} \\ &= \sqrt{162(162-85)(162-154)(162-85)} \\ &= \sqrt{162 \times 77 \times 8 \times 77} \\ &= \sqrt{2 \times 9 \times 9 \times 7 \times 11 \times 2 \times 2 \times 2 \times 7 \times 11} \\ &= \sqrt{11 \times 11 \times 9 \times 9 \times 7 \times 7 \times 2 \times 2 \times 2 \times 2} \\ &= 11 \times 9 \times 7 \times 2 \times 2 = 2772 \text{ m}^2 \end{aligned}$$

$\therefore$  area of triangle =  $2772 \text{ m}^2$

Also, area of triangle =  $\frac{1}{2} \times \text{base} \times \text{height}$

$$2772 = \frac{1}{2} \times 154 \times h = 77h$$

$$\therefore 77h = 2772$$

$$\therefore h = \frac{2772}{77} = 36 \text{ m}$$

$\therefore$  the length of the perpendicular from the opposite vertex on the side measuring 154 m = 36 m.

#### Question 9:

Let  $a = 13$  cm,  $b = 13$  cm and  $c = 20$  cm

$$\begin{aligned}\text{Now, } s &= \frac{1}{2}(a+b+c) \\ &= \left(\frac{13+13+20}{2}\right) \text{ cm} = \frac{46}{2} = 23 \text{ cm}\end{aligned}$$

$$\begin{aligned}\therefore \text{ area of the triangle} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{23(23-13)(23-13)(23-20)} \\ &= \sqrt{23 \times 10 \times 10 \times 3} \\ &= 10\sqrt{69} \\ &= 10 \times 8.306 = 83.06 \text{ cm}^2\end{aligned}$$

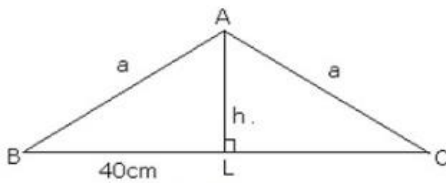
$\therefore$  area of an isosceles triangle =  $83.06 \text{ cm}^2$

**Question 10:**

Let  $\triangle ABC$  be an isosceles triangle and Let  $AL \perp BC$ .

Given that  $BC = 80$  cm and Area of  $\triangle ABC = 360 \text{ cm}^2$

$$\begin{aligned}\therefore \frac{1}{2} \times BC \times AL &= 360 \text{ cm}^2 \\ \Rightarrow \frac{1}{2} \times 80 \times h &= 360 \text{ cm}^2 \\ \Rightarrow 40 \times h &= 360 \text{ cm}^2 \\ \Rightarrow h &= \frac{360}{40} = 9 \text{ cm}\end{aligned}$$



$$\begin{aligned}\text{Now } BL &= \frac{1}{2}(BC) \\ &= \left(\frac{1}{2} \times 80\right) \text{ cm} = 40 \text{ cm and } AL = 9 \text{ cm} \\ a &= \sqrt{BL^2 + AL^2} \\ &= \sqrt{(40)^2 + (9)^2} \Rightarrow \sqrt{1600 + 81} \\ \Rightarrow \sqrt{1681} &= 41 \text{ cm}\end{aligned}$$

$\therefore$  Perimeter =  $(41 + 41 + 80) = 162$  cm  
Perimeter of the triangle = 162 cm.

**Question 11:**

In an isosceles triangle, the lateral sides are of equal length.

Let the length of lateral side be  $x$  cm.

Then, base =  $\frac{3}{2} \times x$  cm [given]

(i) Length of each side of the triangle :

Perimeter of an isosceles triangle = 42 cm

$$\Rightarrow x + x + \frac{3}{2}x = 42 \text{ cm}$$

$$\Rightarrow 2x + 2x + 3x = 84 \text{ cm}$$

$$\Rightarrow 7x = 84$$

$$\Rightarrow x = \frac{84}{7} = 12 \text{ cm}$$

$\therefore$  length of lateral side = 12 cm

$$\text{And base} = \frac{3}{2}x = \frac{3}{2} \times 12 = 18 \text{ cm}$$

$\therefore$  the length of each side of the triangle = 12 cm, 12 cm and 18 cm.

(ii) Area of the triangle :

Let  $a = 12$  cm,  $b = 12$  cm and  $c = 18$  cm.

$$\text{Now, } s = \frac{1}{2}(a + b + c)$$

$$= \left( \frac{12 + 12 + 18}{2} \right) \text{ cm} = \left( \frac{42}{2} \right) \text{ cm}$$

$$= 21 \text{ cm}$$

$$\therefore \text{ area of the triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{21(21-12)(21-12)(21-18)}$$

$$= \sqrt{21 \times 9 \times 9 \times 3}$$

$$= \sqrt{3 \times 7 \times 9 \times 9 \times 3}$$

$$= 27\sqrt{7} = 71.42 \text{ cm}^2 \quad (\sqrt{7} = 2.64)$$

$$\therefore \text{ area of the triangle} = 71.42 \text{ cm}^2.$$

(iii) Height of the triangle :

Area of a triangle =  $\frac{1}{2}$  x base x height

$$71.42 \text{ cm}^2 = \frac{1}{2} \times 18 \times h$$

$$\Rightarrow 71.42 \text{ cm}^2 = 9 \times h$$

$$\Rightarrow h = \frac{71.42}{9} = 7.94 \text{ cm}$$

$\therefore$  the height of the triangle = 7.94 cm.

#### Question 12:

Let  $a$  be the length of a side of an equilateral triangle.

$$\therefore \text{ Area of an equilateral triangle} = \frac{\sqrt{3} \times a^2}{4} \text{ sq units}$$

Area of the equilateral triangle =  $36\sqrt{3} \text{ cm}^2$  [given]

$$\Rightarrow \frac{\sqrt{3} \times a^2}{4} = 36 \times \sqrt{3}$$

$$\Rightarrow a^2 = \frac{36 \times \sqrt{3} \times 4}{\sqrt{3}}$$

$$\Rightarrow a^2 = 36 \times 4 = 144$$

$$\therefore a = \sqrt{144} = 12 \text{ cm}$$

Perimeter of an equilateral triangle =  $3 \times a$

Since,  $a = 12$  cm,

$$\text{Perimeter} = (3 \times 12) \text{ cm} = 36 \text{ cm}$$

#### Question 13:

Let  $a$  be the length of the side of an equilateral triangle

$$\therefore \text{Area of an equilateral triangle} = \frac{\sqrt{3}}{4} a^2 \text{ sq units}$$

$$\text{Area of the equilateral triangle} = 81\sqrt{3} \text{ cm}^2 \quad [\text{given}]$$

$$\Rightarrow 81\sqrt{3} \text{ cm}^2 = \frac{\sqrt{3}}{4} a^2$$

$$\Rightarrow a^2 = \frac{81\sqrt{3} \times 4}{\sqrt{3}} = 324$$

$$\Rightarrow a = \sqrt{324} = 18 \text{ cm}$$

$$\text{Height of an equilateral triangle} = \frac{\sqrt{3}}{2} a$$

Since  $a = 18$  cm,

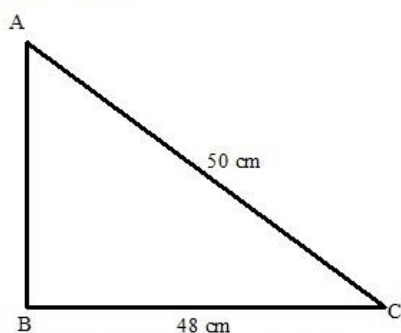
$$\text{Height of the equilateral triangle} = \frac{\sqrt{3}}{2} \times 18 = 9\sqrt{3} \text{ cm.}$$

**Question 14:**

Base of the right triangle is  $BC = 48$  cm

Hypotenuse of the right triangle is  $AC = 50$  cm

Let  $AB = x$  cm



By Pythagoras Theorem, we have,

$$AC^2 = AB^2 + BC^2$$

That is we have

$$50^2 = x^2 + 48^2$$

$$\Rightarrow x^2 = 50^2 - 48^2$$

$$\Rightarrow x^2 = 2500 - 2304 = 196$$

$$\Rightarrow x = \sqrt{196} = 14 \text{ cm}$$

$$\therefore \text{Area of the right angle triangle} = \frac{1}{2} \times \text{base} \times \text{height}$$

$$= \frac{1}{2} \times 48 \times 14$$

$$= (24 \times 14) \text{ cm}^2 = 336 \text{ cm}^2$$

$$\therefore \text{Area of the triangle} = 336 \text{ cm}^2$$

**Question 15:**

$$(i) \text{ Area of an equilateral triangle} = \frac{\sqrt{3}}{4} a^2$$

Where  $a$  is the side of the equilateral triangle

$$\begin{aligned} \therefore \text{area} &= \frac{\sqrt{3}}{4} \times 8^2 \\ &= \frac{\sqrt{3}}{4} \times 64 \Rightarrow \sqrt{3} \times 16 \\ &= 1.732 \times 16 \\ &= 27.712 = 27.71 \text{cm}^2. \quad \left[ \begin{array}{l} \text{correct upto 2} \\ \text{decimal places} \end{array} \right] \end{aligned}$$

$$\begin{aligned} \text{(ii) Height of an equilateral triangle} &= \frac{\sqrt{3}}{2} a \\ &= \frac{\sqrt{3}}{2} \times 8 \\ &= \sqrt{3} \times 4 \\ &= 1.732 \times 4 = 6.928 \\ &= 6.93 \text{cm} \quad \left[ \begin{array}{l} \text{Correct upto 2} \\ \text{decimal places} \end{array} \right] \end{aligned}$$

**Question 16:**

Let a be the side of an equilateral triangle.

$$\therefore \text{Height of an equilateral triangle} = \frac{\sqrt{3}}{2} a \text{ units}$$

Height of an equilateral triangle = 9cm [given]

$$\Rightarrow \frac{\sqrt{3}}{2} a = 9$$

$$\Rightarrow a = \frac{9 \times 2}{\sqrt{3}}$$

$$\Rightarrow = \frac{9 \times 2 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} \quad \text{[Rationalizing the denominator]}$$

$$\Rightarrow = \frac{9 \times 2\sqrt{3}}{\sqrt{3} \times \sqrt{3}}$$

$$\Rightarrow a = 6\sqrt{3}$$

$$\Rightarrow \text{base} = 6\sqrt{3}$$

$$\begin{aligned} \text{Area of the equilateral triangle} &= \frac{1}{2} \times \text{base} \times \text{height} \\ &= \frac{1}{2} \times 6\sqrt{3} \times 9 \quad [\because \text{base} = 6\sqrt{3} \text{ and height} = 9\text{cm}] \\ &= 27\sqrt{3} \end{aligned}$$

$$\begin{aligned} \text{Area of the equilateral triangle} &= 27 \times 1.732 = 46.764 \\ &= 46.76 \text{cm}^2 \\ &\quad \text{[Correct to 2 places of decimal]} \end{aligned}$$

**Question 17:**

Let a=50cm, b=20cm and c=50cm.

Let us find s:

$$\begin{aligned} s &= \frac{1}{2}(a+b+c) \\ &= \left( \frac{50+20+50}{2} \right) \text{cm} = \left( \frac{120}{2} \right) \text{cm} \\ &= 60 \text{cm} \end{aligned}$$

Now, area of one triangular piece of cloth

$$\begin{aligned} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{60(60-50)(60-20)(60-50)} \\ &= \sqrt{60 \times 10 \times 40 \times 10} \\ &= \sqrt{6 \times 10 \times 10 \times 4 \times 10 \times 10} \\ &= \sqrt{10 \times 10 \times 10 \times 10 \times 2 \times 2 \times 2 \times 3} \\ &= 10 \times 10 \times 2\sqrt{6} \\ &= 200\sqrt{6} = 200 \times 2.45 = 490 \text{cm}^2 \end{aligned}$$

$$\therefore \text{area of one piece of cloth} = 490 \text{cm}^2$$

$$\text{Now area of 12 pieces} = (12 \times 490) \text{cm}^2 = 5880 \text{cm}^2$$



**Question 18:**

Let,  $a = 16$  cm,  $b = 12$  and  $c = 20$  cm

Let us now find  $s$ :

$$\begin{aligned}s &= \frac{1}{2}(a + b + c) \\ &= \left(\frac{16 + 12 + 20}{2}\right) \text{ cm} = \left(\frac{48}{2}\right) \text{ cm} \\ &= 24 \text{ cm}\end{aligned}$$

$$\begin{aligned}\text{Area of one triangular tile} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{24(24-16)(24-12)(24-20)} \\ &= \sqrt{2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3} \\ &= 2 \times 2 \times 2 \times 2 \times 2 \times 3 \\ &= 96 \text{ cm}^2\end{aligned}$$

$$\therefore \text{Area of one tile} = 96 \text{ cm}^2$$

$$\Rightarrow \text{Area of 16 tiles} = 96 \times 16 = 1536 \text{ cm}^2$$

Cost of polishing the tiles per sq.cm = Re.1

$$\begin{aligned}\text{Thus, the total cost of polishing all the tiles} &= \text{Rs. } (1 \times 1536) \\ &= \text{Rs. } 1536.\end{aligned}$$

**Question 19:**

Consider the right triangle ABC.

By Pythagoras Theorem, we have,

$$\begin{aligned}BC &= \sqrt{AB^2 - AC^2} \\ &= \sqrt{17^2 - 15^2} \\ &= \sqrt{289 - 225} \\ &= \sqrt{64} \\ &= 8 \text{ cm}\end{aligned}$$

$$\text{Perimeter of quad. ABCD} = 17 + 9 + 12 + 8 = 46 \text{ cm}$$

$$\begin{aligned}\text{Area of triangle } \triangle ABC &= \frac{1}{2} \times \text{base} \times \text{height} \\ &= \frac{1}{2} \times BC \times AC \\ &= \frac{1}{2} \times 8 \times 15 \\ &= 60 \text{ cm}^2\end{aligned}$$

For area of triangle ACD,

Let  $a = 15$  cm,  $b = 12$  cm and  $c = 9$  cm

$$\text{Therefore, } s = \frac{a+b+c}{2} = \frac{15+12+9}{2} = 18 \text{ cm}$$

$$\begin{aligned}\text{Area of } \triangle ACD &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{18(18-15)(18-12)(18-9)} \\ &= \sqrt{18 \times 3 \times 6 \times 9} \\ &= \sqrt{18 \times 18 \times 3 \times 3} \\ &= 18 \times 3 = 54 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Thus the area of quad. ABCD} &= \text{Area of } \triangle ABC + \text{Area of } \triangle ACD \\ &= 60 + 54 = 114 \text{ cm}^2.\end{aligned}$$

**Question 20:**

Perimeter of quad. ABCD =  $34 + 29 + 21 + 42 = 126$  cm

Area of triangle BCD =  $\frac{1}{2} \times 20 \times 21 = 210$  cm<sup>2</sup>

For area of triangle ABD,

Let  $a = 42$  cm,  $b = 20$  cm and  $c = 34$  cm

Therefore,  $s = \frac{42 + 20 + 34}{2} = \frac{96}{2} = 48$  cm

$$\begin{aligned}\text{Area of } \triangle ABD &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{48(48-42)(48-20)(48-34)} \\ &= \sqrt{48 \times 6 \times 28 \times 14} \\ &= \sqrt{16 \times 3 \times 3 \times 2 \times 2 \times 14 \times 14} \\ &= 4 \times 3 \times 2 \times 14 = 336 \text{ cm}^2\end{aligned}$$

Area of quad. ABCD = Area  $\triangle$ ABD + Area  $\triangle$ BCD

Thus the area of quad. ABCD =  $336 + 210 = 546$  cm<sup>2</sup>.

**Question 21:**

Consider the right triangle ABD.

By Pythagoras Theorem, we have

$$\begin{aligned}AB &= \sqrt{BD^2 - AD^2} \\ \therefore AB &= \sqrt{26^2 - 24^2} \\ &= \sqrt{676 - 576} \\ &= \sqrt{100}\end{aligned}$$

AB = 10 cm

$\Rightarrow$  base = 10 cm

Area of the triangle ABD =  $\frac{1}{2} \times \text{base} \times \text{height}$

$\Rightarrow$  Area of  $\triangle$ ABD =  $\frac{1}{2} \times 10 \times 24$  [ $\because$  base = 10 cm, height = 24 cm]

$\Rightarrow$  Area of  $\triangle$ ABD = 120 cm<sup>2</sup>

Area of equilateral triangle BCD =  $\frac{\sqrt{3}}{4} a^2$

$\Rightarrow$   $= \frac{1.73}{4} (26)^2$  [ $a = 26$  cm,  $\sqrt{3} = 1.73$ ]

$\Rightarrow$   $= 292.37$  cm<sup>2</sup>

Area of quad. ABCD = Area of  $\triangle$ ABD + Area of  $\triangle$ BCD

$= 120 + 292.37$

$= 412.37$  cm<sup>2</sup>.

**Question 22:**

Consider the triangle ABC,

Let  $a = 26$  cm,  $b = 30$  cm and  $c = 28$  cm

$$s = \frac{26 + 30 + 28}{2} = \frac{84}{2} = 42 \text{ cm}$$

$$\begin{aligned}\text{Area of ABC} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{42(42-26)(42-30)(42-28)} \\ &= \sqrt{42 \times 16 \times 12 \times 14} \\ &= \sqrt{14 \times 3 \times 16 \times 4 \times 3 \times 14} \\ &= \sqrt{14 \times 14 \times 3 \times 3 \times 16 \times 4} \\ &= 14 \times 3 \times 4 \times 2 \\ &= 336 \text{ cm}^2\end{aligned}$$

In a parallelogram, diagonal divides the parallelogram in two equal area therefore

$$\begin{aligned}\therefore \text{Area of quad. ABCD} &= \text{Area of } \triangle ABC + \text{Area of } \triangle ACD \\ &= \text{Area of } \triangle ABC \times 2 \\ &= 336 \times 2 \\ &= 672 \text{ cm}^2.\end{aligned}$$

**Question 23:**

Consider the triangle ABC,

Let  $a = 10$  cm,  $b = 16$  cm and  $c = 14$  cm

$$s = \frac{10 + 16 + 14}{2} = \frac{40}{2} = 20$$

$$\begin{aligned}\text{Area of ABC} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{20(20-10)(20-16)(20-14)} \\ &= \sqrt{20 \times 10 \times 4 \times 6} \\ &= \sqrt{10 \times 2 \times 10 \times 4 \times 3 \times 2} \\ &= \sqrt{10 \times 10 \times 4 \times 2 \times 2 \times 3} \\ &= 10 \times 2 \times 2 \times \sqrt{3} \\ &= 40\sqrt{3} \text{ cm}^2\end{aligned}$$

In a parallelogram, diagonal divides the parallelogram in two equal area therefore

$$\begin{aligned}\therefore \text{Area of quad. ABCD} &= \text{Area of } \triangle ABC + \text{Area of } \triangle ACD \\ &= \text{Area of } \triangle ABC \times 2 \\ &= 40\sqrt{3} \times 2 \\ &= 80\sqrt{3} \text{ cm}^2 \\ &= 138.4 \text{ cm}^2 \quad [\because \sqrt{3} = 1.73]\end{aligned}$$

**Question 24:**

$$\begin{aligned}\text{Area of triangle ABD} &= \frac{1}{2} \times \text{base} \times \text{height} \\ &= \frac{1}{2} \times BD \times AL \\ &= \frac{1}{2} \times 64 \times 16.8 \\ &= 537.6 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Area of triangle BCD} &= \frac{1}{2} \times \text{base} \times \text{height} \\ &= \frac{1}{2} \times BD \times CM \\ &= \frac{1}{2} \times 64 \times 13.2 \\ &= 422.4 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}\text{Area of quad. ABCD} &= \text{Area of } \triangle ABD + \text{Area of } \triangle BCD \\ &= 537.6 + 422.4 = 960 \text{ cm}^2.\end{aligned}$$